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**NUMERO: 2245A**

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# **A P P U N T I**

**STUDENTE: Preatto Stefania**

**MATERIA: Testing. and certification - Prof. Carullo**

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IL NOME DEL PROFESSORE, SERVE SOLO PER IDENTIFICARE IL CORSO.**

PREATTO STEFANIA - 235695  
TESTING AND CERTIFICATION

- \* TRACERBILITY & COMPATIBILITY
- \* INTERNATIONAL ORGANISATION OF METROLOGY
- \* CALIBRATION PROCESS
- \* QUALITY MANAGEMENT OF MEASURING INSTRUMENTATION
- \* ANALOG-TO-DIGITAL CONVERSION PROCESS
- \* DIAGNOSTIC INSTRUMENTATION
  - DIGITAL STORAGE OSCILLOSCOPE
  - DEBUG OF DIGITAL SYSTEMS
- \* SERIAL INTERFACES
- \* DATA ACQUISITION BOARD
- \* SENSORS
- \* THERMOCOUPLES
- \* INDUSTRIAL BUSES
- \* PHOTOMETRY AND PHOTONSENSORS

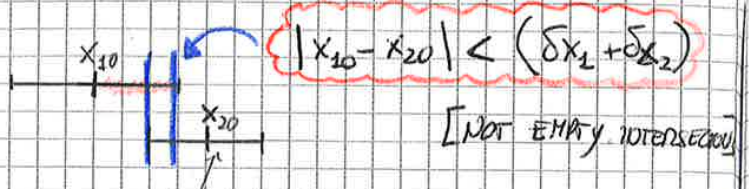
**COMPATIBILITY** → SINCE THE MEASURE (= RESULT OF A MEASUREMENT) IS AN INTERVAL EQUALITY IS NOT USEFUL IN MEASUREMENT COMPARISON

**DETERMINISTIC APPROACH:**

2 MEASUREMENTS OF THE SAME QUANTITY THAT REFER TO THE SAME CONDITIONS ARE COMPATIBLE WHEN THE INTERSECTION BETWEEN THE 2 MEASUREMENT INTERVALS IS NOT AN EMPTY SET

$$X_1 = (x_{10} \pm \delta x_1)$$

$$X_2 = (x_{20} \pm \delta x_2)$$



parameter is surely in this interval

DETERMINISTIC MODEL IS WORST CASE MODEL → WORST POSSIBLE COMBINATION CAUSE IT REFERS TO

[ex: I ordered a Resistor of 1 kΩ ; R = 1 kΩ, 1%]

[99.9 ÷ 100.1] Ω, 950 Ω is wrong]

**PROBABILISTIC APPROACH** → WE STATE THAT PARAMETER IS IN THE INTERVAL WITH A PROBABILITY:

- EXPECTED VALUES :  $x_{10}, x_{20}$

- STANDARD UNCERTAINTIES :  $u(x_1), u(x_2)$  → WHICH REMEMBER THE STANDARD DEVIATION OF A PROBABILITY DENSITY FUNCTION

IT DEPENDS ON THE SHAPE OF THE FUNCTION

COMPATIBILITY IS MET IF :  $|x_{10} - x_{20}| < k \cdot u(x_1 - x_2)$

**COVERAGE FACTOR** → AFFECTS THE CONFIDENCE LEVEL OF THE COMPARISON

IF YOU'RE CONFIDENT THAT THERE'S A NORMAL DISTRIBUTION  $k$  CAN BE FOUND IN THE TABLE OF GAUSSIAN DISTRIBUTION

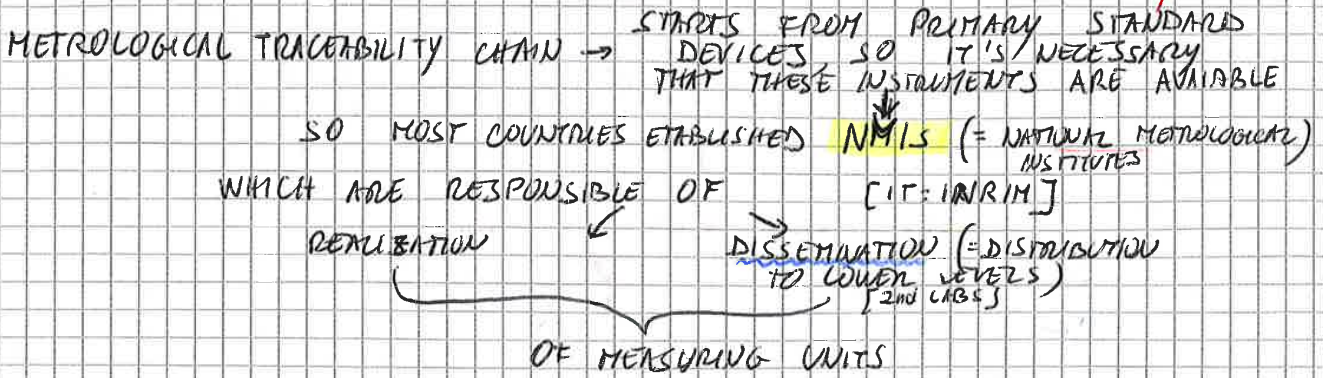
for ex: if we have 2 uncorrelated measurements (STATISTIC INDEPENDENCE)

$$|x_{10} - x_{20}| < k \sqrt{u^2(x_1) + u^2(x_2)}$$

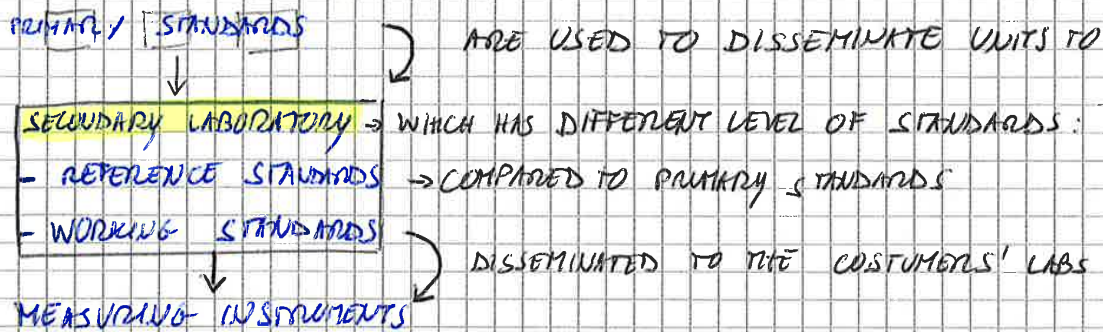
**!** USUALLY IN A COMPATIBILITY CHECK DETERMINISTIC APPROACH IS PREFERRED

CAUSE YOU HAVE TO BE SURE IF THERE IS <sup>OR</sup> NOT COMPATIBILITY IN DESIGN PROJECT WE HAVE TO WORK IN WORST CASE SO WITH DETERMINISTIC APPROACH

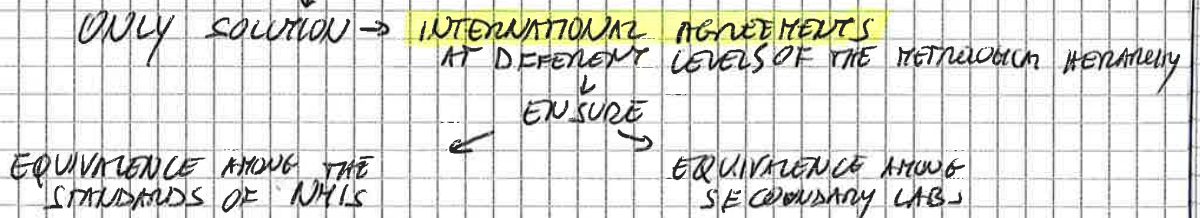
# INTERNATIONAL ORGANISATION OF METROLOGY



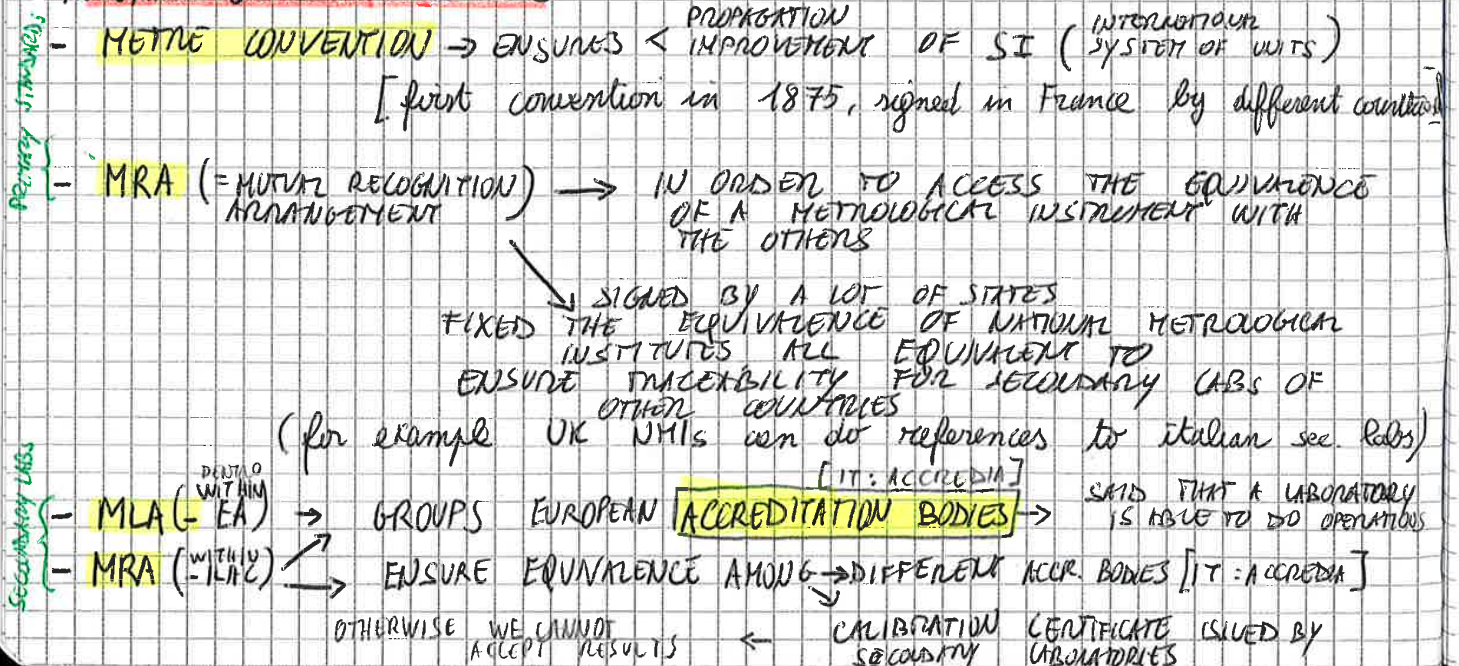
**DISSEMINATION PROCESS** IN TRACEABILITY CHAIN HAS DIFFERENT LEVELS



WE HAVE TO ENSURE THE "FREE EXCHANGE" OF THE MEASUREMENTS WHICH REQUIRE A HIGH LEVEL OF CONFIDENCE AMONG THE METROLOGICAL FACILITIES AT DIFFERENT COUNTRIES

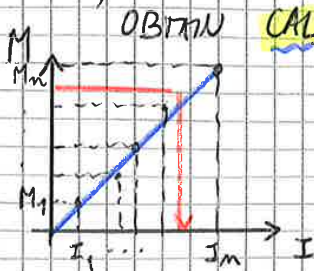


## INTERNATIONAL AGREEMENTS



TO OBTAIN CALIBRATION:

(1) WE APPLY A SET OF VALUES TO THE INSTRUMENT INPUT



OBTAIN CALIBRATION CURVE

we have from the input to the output  
we apply  $M$  and record results



WHEN YOU FIT EXPERIMENTAL DATA:

- TRY TO FIND THE MODEL THAT FITS THE EXPERIMENTAL DATA
- BASED ON PRIMARY KNOWLEDGE OF INSTRUMENTS

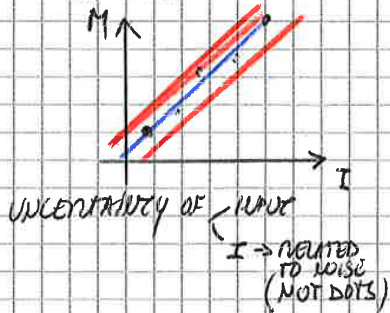
USUALLY THE MOST USED IS LINEAR BEHAVIOR  
IT ISN'T POSSIBLE TO OBTAIN PERFECT LINEAR BEHAVIOR → THE BEST FUNCTION IS A STRAIGHT LINE

ISN'T PERFECTLY REPRESENTATIVE OF LINEAR BEHAVIOR

WE TRY TO MINIMIZE SQUARE

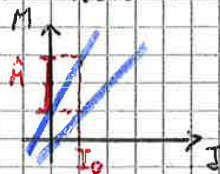


(2) WE DRAW CALIBRATION DIAGRAM TAKING THE MAIN UNCERTAINTY CONTRIBUTIONS INTO ACCOUNT



- REFERENCE-STANDARDS UNCERTAINTY → INPUT AREN'T PERFECT SO INTERVALS AREN'T EXACTED POINTS if we repeat the experiment we don't obtain the same results because of noise, environmental conditions and all quantities that affect the behavior of the instrument
- NON LINEARITY OF DEVICE
- TIME DRIFT
- etc...

ONCE THE MANUFACTURER HAS ASSIGNED THE CALIBRATION DIAGRAM



TO OBTAIN AN ESTIMATION OF THE INTERVAL

BUT ONE I/O IS NOT REPRESENTATIVE OF THE REAL INSTRUMENT

AFTER CALIBRATION INTERVAL HAS ELAPSED → YOUR MEASUREMENTS AREN'T RELIABLE  
 SO THEY CAN BE OUT OF TOLERANCE

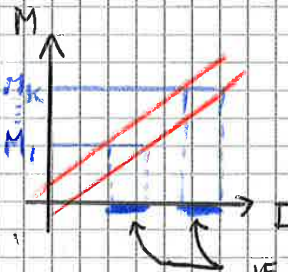
THE INSTRUMENT HAS TO BE SUBJECTED TO A VERIFICATION

2. **VERIFICATION** → IS THE SET OF OPERATIONS INTENDED TO VERIFY THE VALIDITY OF THE CALIBRATION RELATION

(During lab session we have to verify the calibration function of a DMM)

A SET OF KNOWN VALUES ARE APPLIED AT THE INSTRUMENT INPUT (We move from in to out but we know calibration function)

ERRORS BETWEEN INDICATIONS ARE COMPARED TO **MAXIMUM ADMITTED ERRORS (INSTRUMENT TOLERANCE)**



WE APPLY KNOWN INPUT VALUES AND WE RECORD THE OUTPUT

IF WE OBTAIN A MEASURE IN THIS INTERVAL THAT'S OK IF JUST ONE ISN'T IN THE INTERVAL → FAIL

IN **IDEAL SITUATION** → VERIFICATION HAS 2 POSSIBLE RESULTS

$\delta M_i = 0$

**PASS**

**FAIL**

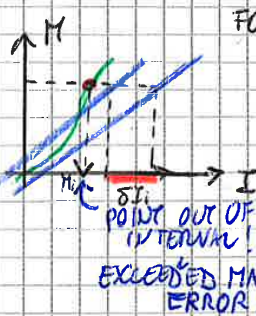
FOR ALL VERIFICATION POINTS

$S_i = |M_i - I_i| < \delta I_i, \forall i$

YOU CAN CONTINUE USING THE INSTRUMENT

$\exists i \mid S_i > \delta I_i$

EXISTS AT LEAST 1 VERIFICATION POINT WHERE THE ERROR EXCEEDS  $\delta I_i$



BUT IN **REAL SITUATION** → WE HAVE A MEASUREMENT INTERVAL  $\delta M$  TO WE HAVE TO CONSIDER FALSE RESULTS

**FALSE FAIL**

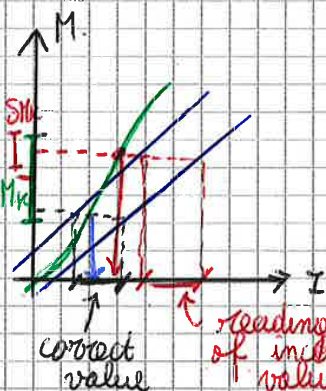
EVEN IF THE INSTRUMENT IS CONFORM TO ITS CALIBRATION RELATION ONE VALUE IS OUT OF  $\delta I$

SO IT DOESN'T PASS VERIFICATION

**FALSE PASS**

THE INSTRUMENT PASSES VERIFICATION, SO WE USE IT EVEN THOUGH IT ISN'T CONFORM TO CALIBRATION

! **VERY DANGEROUS!**  
 SITUATION SHOULD BE AVOIDED!  
 (but it isn't always possible)



PROBABILISTIC APPROACH → PROVIDES A MORE REALISTIC ESTIMATION OF THE FALSE-EVENT PROBABILITIES

STANDARDS UNCERTAINTIES (DEVIATION) → CHARACTERIZE INSTRUMENT  
STANDARD  
(INSTRUMENT)

MAIN DIFFERENCES

DETERMINISTIC	PROBABILISTIC
USES UNIFORM DISTRIBUTION	UNCERTAINTY = RANDOM VARIABLE DESCRIBED WITH A PROBABILITY DISTRIBUTION

PROBABILITY OF FALSE EVENTS DECREASES → AS THE UNCERTAINTY OF THE INPUT VALUES  $\mu_i$  DECREASES

**TUR** (= TEST UNCERTAINTY RATIO)

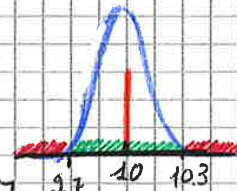
→ IS USED TO EXPRESS THE SUITABILITY OF A DEVICE TO ACT AS A REFERENCE STANDARD

= RATIO OF INSTRUMENT UNDER VERIFICATION  $I_i$  INPUT VALUE  $\mu_i$

$$TUR_i = \frac{\mu(I_i)}{\mu(\mu_i)}$$

THE HIGHEST THE TUR IS → THE LOWEST THE PROBABILITY OF FALSE EVENTS IS

2.1 PROBABILISTIC APPROACH  
IDEAL SITUATION -  $\mu(\mu_0) = 0$   
 $\mu_0 = 1.0$       $\mu(I_0) = 0.1$



DISTRIBUTION ACCORDED TO NORMAL FUNCTION

$$U(k) = k \cdot \mu(x)$$

EXTENDED UNCERTAINTY

CONFIDENCE LEVEL

$$[x_0 \pm 3 \mu(x)]$$

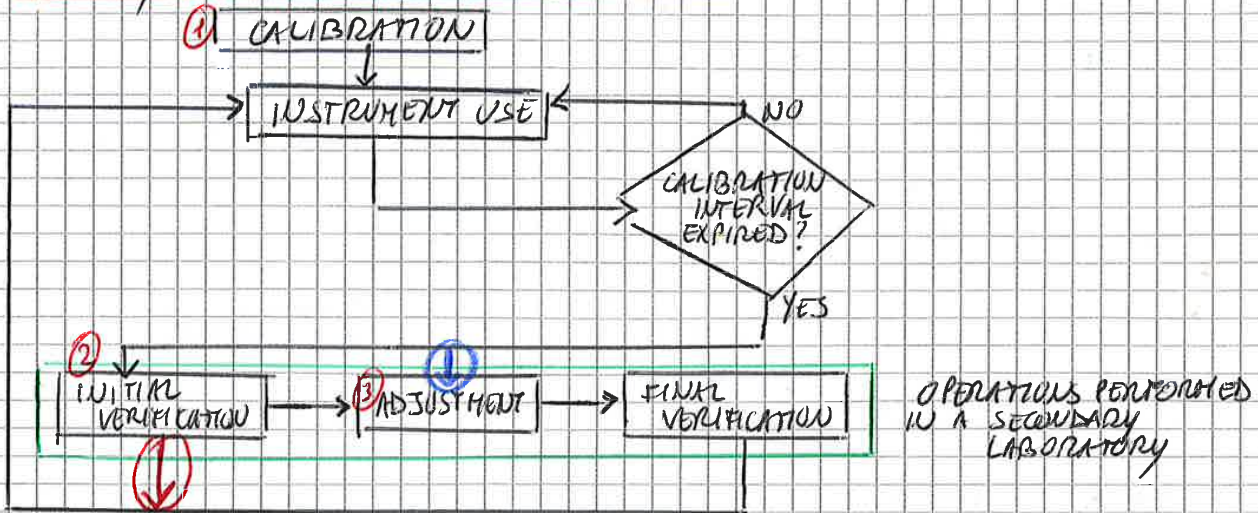
→  $k = 3$ ,  $p = 99,7\%$

$$[x_0 \pm 2 \mu(x)]$$

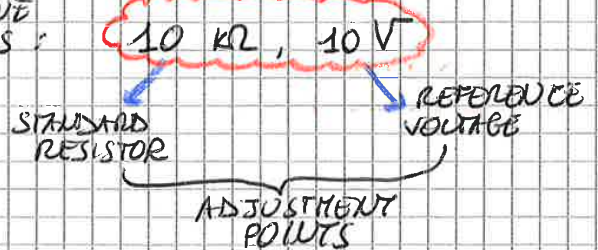
→  $k = 2$ ,  $p = 95\%$



## LIFE-CYCLE OF A MEASURING INSTRUMENT



ADJUSTMENT = OPERATION THAT HAS TO BE DONE WITH REFERENCE STANDARDS:



INITIAL VERIFICATION → PRE-ADJUSTMENT

→ BEFORE THE ADJUSTMENT HAS AT THE END OF CALIBRATION INTERVAL

IT'S VERY IMPORTANT CAUSE YOU DISCOVER YOU DIDN'T KNOW WHERE MEASUREMENTS (HAPPY SO!)

FINAL VERIFICATION → POST-ADJUSTMENT

→ AFTER THIS THE INSTRUMENT RETURNS TO USER ALLOWS TO GIVE YOU THE SITUATION OF INITIAL USE

### ALTERNATIVE PATHS:

• **↓** BECAUSE OF COSTS → IF VERIFICATION PASSES  $S_i < \delta I_i$   $V_i$

IT'S SUGGESTED TO TEST BETTER THIS CONDITION (e.g.  $S_R = 0.99 \delta I_R$  DANGEROUS!)

RISK: WITHOUT COMPENSATING THE DRIFT DURING THE 2nd YEAR THERE COULD BE SOME ERRORS

IF  $S_i < 0.15 \delta I_i$  → OK! YOU CAN DO IT

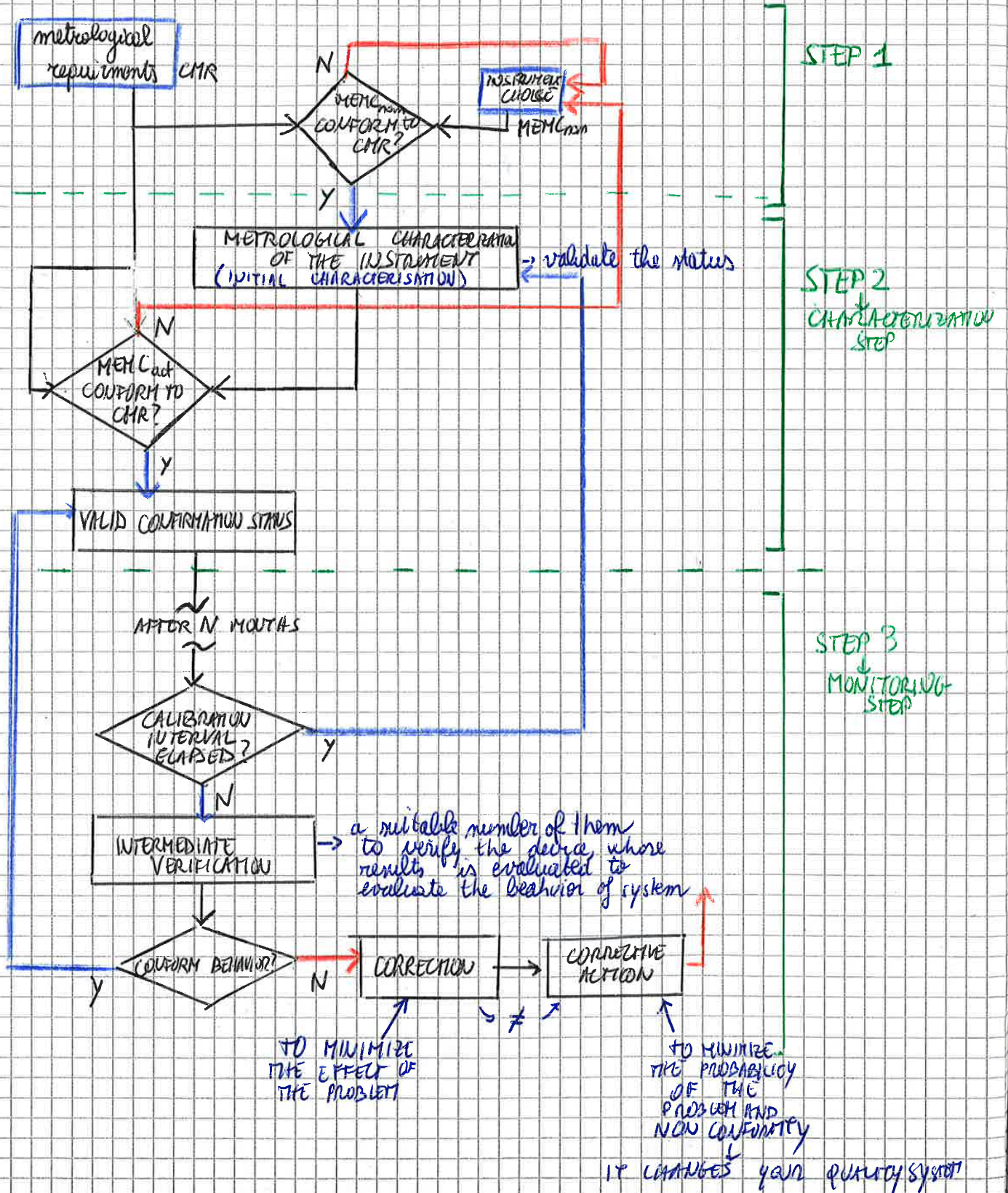
• **↓** PAY MUCH ATTENTION! DANGEROUS!

YOU DON'T KNOW THE EFFECT OF YOUR DECISIONS BEFORE SO YOU DELETE INSTRUMENT HISTORY!

IF AN INSTRUMENT CERTIFIED BY A COUNTRY WHICH ISN'T IN THE AGREEMENTS, I CAN FOLLOW IT CAUSE I'M NOT INTERESTED IN PASS HISTORY OF THE INSTRUMENT

# LIFE-CYCLE OF A MEASURING EQUIPMENT → 3 MAIV STEPS :

- ① CHOICE OF INSTRUMENT MODEL THAT POTENTIALLY MEETS THE METROLOGICAL REQUIREMENTS → INPUT: CMR
- ② EVALUATION OF INSTRUMENT CONFIRMATION-STATUS (BEFORE ITS USE)
- ③ MONITORING OF INSTRUMENT CONFIRMATION-STATUS (DURING ITS USE)



14/10/16

MANAGEMENT OF INSTRUMENTATION

① CHOICE OF MEASURING INSTRUMENT → RELATED TO CMR  
 (related to the field where measurement is implemented)

- 1st INFORMATION → KIND OF QUANTITY UNDER MEASUREMENT  
 WHEN YOU'VE TO MEASURE MORE THAN 1 QUANTITY: V, R, I, P  
 INSTEAD OF USING A VOLTMETER, OHMMETER, AMPEROMETER, ETC...  
 USE A DMM  
 ↓  
 SELECT A FEW SET OF INSTRUMENT  
 (IF A HAVE TO CONFIRM VALIDATION STATUS → IT'S CONVENIENT TO WORK WITH ONE INSTRUMENT)
- EXPECTED RANGE OF VARIATION QUANTITIES → THAT ALLOWS A SUBSET OF THE INITIALLY SELECTED DEVICES TO BE IDENTIFIED

Examples: 1a) quantity: Voltage  
 waveform: sinusoidal  
 $V_{RMS} = 230 V @ f = 50 Hz$  } → average responding  
 peak responding

1b) if same voltage and arbitrary waveform → true RMS voltmeter

1c) if  $V_{RMS} = 30 kV$  → arrange a measurement chain  
 No direct connection  
 voltage transformer → puts 30 kV to a lower value  
 + average / peak / true RMS voltmeter

2) quantity: Temperature inside an oven  
 use of memory chain which starts from a sensor  
 can be - resistive temperature sensors  
 - thermo-couple devices  
 - thermoresistors  
 - thermopile  
 coarse of range -  $(1000 \div 1500) ^\circ C$  → thermocouples  
 thermopile

! RESOLUTION } IN CMR AFFECT CHOICE  
 MAXIMUM ADMITTED ERROR (MAE) } OF EQUIPMENT!  
 maximum difference (actual value - nominal value) ↓  
 HAVE TO BE BOTH LOWER THAN THE CORRESPONDING REQUIREMENTS

② EVALUATION OF THE INSTRUMENT CONFIRMATION STATUS (BEFORE ITS <sup>FIRST</sup> USE)

ONCE WE SELECT AN INSTRUMENT WE KNOW  $MEMC_{nom}$   
 BUT WE HAVE TO ESTIMATE  $MEMC_{act}$

IN ORDER TO COMPARE THEM

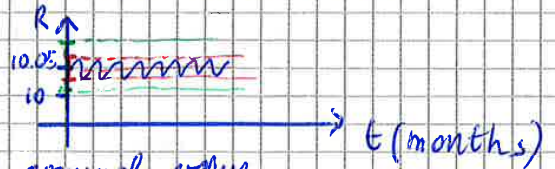
THIS DOESN'T MEAN WE HAVE TO REPEAT CALIBRATION! NO!

NOT ALL THE CHARACTERISTICS OF MANUFACTURER HAVE TO BE VERIFIED  
 BUT ONLY THE CHARACTERISTICS OF CMR  
 THEREFORE THE EFFECT OF  $\Delta T$  IS VERY CONSIDERED

ex1) 10 k $\Omega$  resistor  $\rightarrow$  MAE: 0.001%  
 $T_{test}$  affects  $T_{range}$  (20  $\div$  80)  $^{\circ}C$

We select a standard resistor  $\rightarrow$  but we don't use it immediately!  
 we have to  $\rightarrow$  initially characterize it  
 $\rightarrow$  fix uncertainty that has to be  $<$  MAE  
 (eg 0.0001%)

We need to know time drift



$10.05 \pm$  T enlarges uncertainty interval

ex2) DMM  $\rightarrow$  employed as a DC voltmeter

quantity : DC Voltage  
 Range = 1 mV  $\div$  1 V  
 $T = 23^{\circ}C$  MR % = 50%  
 MAE = 0.01% Range

$\Rightarrow$  we have to estimate  $MEMC_{act}$   
 the calibration function for DC voltage  
 we have to verify only the  
 ranges which are specified (eg: 200 mV  $\div$  2 V)

VALID CONFIRMATION STATUS OF AN INSTRUMENT  $\rightarrow$  MAINTAIN ALL REGISTRATIONS RELATED TO THIS OPERATION IN DEFINED TIME INTERVAL

LABORATORY CAN PROVIDE CALIBRATION  $\downarrow$  CONFORMITY WHICH REFERS TO CALIBRATION CERTIFICATES THAT STATE THE CONFORMITY OF THE INSTRUMENT

PAY ATTENTION TO AVOID AMBIGUOUS INDICATIONS OF THE CONFIRMATION STATUS  
 GREEN  $\rightarrow$  INSTRUMENT VALID CONFIRMATION STATUS IN ALL RANGES

LABEL  $\leftarrow$  RED  $\rightarrow$  DO NOT USE THIS INSTRUMENT

$\downarrow$  YELLOW  $\rightarrow$  INSTRUMENT CONFIRMED ONLY FOR PARTICULAR FUNCTIONS IN PARTICULAR CONDITIONS

**INTERMEDIATE VERIFICATION** → VERY IMPORTANT

→ KNOWS TO MONITOR THE RISK OF NON CONFORMITY



A POSSIBLE WAY TO REDUCE THE PROBABILITY OF NON CONFORMITY CONSISTS IN REDUCING THE INSTRUMENT CALIBRATION INTERVAL (DURING WHICH WE HAVE TO MONITOR THE BOMBS) (execution of intermediate verification during calibration interval)

IT'S A COMPARISON BETWEEN GENERATORS & MEASURING DEVICES

IT REQUIRES AVAILABILITY OF GENERATORS

if I have Power supply & DM I can compare these 2 devices

IN CALIBRATION LABORATORIES → YOU HAVE TO OBTAIN CONFORM RESULTS

TAKING CONSIDERATION OF THE TIME DUE TO 2 INSTRUMENTS A FAIL RESULT PROVIDES A DANGEROUS SITUATION SO YOU ACTIVATE FURTHER PROCEDURES

PERIODICAL } VERIFICATIONS → REINFORCED APPLYING KNOWN VALUES  
NON-PERIODICAL } → RELATED TO COSTS

2 STEPS: 1) FURTHER MEASUREMENTS REQUIRED TO BE CARRIED OUT WITH MORE ACCURATE DEVICES

2) SAME OPERATIONS OF A NOT CONFORM SITUATION AT THE END OF CALIBRATION INTERVAL

**CORRECTION** → ANALYSIS OF EFFECT OF NON CONFORMITY

**CORRECTIVE ACTION** → PURPOSE: MINIMIZE PROBABILITY OF OCCURRENCE OF NON CONFORMITY

IDENTIFICATION OF NON-CONFORMITY CAUSES AND THEN THEIR REMOVAL

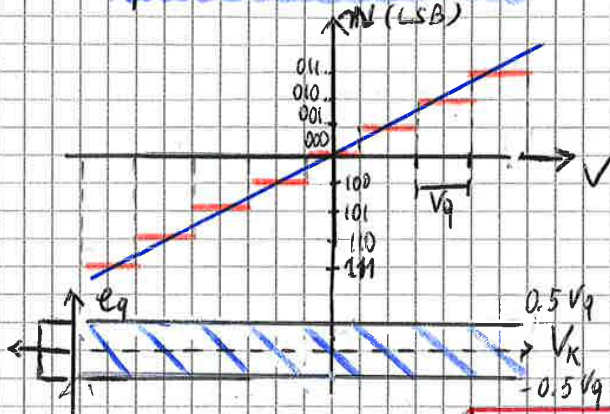
**QUANTIZATION** → DESCRIBES A QUANTITY BY MEANS OF FINITE NUMBER OF VALUES

**ADC** → DEVICE ACCEPTING AS INPUT: ANALOG SIGNAL PROVIDING AS OUTPUT: DIGITAL CODE

INTRODUCES AMBIGUITY IN THE INTERPRETATION OF DIGITAL CODES

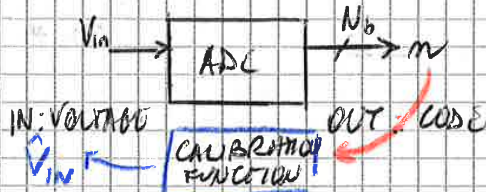
MEASUREMENT RANGE → SUBDIVIDED INTO A FINITE NUMBER OF INTERVALS ALL WITH THE SAME WIDTH.

TYPICAL CHARACTERISTIC IN/OUT OF 3 BIT BIPOLAR ADC



NOT SYMMETRIC (one has to be spent for internal)

ADC → CAN BE CONSIDERED AS A VOLTMETER



QUANTIZATION VOLTAGE:

$$V_q = \frac{V_{FR}}{2^{N_b}}$$

→ REPRESENTS RESOLUTION: MINIMUM CHANGE OF IN THAT CAN BE OBSERVED AT THE OUTPUT

! SOME DIGITAL CODE IS ASSIGNED TO THE VALUES WITHIN THE SAME QUANTIZATION INTERVAL

FOR FINAL USER IT'S IMPORTANT OUT/IN CHARACTERISTIC ( $\hat{V}_{in}$ )

IT'S NOT POSSIBLE TO INVERT THE FUNCTION SO CHARACTERISTIC SHOULD BE APPROXIMATE BY A LINEAR NOMINAL CHARACTERISTIC → THAT ALLOWS TO CONVERT OUT TO IN AND TO ESTIMATE  $V_{in}$  FROM THE CODE  $m$

IT'S ONLY AN APPROXIMATION → SO I CONVERT 111 TO THE CENTRAL VALUE OF THE QUANTIZATION STEP AND IT'S A POSSIBLE SOURCE OF ERROR

**QUANTIZATION ERROR:**

$$e_q = \hat{V}_{in} - V_{in}$$

DIFFERENCE BETWEEN → ESTIMATED  $V_{in}$   
→ ACTUAL  $V_{in}$

$$e_q = \frac{V_q}{2} = \frac{V_{FR}}{2^{N_b+1}}$$

$\max(e_q) = 0.5 V_q$  WHEN  $V_{in}$  IS VERY CLOSE TO THE TRANSITION VOLTAGE

FROM A PROBABILITY POINT OF VIEW → I CAN DRAW THE PROBABILITY DENSITY FUNCTION

WHEN → ANALOG SIGNAL CHANGES IN A CONTINUOUS WAY → THERE IS NO CORRELATION BETWEEN  $V_{in}$ ,  $N$

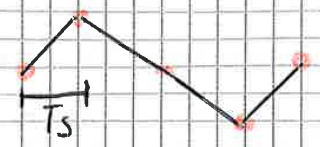
DETERMINISTIC MODEL (WORST CASE MODEL) UNIFORM PROBABILITY DENSITY FUNCTION

**SAMPLING** → MEANS OBSERVING THE SIGNAL ONLY IN PARTICULAR INSTANTS

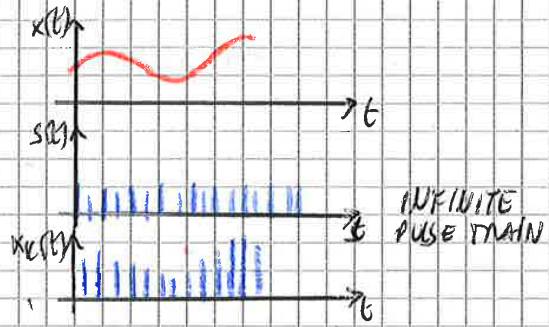


• SAMPLES OBTAINED AT EACH TIME INSTANTS  
 → LINEAR INTERPOLATION  
 ↓  
 VERY SIMILAR TO THE ORIGINAL ONE

IF WE INCREASE SAMPLE INTERVAL



WAVEFORM ISN'T A GOOD RECONSTRUCTION OF THE ORIGINAL SIGNAL



**SAMPLE SIGNAL**

$$x_s(t) = x(t) \cdot \sum_{k=-\infty}^{+\infty} \delta(t - kT_s)$$

↑  
 ANALOG SIGNAL  
 ↑  
 INFINITE PULSE TRAIN  
 ↑  
 EVEN IF THE SIGNAL ISN'T A BIG VARIATION  
 ↓  
 THIS REPRESENTS VERY FAST TRANSIENT

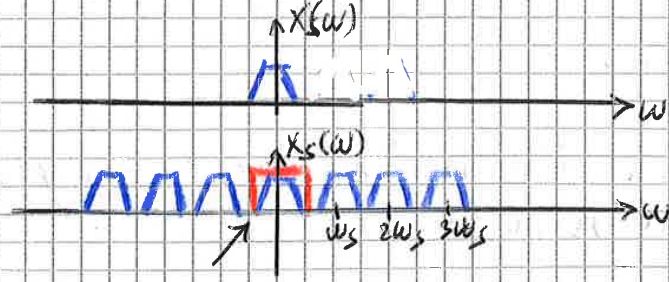
IF WE APPLY THE RULES OF FOURIER TRANSFORM (PRODUCT IN TIME → CONVOLUTION IN FREQUENCY)

$$X_s(\omega) = X(\omega) * S(\omega) = \omega_s \sum_{k=-\infty}^{+\infty} X(\omega - k\omega_s)$$

↑  
SPECTRUM

**GRAPHICAL REPRESENTATION**

ASSUMPTION: BANDS LIMITED SIGNAL



SPECTRUM CAN BE REPRESENTED AS AN INFINITE REPETITION

BUT WE'RE INTERESTED IN THE ORIGINAL SIGNAL SO WE USE **IDEAL** LOW PASS FILTER (CANNOT BE IMPLEMENTED IN REAL SITUATION AS IDEAL)

WE HAVE TO RESPECT SAMPLING THEOREM

$$f_s \geq 2 f_{max} \rightarrow f_s > 2 f_{max}$$

↑  
 identified from the characteristics of a sensor

DON'T USE EQUAL CONDITION!

21/10/16

**CONVERSION TIME** = FINITE TIME NECESSARY FOR ADC TO COMPLETE CONVERSION PROCESS

ANALOG SIGNAL IS CONVERTED IN A CODE

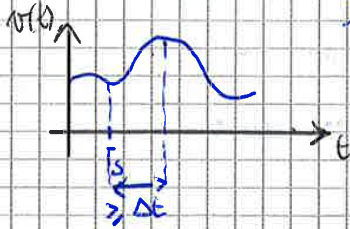
! DURING THE CONVERSION TIME → THE ADC INPUT HAS TO REMAIN STABLE  
 (cause of resolution of ADC which isn't able to see continuous signals)

SIGNAL SHOULD REMAIN IN THIS RANGE IN ORDER TO BE SEEN:  $\pm \frac{1}{2} V_q$

→ IT FIXES A LIMIT TO  $f_s$ , REGARDLESS OF THE SAMPLING THEOREM ( $f_s > 2f_{max}$ )

(according to conversion time, it's a more important limit than  $f_s$ )

eg:  $\Delta t = 10 \mu s$  → fixes a limit to  $f_s$   
 next sample cannot be taken before this interval has elapsed



$$f < \frac{1}{\Delta t} = 100 \text{ kSa/s}$$

Applying the Shannon theorem

$$f_{max} < \frac{f_s}{2}$$

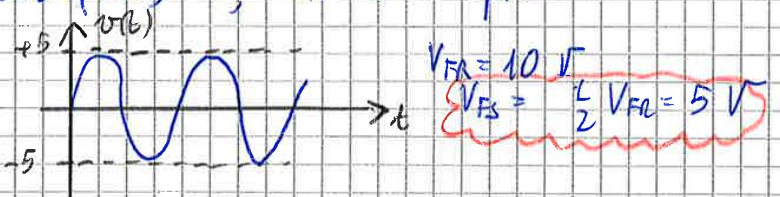
$$f_{max} < 50 \text{ kSa/s}$$

$$N_b = 12 \text{ bit}$$

$$V_{FR} = 10 \text{ V}$$

$$V_p = \frac{V_{FR}}{2^{N_b}} \approx 2.5 \text{ mV}$$

our signal:  $v(t) = A \sin(\omega t)$ ,  $A = 5 \text{ V} = V_{pk}$   
 Bipolar ADC



( $\omega = 2\pi f$  angular frequency)

What is  $f_{max}$  that could be correctly converted?

$\Delta v_{max} \leq \frac{1}{2} V_q$  during  $\Delta t$  → in order to have a correct conversion  
 SENSITIVITY RESPECT TO TIME

$$\Delta v_{max} = \left. \frac{dv(t)}{dt} \right|_{max} \Delta t = \omega A \cos(\omega t) \cdot \Delta t = \omega A \Delta t$$

$$\omega A \Delta t = 2\pi f A \Delta t \leq \frac{1}{2} V_q$$

$$f_{max} \leq \frac{V_q}{4\pi A \Delta t} = \frac{2.5 \text{ mV}}{4\pi \cdot 5 \text{ V} \cdot 10 \mu s} \approx 4 \text{ Hz}$$

**SURPRISING RESULT!**  
 WE HAVE TO LIMIT  $f_{max}$  TO 4 Hz!



WHEN YOU HAVE A SYSTEMATIC EFFECT → TRADITIONAL METHODS

- RECOGNISE IT
- ESTIMATE THE EFFECT, ITS VALUE
- COMPARE WITH UNCERTAINTY CONTRIBUTION

IF HIGHER TRY TO COMPENSATE

Example of ADC specifications

•  $f_{smax} = 40 \text{ MSa/s}$  (it's better to distinguish by using  $f_s$ )

Not fixed, you decide it → important for design issue

eg. you have to develop a certain product and you have to use this ADC, but the  $f_{max} = 1 \text{ kHz}$  you need

so we can set ADC  $f_s > 2 \text{ MSa/s}$

We have  $f_{just} = 40 \text{ MSa/s}$

if we use it NO aliasing but there's a drawback for this: large amount of sample means high transmission rate!

So we use  $f_s$  suitable for your application! (In this case  $2 \text{ MSa/s}$ )

•  $N_b = 14$

• Unipolar  $[0 \div 2^+] \text{ V}$  Bipolar  $[-1 \div 1] \text{ V}$  → some resolution  $V_q \approx 120 \mu\text{V}$

• One chip S/H

•  $E_{TOT} = E_q + E_{\pm} + E_0 + E_g$

uncertainty      offset      GAIN

→ you can estimate uncertainty as  $V$  or LSB

$V_{FR} = 2 \text{ V}$

$FR = 2^{14} \text{ LSB}$

$FS = 2^{13} \text{ LSB}$

$\delta V_{IN} = E_{TOT} \cdot V_q$

→  $N_b^E = N_b - \log_2(2 \cdot E_{TOT})$

effective number of bits

! IT IS POSSIBLE TO COMPENSATE OFFSET AND GAIN ERROR:

- GAIN ERROR: known input  $V$ , obtain  $\frac{V_{out}}{V_{in}} = \text{slope}$

- OFFSET →  $V_{OFF}$  → set  $V_{in} = 0 \text{ V}$  → OUT: OFFSET → compensate in software

IN THIS WAY ↓  $< E_{TOT} \Rightarrow > N_b^E$

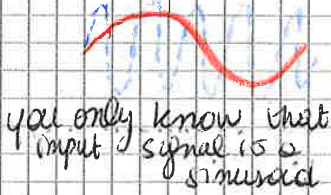
**DSO** → DOESN'T INCLUDE ANTI-ALIASING FILTERS

IT'S POSSIBLE TO SEE A WAVEFORM WHICH IS WRONG RESPECT TO THE INPUT SIGNAL

**ALIASING** PHENOMENA IS POSSIBLE!

--- real signal  
 --- signal seen ] → DUE TO LOW SAMPLE RATE!

YOU CAN HAVE AN ERROR OF  $\Delta$  AMPLITUDE



IN DSO ALIASING CAN BE HIGHLIGHTED

IF YOU CHANGE TIME-BASE CONFIGURATION YOU SEE NON COHERENT WAVEFORMS

(because you sub-sampled signal in a different way)



! SUGGESTION : TO SEE A RIGHT RECONSTRUCTION ⇒ CHANGE TIME BASE  
 IF NON COHERENT WAVEFORMS - CHANGE  $f_s$

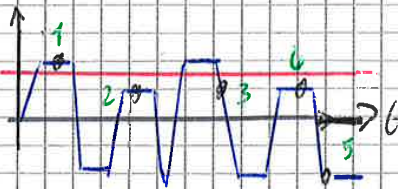
**SAMPLING THEOREM REQUIREMENT**

HAS TO BE MET WHEN TRANSIENT SIGNALS ARE ACQUIRED (NO REPETITIVE/DOT PERIODIC SIGNALS)

ONE SHOT (real time) MODE OF DSO  
 [one possibility to acquire the sample]

CAN BE OVERCOME WITH REPETITIVE SIGNALS (PERIODIC SIGNALS ⊂ REPETITIVE SIGNALS SUBSET)

**EQUIVALENT-TIME SAMPLING**



YOU CAN OBTAIN SAMPLES FROM DIFFERENT REPETITIONS

RANDOM SAMPLING REFERS THAT THERE IS NO CORRELATION BETWEEN SAMPLES (ASYNCHRONOUS TO IT) TRIGGER EVENT

TRIGGER EVENT → ACTS LIKE A RESET FOR A COUNTER

WE OBTAIN SAMPLES AND REORDER THEM REFERRING TO TRIGGER EVENT WHICH PROVIDES  $\Delta t_i$  WHEN EACH SAMPLE ARRIVES (such that we assign a correct time slot) to each sample

$f_{seq}$  → EQUIVALENT SAMPLING FREQUENCY → DEPENDS ON DSO CAPABILITY TO MEASURE THE DELAY BETWEEN TRIGGER EVENT SAMPLES

$f_{seq} = \frac{1}{\Delta t}$

with  $\Delta t$  = resolution that allows to distinguish the position

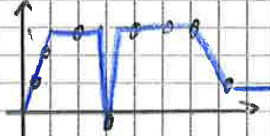
$f_{seq} \geq f_{real}$

REAL FS OF DSO

① **SAMPLE MODE** → DEFAULT MODE  
 USES:  $T_s = \frac{(\text{time/div}) \cdot 10}{N_w}$   
 DEPENDS ON YOUR TIME BASE CONFIGURATION  
 FIXES  $\Delta f_s$   
 NUMBER OF WAVEFORMS POINT ON THE DISPLAY  
 FIXES BY THE MANUFACTURER

② **AVERAGE MODE** → OPERATION FIXES TIME/DIVISIONS  
 AVERAGE OF THE WAVEFORM POINTS OF SUBSEQUENT ACQUISITIONS  
 USEFUL IF YOU HAVE REPETITIVE SIGNALS IN ORDER TO REDUCE NOISE (even if noise has the same  $f$  of the signal)

IN DSO < BAND LIMITATION → NOT USEFUL REDUCES BANDWIDTH } TO REDUCE NOISE  
 AVERAGE MODE

③ **PEAK DETECT MODE** → DECIMATION TECHNIQUE: WAVEFORM POINTS OBTAINED AS MINIMUM AND MAXIMUM SAMPLE POINTS ACQUIRED DURING 2 WAVEFORM INTERVALS  
  
 INCREASES THE PROBABILITY TO CATCH GLITCHES / SHORT PULSES (more than default mode)

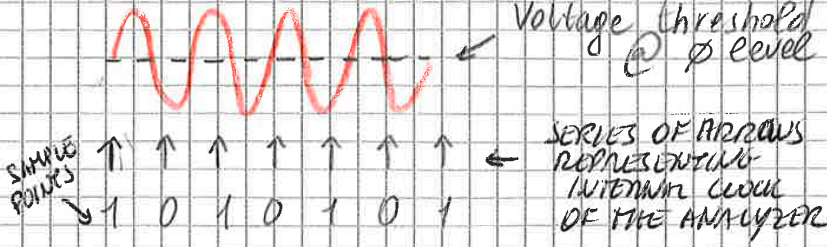
④ **ENVELOP MODE** → DECIMATION TECHNIQUE: MINIMUM & MAXIMUM SAMPLE POINTS OF SUBSEQUENT ACQUISITIONS USED TO SHOW MINIMUM AND MAXIMUM ENVELOPE  
 YOU BUILD A BAND OF MINIMUM AND MAXIMUM TRANSITIONS

⑤ **HIGH RESOLUTION MODE** → DECIMATION TECHNIQUE: WAVEFORM OBTAINED AS MEAN VALUE OF SAMPLE POINTS ACQUIRED DURING A WAVEFORM INTERVAL  
 NOISE REDUCTION  
 AS DIETHERING TECHNIQUE IN DAQ BOARDS  
 RESOLUTION IMPROVEMENTS  
 WITH SLOW CHANGES WITH RESPECT TO THE  $f_s$   
 WITHOUT INCREASING THE NUMBER OF BITS

**④ TIMING MODE** → USED WHEN IT'S NOT REQUESTED AN  $f \sim f$  OF THE SYSTEM

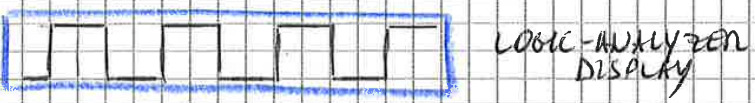
INPUT SIGNALS ASYNCHRONOUSLY SAMPLED

SAMPLE POINTS COMPARED TO VOLTAGE THRESHOLD IN ORDER TO OBTAIN A HIGH OR LOW STATES



NO PARAMETRIC INFOS BE'S REPRESENTED AS DIGITAL SIGNAL

NO CORRELATION BETWEEN TIME OF THE SIGNAL & TIME OF INSTR.



TIME RESOLUTION ( $t_{clk}$ ) → INTRODUCES AMBIGUITY IN THE ANALYSIS OF DIGITAL SYSTEMS BECAUSE THE ANALYZER PLACES THE TRANSITION POINTS AT THE NEXT SAMPLE → WORST ERROR:  $\downarrow$  SAMPLE PERIOD

because transition point has a delay

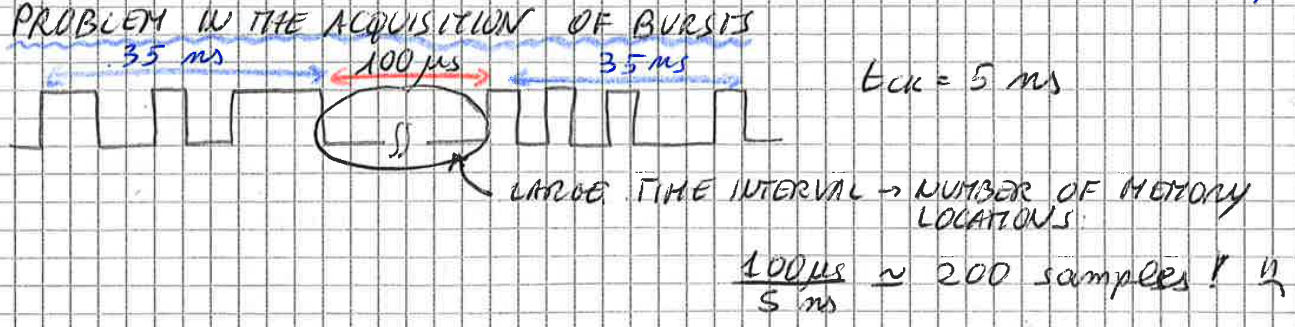
TRADE-OFF BETWEEN } RESOLUTION → LOW VALUE OF ACQUISITION WINDOW

ACQUISITION TIME

(DUE TO LIMITATION OF INTERNAL POINTS) WE HAVE TO DECREASE ACQ. TIME

eg: Memory of 64 kSamples → 4 channels →  $t_{clk} = 1 \mu s \Rightarrow$  ACQ. TIME = 4.6.8 ms

$t_{clk} = 5 ns \Rightarrow$  ACQ. T = 81.92  $\mu s$



IT'S POSSIBLE TO MODIFY THE LOGIC ANALYZER IN ORDER TO HAVE A MORE EFFECTIVE USE OF MEMORY

**TRANSITIONAL ANALYZER** → HAS THE POSSIBILITY TO DETECT THE TRANSITIONS AND USING A COUNTER ABLE TO MEASURE TIME INTERVAL BETWEEN TRANSITIONS

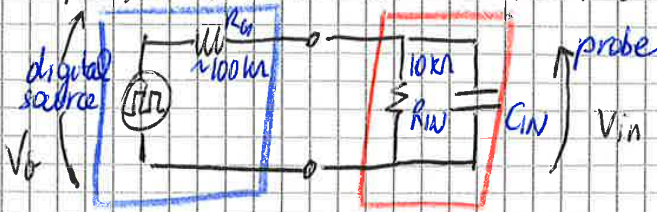
STORED DATA → SAMPLES PRECEDED BY A TRANSITION → ELAPSED TIME FROM THE LAST TRANSITION (COUNTER STARTS AND IT'S RESET AT EACH TRANSITION)

IN THE PREVIOUS EXAMPLE → WHEN THERE'S A LONG TIME INTERVAL, DURING WHICH COUNTER REACHES THE VALUE 20000 → STORED IN MEMORY → LESS MEMORY LOCATIONS! SORT OF COMPRESSION TECHNIQUE

• **PROBES** (→ called PODS)

→ A PROBE ALLOWS A LARGE NUMBER OF SIGNALS TO BE EASILY CONNECTED BY MINIMIZING SYSTEMATIC LOAD EFFECT ON TIME BEHAVIOR (WE CAN TOLLERATE THE EFFECT ON AMPLITUDE BUT NOT ON TIME!)

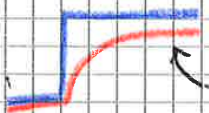
PROBE → HAS AN INPUT IMPEDANCE → THAT CAUSES SYSTEMATIC EFFECT



$$V_{in} = V_0 \frac{R_{in}}{R_{in} + R_0} \quad \text{VOLTAGE DIVIDER}$$

$$\frac{V_{in}}{V_0} = \frac{10^4}{10^4 + 10^2}$$

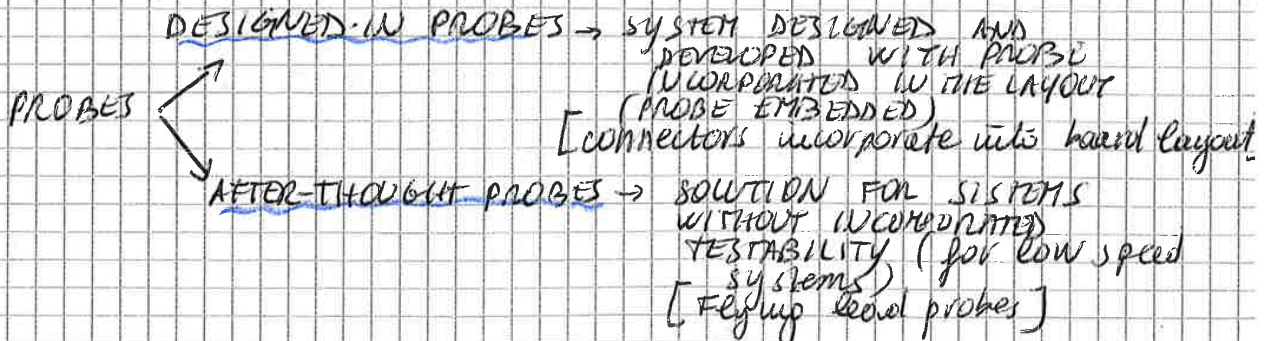
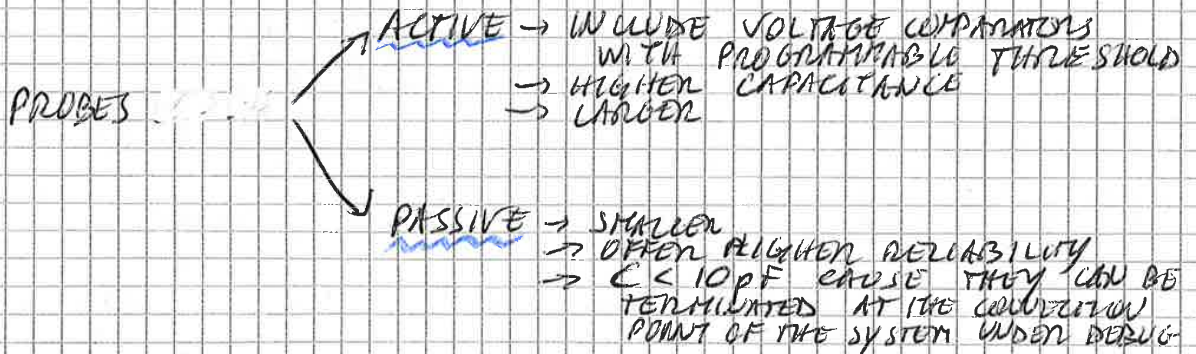
NO STRONG ATTENUATION IN ORDER TO NOT CHANGE HIGH LEVEL  
IF YOU HAVE  $C_{in} = 10 \text{ pF}$



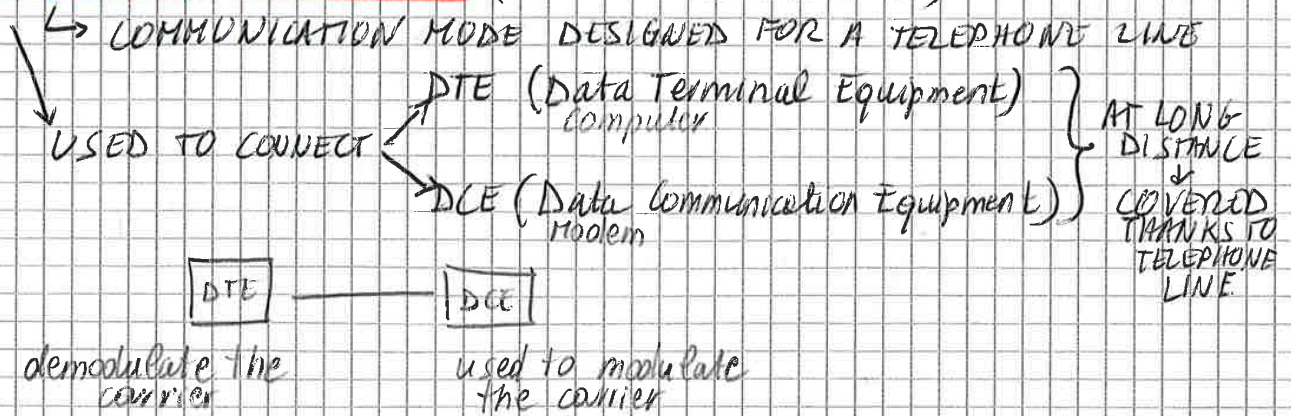
$$\tau \approx R_0 \cdot C_{in} \rightarrow \tau \approx 10^2 \cdot 10^{-12} = 10^{-1} = 0.1 \text{ ns} \leftarrow \text{CHANGE TIME CONSTANT}$$

SIGNAL RECEIVED BY LOGIC ANALYZER DUE TO EFFECT OF PROBE

DETECTED SIGNAL AMPLITUDE IS LOWER BUT THERE'S ALSO A DELAY! DANGER! SIGNAL CAN BE VERY DIFFERENT FROM THE SIGNAL OF THE INSTRUMENT UNDER DEBUG



## SERIAL INTERFACE RS-232 (EIA STANDARD INTERFACE)



- MAIN PARAMETERS :
- MAXIMUM DISTANCE BETWEEN DEVICES   
  $< 15 \text{ m}$  -  $\frac{\text{Band rate}}{\text{Hz}}$    
  $\rightarrow$  distance enter band rate
  - CAPACITIVE LOAD  $< 2.5 \text{ nF}$    
  $\downarrow$    
 AFFECTS THE VALUE OF THE SIGNAL WE TRANSMIT

- VOLTAGE SIGNALS REFERRED TO A COMMON GROUND
- DIGITAL LEVELS   
 MARK  $\rightarrow$  NEGATIVE VOLTAGE  $(-25 \div -3) \text{ V}$    
 SPACE  $\rightarrow$  POSITIVE VOLTAGE  $(+3 \div +25) \text{ V}$    
 TRANSITION REGION  $(-3 \div +3) \text{ V}$    
 (MONOTONIC BEHAVIOUR)

## ELECTRICAL RULES

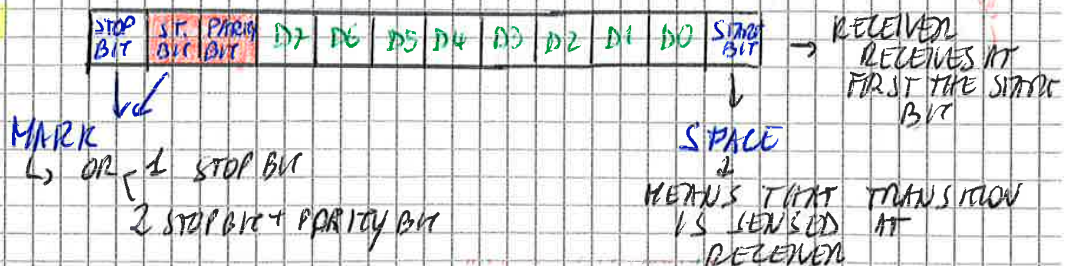
TIME TO PASS THROUGH THE TRANSITION REGION:

- less than  $1 \mu\text{s}$   $\rightarrow$  for control signals
- less than  $4 \mu\text{s}$   $\rightarrow$  for data signals

MAXIMUM SLEW-RATE:  $30 \text{ V}/\mu\text{s}$

IF DEVICE IN IDLE STATE  $\rightarrow$  LINE IS KEPT AT THE MARK LEVEL

## DATA PACKET



PACKET SIZE:  $9 \div 12 \text{ BITS}$

→ FREQUENCIES OF TRANSMITTER & RECEIVER ARE DIFFERENT

↓  
EACH ONE HAS A TOLERANCE

AN ERROR HAS A CORRESPONDING SHIFT

> Baud rate => > possibility of error

↓  
IF ERRORS ONE SOLUTION IS TO DECREASE BAUD RATE

### ERROR DETECTION

• PARITY ERROR

• FRAMING ERROR → WE EXPECT A PACKET WITH A CERTAIN NUMBER OF BITS → IF STOP BIT IS N'T CORRECTLY IDENTIFIED (SPACE INSTEAD OF 1) → ERROR IDENTIFIED

↓  
THE DEVICE TRIES TO RESYNCHRONISE ON NEW INCOMING PACKETS  
↳ IF THE SITUATION PERSISTS THE ERROR IS NOTIFIED

THIS IS DUE TO A WRONG BAUD RATE FORMAT SETTING

• OVERFLOW → PROBLEM OF MANAGEMENT OF DIGITAL CIRCUIT

↓  
NEW DATA PACKET IS GENERATED IN THE RECEIVER BUT THE PREVIOUS ONE HASN'T BEEN REMOVED YET.

↓  
DUE TO PROTOCOL PROBLEMS

### COMMUNICATION MODES :

• DTE1 AND DTE2 CONNECTED THROUGH A SWITCHED LINE (MODEM) (DIALING NUMBER IS REQUIRED)

• DTE1 AND DTE2 CONNECTED THROUGH A DEDICATED LINE

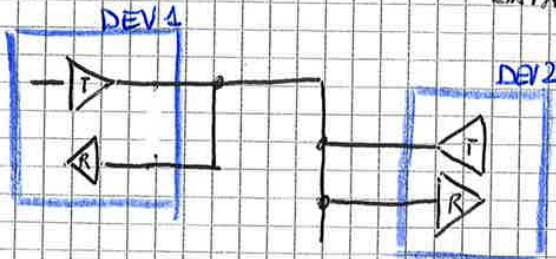
• DIRECT LINK WITHOUT A MODEM (MOST EMPLOYED)

↓  
WE CONNECT DIRECTLY DEVICES

SIGNALS RESERVED TO A MODEM ARE NOT EMPLOYED (EMPLOYED IN A DIFFERENT WAY) (BASED ON LOCAL CONNECTIONS)

**RS-485**

- TRANSMISSION ONE-TO-MANY (NO SIMPLEX!) (32 max)
- DIFFERENTIAL SIGNALS
- MAX DISTANCE: 1.2 km
- THREE-STATE DRIVERS → DIFFERENT DRIVERS CAN DRIVE THE DATA LINE → ONLY ONE OF THE DEVICES IS SELECTED



WHEN A DRIVER ISN'T SELECTED IT GOES IN HIGH IMPEDANCE STATE

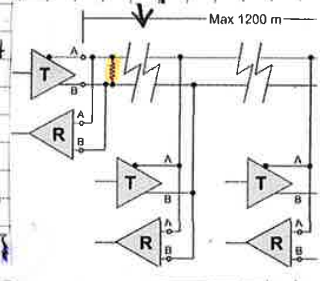
When DEV1 is selected as Master DEV2 is disabled and put in high impedance state

2 DIFFERENT PROTOCOLS:

**RS-485 2-WIRE**

- TRANSMITTER } OF EACH DEVICE ARE CONNECTED THROUGH A TWISTED PAIR
- RECEIVER
- NODE HAS THE POSSIBILITY TO SEND INFORMATION TO AN OTHER NODE (HALF-DUPLEX TRANSMISSION POSSIBLE)
- LOW WIRING COST → DUE TO THE # OF WIRES (LESS WIRES 2 C4)

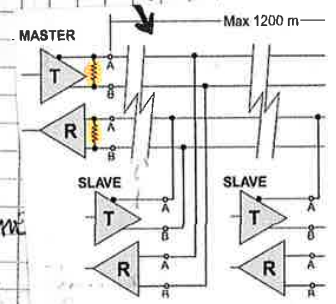
COMMON TWISTED-CABLE CONNECTS ALL DEVICES



**RS-485 4-WIRE**

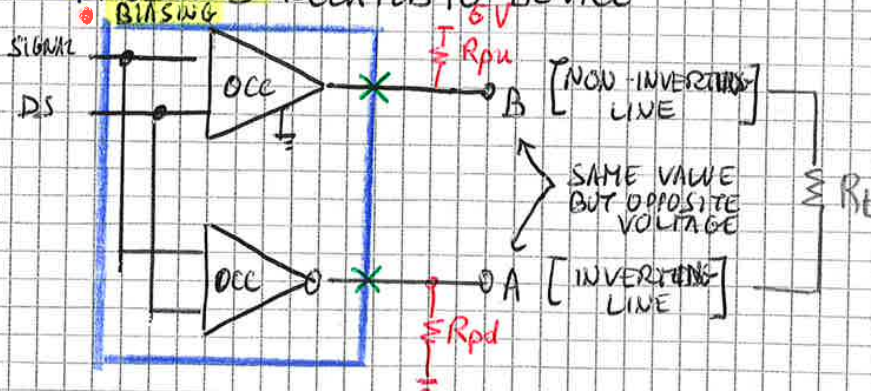
- TRANSMITTER OF MASTER → ALL RECEIVERS OF SLAVE NODES
- RECEIVER OF MASTER → ALL TRANSMITTERS OF SLAVE NODES

DIFFERENT CABLING



FULL-DUPLEX → POSSIBLE BUT LIMITED TO MASTER-SLAVE NO COMMUNICATION AMONG SLAVES

**PROBLEMS RELATED TO DEVICE**



IT'S POSSIBLE THAT ALL THE TRANSMITTERS ARE DISABLED (OR OPEN CABLE)

↓

OPEN CIRCUIT

↓

WE CAN HAVE UNDEFINED LEVELS

IN ORDER TO AVOID THIS SITUATION

↓

2 BIAS RESISTORS ARE EMPLOYED TO KEEP THE LINE IN A DEFINED STATE

(OCC = OPEN COLLECTOR CIRCUIT STANDS FOR 13-STATE)



**USB = UNIVERSAL SERIAL BUS** → SHORT RANGE DISTANCE BUS

SET OF SPECIFICATION FOR COMMUNICATION BETWEEN ELECTRONIC SYSTEMS

THANKS TO ITS HIGH SPEED, IT HAS REPLACED RS-232 AND ALL OTHER PARALLEL INTERFACES

IT'S NOT ONLY A COMMUNICATION CHANNEL → ACTS AS AN EXTENSIVE EXPANSION BUS TO CONNECT PERIPHERALS TO A PC IN A SIMPLE WAY (mouse, keyboards, joysticks, ...)

- ALLOWS HOT-SWAPPING → YOU CAN INSERT AND REMOVE USB WITHOUT TURNING OFF THE SYSTEM
- PROVIDES POWER TO THE BUS
- BAND RATE → DEPENDS ON THE VERSION

28/10/16

(ARNDINO → CONNECTED TO PC THROUGH A USB INTERFACE)

**DEVICES INCLUDED IN USB BUS**

A HOST-DEVICE WHICH MANAGES THE PROTOCOL

1 OR MORE USB PORTS

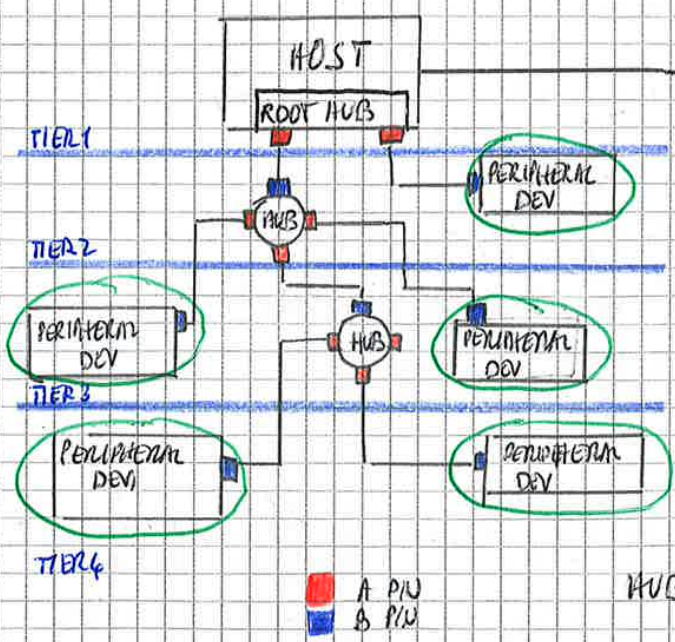
PERIPHERAL DEVICES CONNECTED IN TIERED-STAR TOPOLOGY  
THERE ARE HUBS WHICH EXPAND THE NUMBER OF AVAILABLE PORTS

(DIFFERENT LEVELS OF TIERS, UP TO 6 IN ORDER TO SUPPORT UP TO 127 DEVICES)

USB RECOGNIZES 2 KINDS OF PERIPHERALS

STAND-ALONE DEVICES [→ SINGLE FUNCTION] USUALLY EMPLOY ONE COMMUNICATION CHANNEL (mouse, flash drive...)

COMPOUND DEVICES [→ MULTI-FUNCTIONS] MANAGED USING SEPARATED CHANNELS (webcam...  
↳ video/audio ch...)



MASTER → MANAGES AND CONTROLS THE BUS EMBODIES A ROOT HUB TO HAVE THE CAPABILITY TO CONTROL AND SCHEDULING

SLAVES → ONLY ABLE TO RESPOND TO COMMANDS FROM THE HOST  
[A part from an exception usually controls are sent by master and received by slaves]

HUB = BRIDGES THAT EXPAND THE BUS THEY CAN HAVE THEIR OWN POWER SUPPLY AND MAY INCORPORATE SOME AMOUNT OF INTELLIGENCE



**THERE ARE 4 DATA TRANSFER MODES:**

- 1) CONTROL → CONFIGURATION SETUP COMMANDS INFO } CAN BE TRANSFERRED BETWEEN HOST PERIPHERALS
  - 2) ISOCRONOUS → USED BY TIME CRITICAL STREAMING DEVICES (eg. video camera)
    - REAL-TIME DATA TRANSFER BETWEEN HOST PERIPHERALS
    - ↓
    - SO THAT NO ERROR CORRECTION IS IMPLEMENTED
  - 3) BULK → USED WHEN BIG AMOUNT OF DATA HAS TO BE TRANSFERRED (eg: printer)
    - ERROR CHECK IS IMPLEMENTED
  - 4) INTERRUPT → USED WITH SMALL AMOUNT OF DATA THAT NEED IMMEDIATE ATTENTION (eg: mouse, keyboard)
    - ERROR CHECK IS IMPLEMENTED
- ISOCRONOUS } PERIPHERALS → CAN CONSUME UP TO 90% OF AVAILABLE BANDWIDTH
- INTERRUPT }
- AFTER 90%, HOST DENIES ACCESS TO THEM
- CONTROL } TRANSFERS USE BANDWIDTH LEFT OVER
- BULK }

# DATA ACQUISITION BOARD

04/11/16

**DAQ BOARD** = ELECTRONIC DEVICE

THERE ARE DIFFERENT VERSIONS:

- 1) INTERNAL TO THE PC (you have to open PC, restart it in order to restart DAQ)
- 2) EXTERNAL DAQ → RELATED TO DIFFERENT CONNECTIONS ON THE PC  
(once you've installed the driver you can connect the board according to specifications of USB peripheral)

IT'S A DEVICE THAT → ALLOWS A CHEAP MULTI-CHANNEL SYSTEM TO BE ARRANGED

OFFERS LIMITED PERFORMANCES (DAQ COMPARED TO DMM)

UNCERTAINTY IS AFFECTED BY PC INTERNAL NOISE (or due to power supply) → IMPROVEMENTS ARE OBTAINED WITH DAQ BOARDS FOR EXTERNAL BUSES

IT'S NOT A STAND-ALONE DEVICE (≠ DMM)

IT HAS TO BE CONNECTED TO THE PC IN ORDER TO OBTAIN VOLTAGE SUPPLY

IT HAS TO BE MANAGED THROUGH SW PROGRAMS

IT DOESN'T HAVE A DISPLAY (NO BUTTONS...) DATA ARE STORED AND CAN BE SEEN ON THE DISPLAY OF THE PC

MEASUREMENT THE MAIN FUNCTIONS ARE

- ACQUISITION (SAMPLING AND A/D CONVERSION) OF ANALOG SIGNALS (VOLTAGE, CURRENT, RESISTANCE...)

EVEN THROUGH THE ADC IS A VOLTMETER YOU CAN HAVE PARTICULAR CONFIGURATIONS IN ORDER TO MEASURE CURRENT, RESISTANCE, ETC.

- GENERATION OF ANALOG SIGNALS (VOLTAGE)
- DIGITAL I/O → IT HAS EXTRA FUNCTIONS BECAUSE IT'S USED TO CONTROL THE SYSTEM USING OUTPUT CHANNELS.

COUNTERS → IN ORDER TO MEASURE TIME INTERVALS  
TIMERS

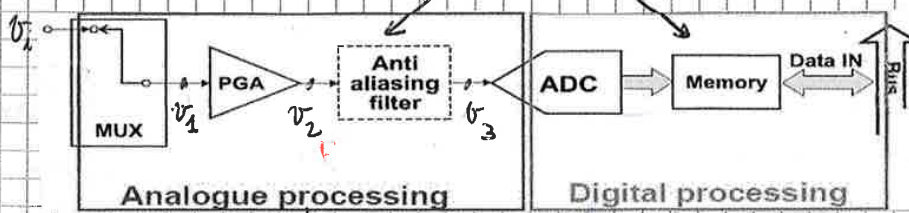
TYPICAL PERFORMANCES:

- 16/32 SINGLE ENDED } VOLTAGE
- 8/16 DIFFERENTIAL } VOLTAGE
- RANGES FROM 0.5 V → UP TO 20 V → NO VERY LOW } VOLTAGE SIGNALS
- RESOLUTION → 8 BIT → UNCERTAINTY: 1% } USES HIGHER RESOLUTION BUT LOWER f<sub>s</sub> THAN A DSD
- → 16 BIT → UNCERTAINTY: 0.1% }
- SAMPLING FREQUENCY: 50 kS/s - 50 MS/s
- VOLTAGE OUTPUT CHANNELS: (-10 ÷ 10) V

**MAIN UNCERTAINTY CONTRIBUTIONS** → IMPORTANT FOR DESIGN

ASSUMPTION: FIXED POSITION OF MUX (TO SIMPLIFY SITUATION BUT NOT OFTEN USED)

MEASURING CHAIN → IS DIVIDED IN 2 PARTS



INCLUDES A PART OF ADC ← INPUT ANALOG CIRCUIT  
S&H A PART OF CONVERSION

**ANALOG PROCESSING**

EACH PART OF MEASURING ELEMENTS HAS AN UNCERTAINTY CONTRIBUTION:

- MUX** → UNCERTAINTY CONTRIBUTIONS BASED ON VOLTAGE OFFSET DUE TO RESISTANCE → IMPORTANT IN PARTICULAR OCCASIONS → IF YOU WANT TO MEASURE A RESISTANCE  
CAN BE CONSIDERED NEGLIGIBLE -  $\sqrt{1} \approx 1$

**PGA**

$V_{FR} = 10V$  (BIPOAR RANGE)  
RANGE =  $(-5 \div 5)V$

$N_b = 10$

$V_q = \frac{10V}{2^{10}} \approx 10 \text{ mV} \rightarrow E_q = \frac{V_q}{2} = 5 \text{ mV}$

if  $V_{in} \approx 100 \text{ mV} \rightarrow E_q = \frac{E_q}{V_{in}} = \frac{5 \text{ mV}}{100 \text{ mV}} = 0.05 \rightarrow E_{qr} = 5\%$   
*high value*

PGA → to amplify signal if it's not close to range

$G = 50 \rightarrow E_q = \frac{5 \text{ mV}}{5V} = 1 \cdot 10^{-3} = 0.001 \rightarrow E_{qr} = 0,1\%$

PGA → GAIN UNCERTAINTY AND  $V_{off}$   
PASS-BAND FLATNESS  
TIME AND THERMAL DRIFTS  
( $I_q \rightarrow T$ )

$\Rightarrow v_2 = [v_1 + V_{off}] \cdot G$

- ANTI ALIASING FILTER** → DEPENDS ON THE CHARACTERISTICS OF THE SYSTEM →  $v_3 = H(v_2)$   
SAME UNCERTAINTY CONTRIBUTIONS

- SAMPLE & HOLD CIRCUIT** → UNCERTAINTY CONTRIBUTIONS SPECIFIED IN ADC SPECS INCLUDED BY MANUFACTURER

$v_3 = v_3(t_s)$  → CAPACITOR IS CHARGED TO THIS VALUE  $v_3$   
SAMPLE

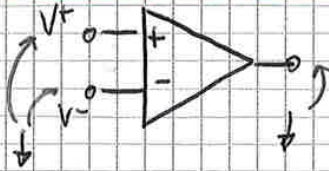
WE OBTAIN

$\Rightarrow v_3 = G H_0 [v_i(t_s) + V_{off}] + n(t_s)$  → **ELECTRONIC NOISE**

← DUE TO BOARD COMPONENTS (AMPLIFIERS, TRANSISTORS...)  
→ INTRODUCED BY OTHER DEV. NOISE IN THE

[ WE DO NOT CONSIDER PROBLEM OF ALIASING ]

**DIFFERENTIAL AMPLIFIER PERFORMANCE**



$V_0 = A_D V_D$

where  $V_D = V^+ - V^-$   
 → IDEAL BEHAVIOR  
 ≠  
 REAL BEHAVIOUR

$V_0 = A_D V_D + A_{CM} V_{CM}$

where  $V_{CM} = \frac{V^+ + V^-}{2}$

≠ 0  
 AVERAGE VALUE  
 OF 2 VOLTAGES

A DIFF. AMPL. IS CHARACTERISED BY

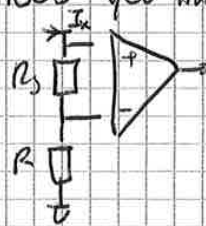
$CMRR = 20 \log_{10} \left( \frac{A_D}{A_{CM}} \right)$  [dB]

EXPRESSES HOW LARGE IS DIFFERENTIAL GAIN RESPECT TO COMMON MODE GAIN

IDEAL CASE:  $A_{CM} = 0 \rightarrow CMRR \rightarrow \infty$

REAL CASE  $A_{CM} \neq 0 \rightarrow V_0 \neq 0$  EVEN THOUGH  $V_D = 0$

IT INTRODUCES AN IMPORTANT ERROR CONTRIBUTION IN MANY SITUATIONS YOU HAVE TO CONSIDER IT 1%



↳ LIKE IN THIS ONE

!  $V^+$  AND  $V^-$  LIMITED BY POWER SUPPLY REGARDLESS OF  $V_D$

$V_S = 12V$

$V_D = 3V \rightarrow$

we cannot apply 10V, 7V cause  $V_{in}$  Amplifier input-range  $\pm 5V$  saturation

**LOAD EFFECT**

→ INPUT IMPEDANCE →  $R \sim G \parallel C$  NOISE

→ CAUSE NOT NEGLECTIBLE EFFECT FOR AC MEASUREMENT



$Z_{IN} = R_{IN} \parallel \frac{1}{j\omega C_{IN}} = \frac{R_{IN}}{1 + j\omega R_{IN} C_{IN}}$

MAINLY @ H.F

WITH A SOURCE WHICH HAS HIGH  $Z_{out}$

as  $f \gg \Rightarrow$  > EFFECT OF CAPACITANCE!

$V_{IN} = V_G \frac{Z_{IN}}{Z_{IN} + R_G} = \frac{R_{IN}}{R_G + R_{IN} + j\omega R_G R_{IN} C_{IN}}$

$Z_{IN} \ll$  NOT NEGLECTIBLE EFFECT AT BASSBAND ( $f_{max} = \frac{B}{S}$ )

IDEAL IF  $\left\{ \begin{array}{l} R_G \rightarrow 0 \\ R_{IN} \rightarrow \infty \end{array} \right\}$  RATIO = 1  $\Rightarrow$  DUE TO BOTH SOURCE AND DAQ BOARDS

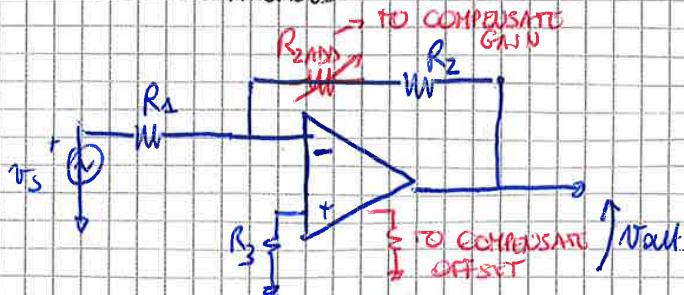
THE COMPENSATION OF DRIFT CAN BE DONE IN 2 WAYS

DIGITAL WAY

CONVENIENT BECAUSE IT ALLOWS THE USE OF VARIABLE COMPONENTS TO BE AVOIDED

ANALOG WAY

BY MEANS OF VARIABLE COMPONENTS WHICH COULD HAVE DRIFTS VERY LARGE



$R_1 = 1 \text{ k}\Omega$   
 $R_2 = 10 \text{ k}\Omega$   
 $G = 10$

$$V_{out} = - \left( \frac{R_2}{R_1} \right) v_s$$

$$V_{out} = - G v_s$$

but we have offset voltage

$$V_{out} = - G (v_s + V_{off})$$

$$V_{out} \rightarrow V_{off} G = + G v_s$$

$$v_s = - \frac{V_{out}}{G} + V_{off} A_0 \Rightarrow v_s = A_1 V_{out} + A_0$$

$A_0 = \text{constant}$  stored in NON-VOLATILE MEMORY

1) we shortcircuit the  $v_{in}$  so find  $A_0 = 100 \mu\text{V}$

2) we apply known value  $v_{s \text{ not}} = 100 \text{ mV}$

we obtain  $V_{out} = 0.95 \text{ V}$

We now find  $A_1 = \frac{v_s - A_0}{V_{out}} = \frac{100 \text{ mV} - 100 \mu\text{V}}{0.95 \text{ V}}$

slightly different from  $G$  ( $G_{\text{new}} = 9.95$ )

we store  $A_0, A_1$  in memory of DAC

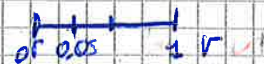
But  $V_{OFF} \frac{RTI - MIN}{RTI - MAX} = 1 \text{ mV}$

time-drift  $\Rightarrow 10 \text{ mV/s} \rightarrow$  input offset can become on the order of  $10 \text{ mV}$

After 1 year

$$V_{OFF} \frac{RTI}{MIN} = 5 \text{ mV}$$

$$V_{out \text{ off}} = G V_{off} = 50 \text{ mV}$$



if we don't compensate with analog circuit it's possible that half of the range can be used



IN MANY CASES IT'S BETTER TO HAVE VARIABLE COMPONENTS  $\rightarrow$  SO USE ANALOG ADJUSTMENT BUT IT INTRODUCES THE PROBLEM OF DRIFT  $\rightarrow$  TO SOLVE: APPLY FREQUENTLY INTERNAL ADJUSTMENT!  
 (DAC STORES VALUES IN NON VOLATILE MEMORY  $\rightarrow$  WHEN DRIFT IS RECEIVED)

## SPECIFICATIONS OF A COMMERCIAL DAQ BOARD

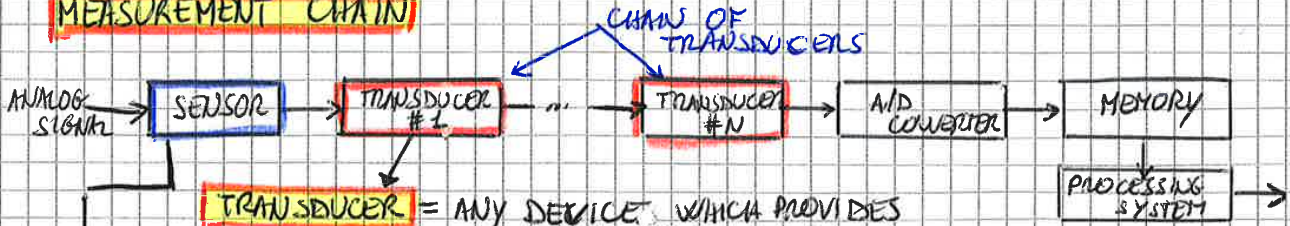
### PCI-6024E - MAIN CHARACTERISTICS:

- DC COUPLED INPUTS
  - INPUT CHANNELS: 16 SINGLE-ENDED OR 8 DIFFERENTIAL
  - AMPLIFIER CHARACTERISTICS
    - INPUT IMPEDANCE:  $100 \text{ G}\Omega \parallel 100 \text{ pF}$ 
      - @ LF IS NEGLIGIBLE
      - @ HF HAS TO BE CONSIDERED
    - CMRR ( $60 \pm 60 \text{ Hz}$ ): 90 dB
    - GAINS  $\rightarrow$  REFERRED TO EACH VOLTAGE  $\pm 1 (\pm 5 \text{ V})$  - corresponds to the input range of the ADC
      - $\swarrow$  CHECK IF PROGRAMMABLE FOR EACH CHANNEL WHEN YOU SELECT A BOARD
  - ADC  $\rightarrow$  SUCCESSIVE APPROXIMATION
    - $\rightarrow f_{\text{SAMPL}} = 200 \text{ kSa/s} \rightarrow 100 \text{ kHz}$  WITHOUT ALIASING
      - @  $f = 500 \text{ kHz} \rightarrow$  PASS-BAND HAS AN EFFECT OF 30%
    - $\rightarrow$  RESOLUTION: 12 BIT
    - $\rightarrow$  OFFSET ERROR  $\rightarrow$  AFTER INTERNAL ADJUSTMENT IS LOWER FOR MORE THAN 3 ORDERS OF MAGNITUDE
    - $\rightarrow$  GAIN ERROR  $\rightarrow$  AFTER INTERNAL ADJ. IS LOWER OF 2 ORDERS OF MAGNITUDE
- } IMPROVEMENTS IN THE PERFORMANCE
- $\rightarrow$  CROSS TALK  $\rightarrow -60 \text{ dB} \rightarrow V_{\text{crosstalk}} = \frac{V_{\text{adj}}}{1000}$ 
    - $\rightarrow$  THE VOLTAGE ON THE CHANNEL n DUE TO THE VOLTAGE OF ADJACENT CHANNEL WAS AN UNCERTAINTY CONTRIBUTION
- IN ORDER TO HAVE A MINIMUM CROSS-TALK EFFECT (VOLTAGE)
- $\downarrow$
- ① NOT ADJACENT CHANNELS (IF YOU HAVE A SCAN LIST)
  - ② ASCENDING (OR DESCENDING) ORDERING ON THE INPUT SIGNALS!
- ALWAYS USED  $\Rightarrow$
- $V_1 < V_2 < V_3 \Rightarrow$  THE EFFECT STILL REMAINS BUT WE'VE REDUCED IT
- $\rightarrow$  SETTLING TIME  $\rightarrow 10 \mu\text{s}$  WITHIN  $\pm 0.5 \text{ Vp}$ 
    - if 4 ch  $\rightarrow$  we have to wait at least  $40 \mu\text{s}$
- $f_{\text{SI}} = \frac{1}{40 \mu\text{s}} = 25 \text{ kSa/s}$

# SENSORS

16/11/16

## MEASUREMENT CHAIN



**TRANSDUCER** = ANY DEVICE WHICH PROVIDES AN OUTPUT SIGNAL THAT IS A MODIFIED VERSION OF THE INPUT SIGNAL

SOME EXAMPLES:

- AMPLIFIER/ATTENUATOR → CHANGES THE VOLTAGE
- FILTER → CHANGES THE FREQUENCY COMPONENT
- ADC → COMPLETELY CHANGES THE DOMAIN FROM ANALOG TO NUMERIC
- THERMAL VOLTAGE CONVERTER

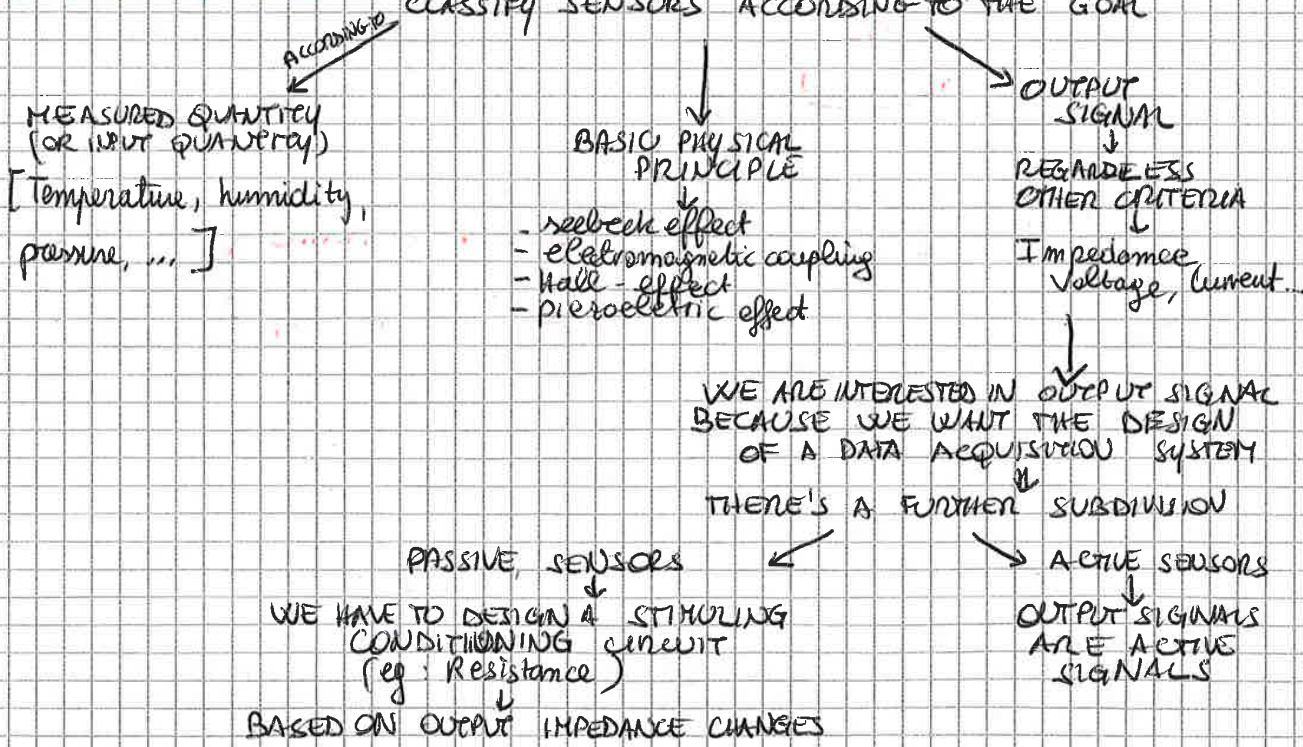
**SENSOR** = THE 1st TRANSDUCER WHICH SENSES THE QUANTITY UNDER MEASUREMENT

EXAMPLES

- THERMOCOUPLE → COUPLE OF 2 DIFFERENT METALS
- STRAIN GAUGE → CONVERTS A DEFORMATION INTO A RESISTANCE CHANGE
- CAPACITIVE HUMIDIMETER → MATERIAL WHICH SENSES RELATIVE HUMIDITY

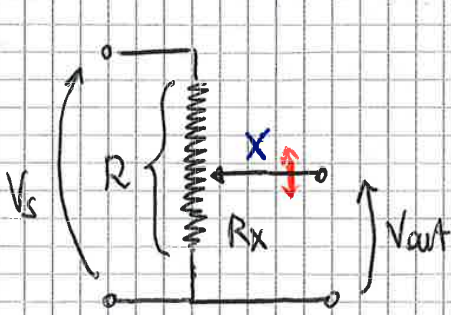
## SENSOR CLASSIFICATION

→ DIFFERENT CRITERIA ARE USED TO CLASSIFY SENSORS ACCORDING TO THE GOAL





A COMMON APPLICATION FOR VOLTAGE DIVIDERS → CAN BE POTENTIOMETER SENSOR (IN AUTOMOTIVE APPLICATIONS → TO MEASURE DISTANCE)



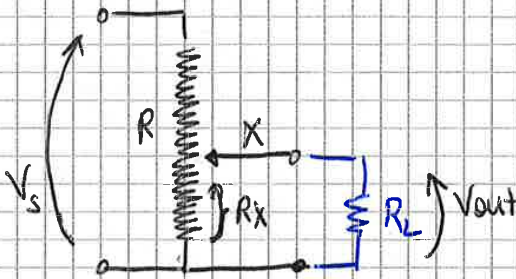
$R_x = X \cdot R$  ← ALL RESISTANCE

$\frac{V_{out}}{V_s} = X$

IT'S AN IDEAL SITUATION  
↓  
WE DON'T CONSIDER THE R OF THE INPUT VOLTMETER



IN REAL SITUATION → WE HAVE TO CONSIDER THE LOAD EFFECT DUE TO THE PRESENCE OF THE VOLTMETER



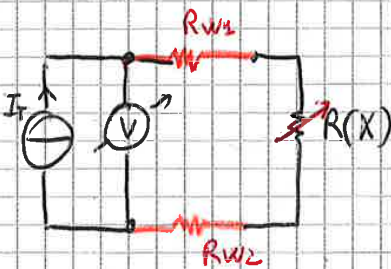
$\frac{V_{out}}{V_s} = \frac{X}{1 + \frac{R}{R_L} X}$

IT'S A VERY IMPORTANT → IF WE NEGLECT IT WE MAKE AN ERROR  
SYSTEMATIC EFFECT

IT'S BETTER TO HAVE R NEGLIGIBLE WITH RESPECT TO THE INPUT RESISTANCE RL OF THE VOLTMETER

$R = \frac{R_L}{10}$

• VOLT-AMMETER METHOD → MEANS TO SEND A TEST CURRENT I AND TO MEASURE VOLTAGE DROP



BY MEANS OF OHM LAW

$R_m = \frac{V_m}{I_T} = R(x) + R_{w1} + R_{w2}$

SYSTEMATIC EFFECT

THE CURRENT SOURCE PROVIDES A TEST CURRENT, MEASURING THE VOLTAGE WE HAVE THE RESISTOR BUT ALSO THE RESISTANCES OF WIRES AND THE CONTACT RESISTANCES

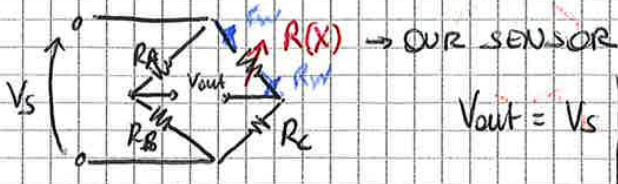
WE HAVE TO COMPARE THE EXPECTED VALUE OF  $R_{w1}, R_{w2}$

IF NEGLIGIBLE OR

IF NOT, SHORTCIRCUIT R(x) AND STORE IN THE INTERNAL MEMORY SO THAT AUTOMATICALLY SUBTRACTS THE RESULT

BUT CONTACT RESISTANCES DEPENDS ON RANDOM VARIABLES.

• **UNBALANCED WHEATSTONE BRIDGE** → IT'S LIKE A DOUBLE VOLTAGE DIVIDER!



$$V_{out} = V_s \left[ \frac{R_B}{R_B + R_A} - \frac{R_C}{R_C + R(X)} \right]$$

INPUT-OUTPUT RELATIONSHIP

$V_{out}$  IS A FUNCTION OF  $R$   
THAT IS A FUNCTION OF  $X$

$$V_{out} = f[R(X)]$$

↓  
WE WANT

$$\frac{R_B}{R_A} = \frac{R_C}{R(X_0)}$$

→ S.T. WE OBTAIN  $V_{out}(X_0) = 0$   
↓  
WE CONVERT A SMALL  $R$  CHANGE IN A SMALL  $V$  CHANGE BUT AROUND 0

↓  
S.T. WE HAVE A LIMITED NUMBER OF DIGIT!

!  $\frac{R_B}{R_A} = \frac{R_C}{R(X_0)}$  → THE UNITARY RATIO ALLOWS THE MAXIMUM BRIDGE SENSITIVITY (LARGER VOLTAGE SIGNAL) BUT ALSO THE STRONGEST NON-LINEARITY

WE HAVE TO FIND A TRADE-OFF BETWEEN NON-LINEARITY & SENSITIVITY

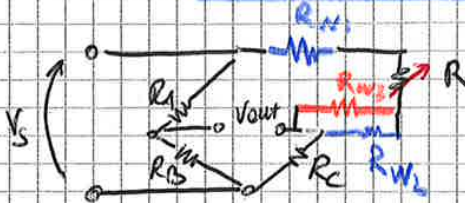
↓  
IF LINEARITY IS A REQUIREMENT → INCREASE THE RATIO!

↓  
IF WE APPLY AN HIGHER VOLTAGE → > BRIDGE SENSITIVITY BUT PAY ATTENTION TO SELF-HEATING PROBLEMS!

THERE'S AN OTHER PROBLEM → DUE TO THE PRESENCE OF WIRE AND CONTACT RESISTANCES  $R_w$

↓  
2 POSSIBLE SOLUTIONS

**3-WIRE CONNECTION**

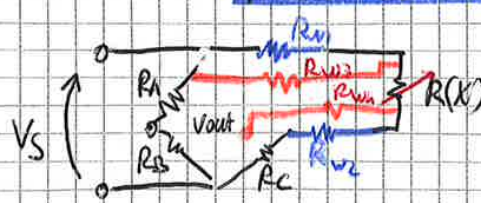


YOU ADD A CONNECTION  $(R_{W1} + R(X))$  AND  $(R_C + R_{W2})$  IN OPPOSITE ARMS OF THE BRIDGE

↓  
A POSSIBLE SOLUTION IS  $R(X_0) = R_C$

AS A CONSEQUENCE THERE'S NO MORE PERFECT COMPENSATION

**4-WIRE CONNECTION**



IF  $R_A, R_C \gg R(X)$

↓  
WE SOLVE THE PROBLEM BY MOVING THE EFFECT FROM  $R(X)$  TO  $R_A, R_C$

↓  
WHEN RESISTORS ARE VERY DIFFERENT

**PLATINUM RTD (PTD)** → EMPLOYED TO ARRANGE

HIGH ACCURACY  
RESISTIVE THERMOMETER

THERMOMETER FOR  
INDUSTRIAL APPLICATIONS

INPUT/OUTPUT RELATIONSHIP → DEPENDENT ON TEMPERATURE RANGE  
(CALENDAR-VAN DUSEN)

- RANGE (0 ÷ 850) °C

$$R = R_0 (1 + A\theta + B\theta^2)$$

- RANGE (-200 ÷ 0) °C

$$R = R_0 [1 + A\theta + B\theta^2 + C(\theta - 100)\theta^3]$$

**CALIBRATION FUNCTION** → USUALLY THIS EXPRESSION IS EXTENDED DOWN TO -40 °C

$$\theta = \frac{-AR_0 + \sqrt{A^2R_0^2 - 4BR_0(R_0 - R)}}{2BR_0}$$

THE VALUE OF (A, B) CONSTANTS DEPENDS ON THE PLATINUM PURITY

$R_0$  = PTD RESISTANCE @ 0 °C

PE 100 →  $R_0 = 100 \Omega$

PE 25 →  $R_0 = 25 \Omega$

PE 1000 →  $R_0 = 1000 \Omega$  → TO MINIMIZE

UNCERTAINTY CLASSES → INSTRUMENTAL UNCERTAINTY

THE PROBLEM OF WIRE AND CONTACT

DEFINED CLASSES

FOR EACH RANGE YOU HAVE A TOLERANCE VALUE WHICH IS A FIXED VALUE

→ SYSTEMATIC EFFECT → DUE TO WIRE AND CONTACT RESISTANCES (LOAD EFFECT)

WIRE EFFECTS HAVE TO BE COMPENSATED OR 4-WIRE CONNECTION HAS TO BE EMPLOYED (BECAUSE CONTACT RESISTANCES ARE NOT WELL REPRODUCIBLE)

→ SELF-OVERHEATING → WITH HIGHER  $I_T$  IS A BIG PROBLEM (IMPORTANT IN THE DESIGN)

FOR → WIRE WOUND SENSORS → (0.05 ÷ 0.3) °C/mW

→ THIN FILM → 0.005 °C/mW

THERMOELECTRIC VOLTAGE → 10  $\mu V$  CAUSES A TEMPERATURE ERROR  $\Delta\theta = 0.25$  °C

USING MATERIALS WITH LOW THERMOELECTRIC COUPLING ETC... IS A GOOD WAY TO MINIMIZE THIS PROBLEM

! FOR A PE-100 → USE OF  $I_T = 1$  mA IS A GOOD TRADE-OFF BETWEEN SELF-OVERHEATING EFFECTS OF  $I_T$

23/11/16

**STRAIN RESISTIVE SENSORS**

→ THE QUANTITY UNDER MEASUREMENT IS THE STRAIN = CONSEQUENCE OF AN EXTERNAL STIMULA

2 → POSSIBLE STRAINS

EXPANSION (POSITIVE)

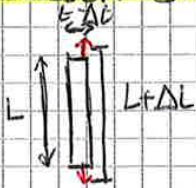
CONTRACTION (NEGATIVE)

STRAIN  $\epsilon$  IS DEFINED AS THE RATIO BETWEEN LENGTH CHANGE  $\Delta L$  WITHIN LENGTH  $L$  OF AN OBJECT

$$\epsilon = \frac{\Delta L}{L}$$

**POISSON STRAIN**

→ IF WE APPLY A TRACTION FORCE TO A METALLIC ROD THE OBJECT IS SUBJECTED



BOTH TO AN EXPANSION ON THE FORCE DIRECTION

AND TO A CONTRACTION IN THE TRANSVERSE DIRECTION WITH RESPECT TO THE FORCE

POISSON MODULE

$$\nu = - \frac{\epsilon_t}{\epsilon} = - \frac{\Delta L_t / L_t}{\Delta L / L}$$

STRAIN → COULD BE THE QUANTITY UNDER MEASUREMENTS BECAUSE

IT GIVES INFORMATION'S ABOUT THE STRESS THE OBJECT IS SUBJECTED AND ABOUT ITS RELIABILITY

→ IT ALLOWS OTHER QUANTITIES TO BE OBTAINED (F, P,  $\sigma$ , ...)

IT NEEDS A DOUBLE STAGE:

QTY OF INTEREST: FORCE

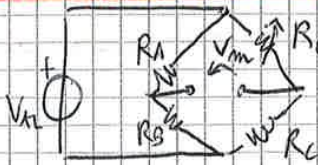
↓  
WE OBTAIN STRAIN FROM R  
WE OBTAIN FORCE FROM STRAIN

2 CATEGORIES OF STRAINS

BOUNDED

UNBOUNDED → METAL WIRES AREN'T FIXED INTO A STRUCTURE

UNBALANCED BRIDGE WITH 1 ACTIVE STRAIN GAUGE



$$\frac{R_A}{R_B} = \frac{R_{CD}}{R_C}$$

$V_m = \phi$  WHEN THE SENSOR IS UNLOADED

$$V_m = V_m \left( \frac{R_B}{R_B + R_A} - \frac{R_D}{R_D + R_C} \right)$$

$$\Delta V_m = \frac{\partial V_m}{\partial \epsilon} \epsilon = V_m \frac{k \epsilon}{4} \frac{1}{1 + \frac{k \epsilon}{2}}$$

ECC & LINEAR EXPANSION  
 $\approx \frac{V_m k \epsilon}{4}$

PROPORTIONAL TO  $\frac{k \epsilon}{\epsilon}$

⇒ SOLUTION NOT COMMONLY EMPLOYED SINCE T EFFECT USN'T COMPENSATED

UNBALANCED BRIDGE WITH ONE ACTIVE STRAIN GAUGE AND 1 INACTIVE STR GAUGE

→ EXACTLY THE SAME CIRCUIT AS BEFORE BUT WITH 2 STRAIN GAUGES

$R_{CD}$  ACTIVE

$R_{CD}$  INACTIVE

- FIXED IN A WAY TO SENSE DEFORMATION
- MOUNTED IN THE DIRECTION OF INTEREST

- MOUNTED IN TRANSVERSE DIRECTION
- USED TO MINIMIZE T EFFECT

BOTH DEPENDENT ON T IN THE SAME FORM

MINIMIZATION OF TEMPERATURE EFFECTS

$$V_m = V_m \left[ \frac{R_B}{R_A + R_B} - \frac{R_D(\theta, \nu)}{R_D(\theta, \nu) + R_C(\theta, \epsilon)} \right]$$

BUT  $R_C$  INTRODUCES 2 PROBLEMS

IF IT'S BOUNDED IT SENSES THE POISSON STRAIN  
 $R_D(\theta, \nu)$

IF IT'S UNBOUNDED IT'S NOT MECHANICALLY COUPLED AND IT'S NOT SUBJECTED TO THE SAME T AND  $\epsilon$  OF  $R_C$

25/11/16

**STRAIN-GAUGE BASED LOAD CELLS**

**LOAD CELL** = TRANSDUCER THAT CONVERTS A FORCE INTO AN ELECTRICAL SIGNAL

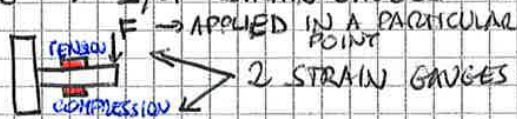
= DOUBLE STAGE DEVICE:

- 1) THROUGH A MECHANICAL ARRANGEMENT → FORCE → <sup>CONVERTED</sup> STRAIN
  - 2) THROUGH A STRAIN GAUGE → STRAIN → RESISTANCE
- (AND THEN A RESISTANCE → VOLTAGE <sup>CONNECTED TO THE ACQUISITION SYSTEM</sup>)

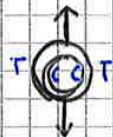
2/4 STRAIN GAUGES IN { HALF-BRIDGE } CONFIGURATION EMPLOYED TO → MAXIMIZE SENSITIVITY  
 ↓  
 MINIMIZE T EFFECT

SEVERAL MECHANICAL ARRANGEMENTS HAVE BEEN DESIGNED IN ORDER TO CONVERT A FORCE INTO A STRAIN (IT DEPENDS ON THE QTY OF INTEREST AND ON THE APPLICATION):

- SIMPLE BENDING → 2/4 STRAIN GAUGES IN PUSH-PULL CONFIGURATION



- NOT SUITABLE IF YOU DON'T HAVE A PRECISE POINT OF APPLICATION
- ↓
- HIGH SENSITIVITY WITH RESPECT TO THE POINT OF APPLICATION
- SUITABLE FOR LOW RANGE (UP TO 5 kN)



- 4 STRAIN GAUGES
- SUITABLE FOR HIGH RANGE (UP TO 1000 kN)

- DOUBLE BENDING → TENSION AND COMPRESSION ARE ON THE SAME SURFACE BEAM THANKS TO THIS PARTICULAR ARRANGEMENT
- ↓
- LOW SENSITIVITY WITH RESPECT TO THE POINT OF FORCE APPLICATION



T COMPENSATION DEPENDS ON REPRODUCIBILITY OF STRAIN GAUGES

S-TYPE → S-SHAPE MECHANICAL ARRANGEMENT

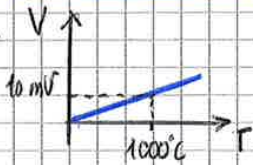
THANKS TO THE INTERNAL HOLE WE HAVE AN AREA SUBJECTED TO COMPRESSION AND ONE OTHER TO EXPANSION



- COMPRESSION/TENSION → COLUMN TYPE → BASED ON THE EFFECT ON BOTH THE DIRECTION OF INTEREST AND ON TRANSVERSE DIRECTION (→ MAX SENSITIVITY)
- SHEAR → STRAIN GAUGE FIXED TO A PARTICULAR ANGLE WITH RESPECT TO THE DIRECTION OF INTEREST (SMALLER AND STRONGLY RESISTANT TO TRANSVERSE LOADING)

**COMMERCIAL THERMOCOUPLES**

→ BY CONVENTION, THE COUPLE OF USED METALS ARE INDICATED BY MEANS OF A LETTER



EXPECTED VOLTAGES ARE ON THE ORDER OF mV

$$S_R = \frac{10 \text{ mV}}{1000^\circ\text{C}} = 10 \mu\text{V}/^\circ\text{C}$$

α → ISN'T CONSTANT WITH TEMPERATURE

NOT LINEAR BEHAVIOR OF THE THERMOELECTRIC VOLTAGE

$$e_{AB} = \sum h_i \Delta\theta^i$$

$k_i, h_i$  FROM INTERNATIONAL STANDARDS

$$\Delta\theta = \sum k_i e^i_{AB}$$

→ FOUND BY MEANS OF HIGH ORDER POLYNOMIAL FACTOR

**UNCERTAINTY CLASSIFICATION** → DIVIDED IN NORMAL/SPECIAL

STANDARDS THAT FIXES THE VALUE OF THE COEFFICIENTS

eg:  $1.7^\circ\text{C}, 0.5\%$   
 $\frac{0.5}{100}$  reading

E-type normal thermocouple

$$\delta\theta = 0.5\% \cdot 400^\circ = 2^\circ\text{C}$$

$$\max\{2^\circ\text{C}, 1.7^\circ\text{C}\} = 2^\circ\text{C} = \delta\theta$$

(IF YOU WANT A BETTER UNCERTAINTY → DO A GOOD CHARACTERIZATION.)

**TEMPERATURE LIMITS** → MEASUREMENT RANGES REFER TO THERMOCOUPLE METALS, NOT TO THE SHEATH

FOR HIGH T ARE EXPENSIVE

USUALLY SPECIAL SHEATHS ARE EMPLOYED ONLY FOR THE THERMOCOUPLE PART EXPOSED TO HIGH TEMPERATURES



VERY THIN TO OBTAIN A LOW TIME CONSTANT (VERY FAST ANSWER WITH RESPECT TO TEMPERATURE TRANSIENT)

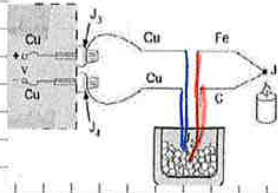
$\theta_1$  HAS TO BE KNOWN

$\theta_0$  COULD BE DIFFERENT

SO IT'S NECESSARY TO NOT INTRODUCE FURTHER THERMOCOUPLES / SO EXTERNAL CABLES

SAME THERMOCOUPLE METALS BUT LARGER DIAMETER AND STANDARD SHEATH

A FURTHER STEP → IS TO USE THE ICE BATH AS THE ISOTHERMAL BLOCK

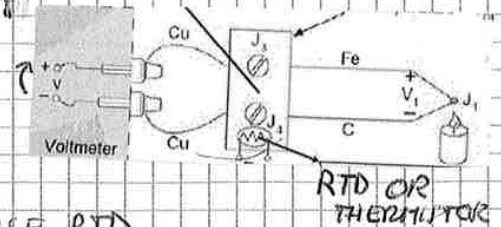


ICE FROM PURE WATER (BECAUSE OF SALT)  
CONTAINER → WELL INSULATED

! USED FOR VERY PRECISE MEASUREMENTS  
AT NMIs AND SECONDARY LABS

IN INDUSTRIAL APPLICATIONS → IT'S NOT CONVENIENT  
TO USE THE ICE-BATH

THE TEMPERATURE OF THE ISOTHERMAL  
BLOCK IS MEASURED BECAUSE J<sub>3</sub> AND  
J<sub>4</sub> BECOME THE REFERENCE  
JUNCTION



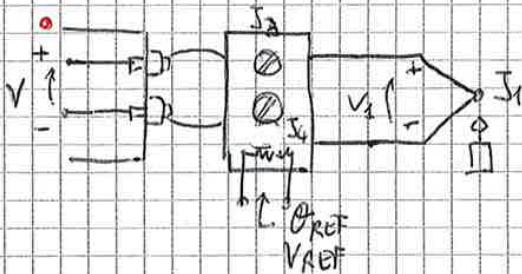
IN ORDER TO MEASURE T ON THIS BLOCK I USE RTD  
OR A THERMISTOR INTEGRATED INTO THE MATERIAL  
(PASSIVE SENSOR)

note

A DATA ACQUISITION SYSTEM WORKS IN A PROCEDURE CALLED **SOFTWARE COMPENSATION**  
WHICH FOLLOWS THESE STEPS

- RTD/THERMISTOR RESISTANCE IS MEASURED AND T<sub>REF</sub> IS ESTIMATED
- THE REFERENCE JUNCTION VOLTAGE V<sub>REF</sub> IS OBTAINED BY MEANS OF T<sub>REF</sub>

$$V_{REF} = \sum h_n \theta_{REF}^n$$



V<sub>1</sub> IS THE CORRECTION TO V  
SO THE MEASURED VOLTAGE  
V IS ADDED TO V<sub>REF</sub>  
IN ORDER TO  
OBTAIN V<sub>1</sub> (Δθ = θ<sub>1</sub> - θ<sub>REF</sub>)  
(WITH THE LAW OF ADDITIVE VOLTAGES)

- θ<sub>1</sub> IS OBTAINED WITH V<sub>1</sub>

I USE A THERMOCOUPLE INSTEAD OF USING A DEVICE THAT MEASURES  
THE ABSOLUTE TEMPERATURE BECAUSE:

- MEASUREMENT RANGES WITH THERMOCOUPLES ARE LARGER  
THAN OTHER TEMPERATURE SENSORS
- THERMOCOUPLES ARE LARGER THAN <sup>THERMISTORS</sup> RTD
- ISOTHERMAL REFERENCE IS USED FOR MANY THERMOCOUPLE ELEMENTS  
SEVERAL CONNECTIONS  
WITH ONE SOFTWARE PROCEDURE

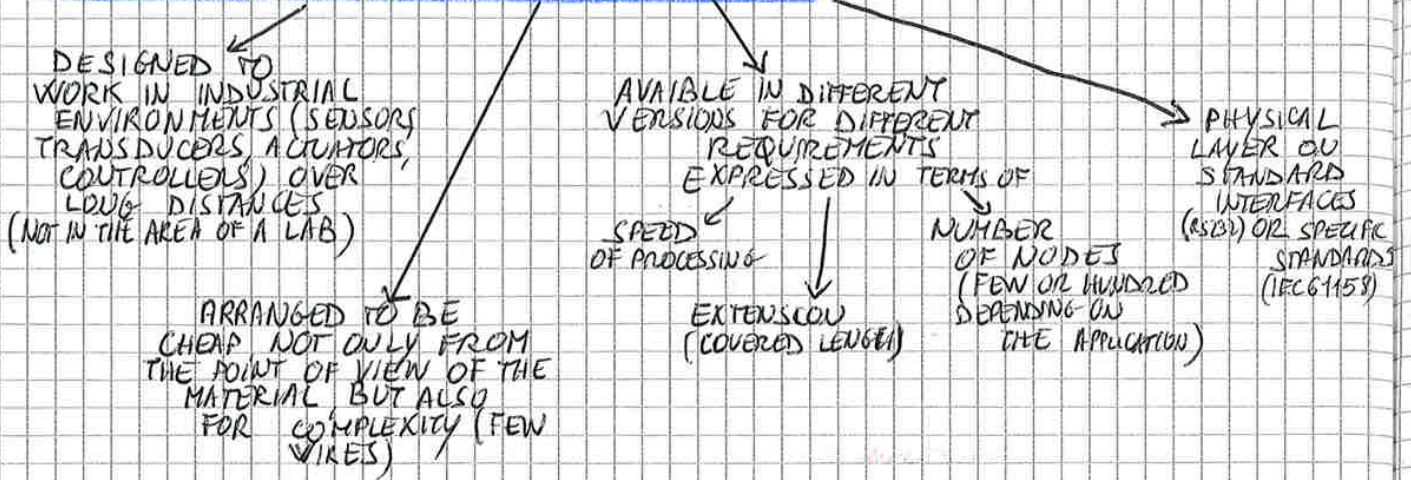


# INDUSTRIAL BUSES

30/11/16

## REQUIREMENTS OF A DATA ACQUISITION SYSTEM

### MAIN CHARACTERISTICS OF AN INDUSTRIAL BUS



NAME USED TO INDICATE ANY INDUSTRIAL BUSES

### FIELD BUS → ONE OF MOST EMPLOYED

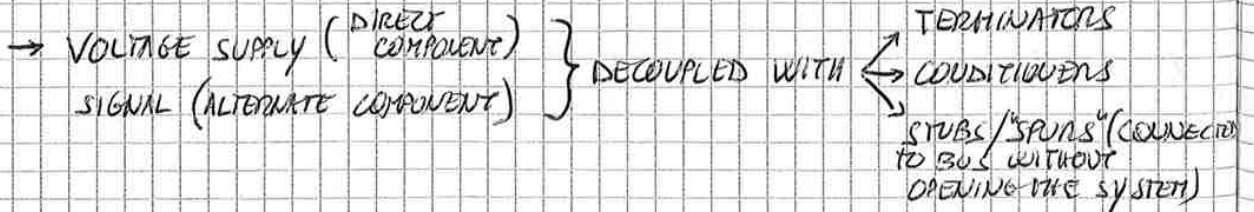
ALL DIGITAL (NO ANALOG SIGNALS IN COMMUNICATION) SERIAL 2-WAY COMMUNICATION SYSTEM (POSSIBILITY TO TRANSFER DATA IN 2 DIRECTIONS) DEFINED IN STANDARD IEC-61158

→ CHEAP BUS WITH A SIMPLE WIRING

BASED ON ONLY 2 WIRES, A SHIELDED (TO MINIMIZE THE EFFECT WITH RESPECT TO NOISE) TWISTED-PAIR CABLE FOR BOTH SUPPLY-VOLTAGE AND SIGNAL

SEGMENTS WITH LENGTH UP TO 1 km AND 10 CONNECTED DEVICES (LONGER DISTANCES BY MEANS OF REPEATERS)

FIXED TRANSMISSION SPEED (31.25 kbit/s)



### BUS COMPONENTS → THE CABLE SECTION HAS TO BE SUITABLE FOR THE SUPPLY VOLTAGE THAT HAS TO BE SUBMITTED

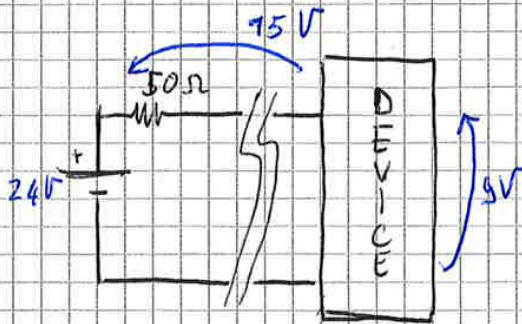
STARTING FROM THE MAIN CHARACTERISTICS WE CAN ESTIMATE

THE DISTANCE WITH THE POWER SUPPLY

THE NUMBER OF INTERCONNECTED DEVICES

**BUS DESIGN** → POWER SUPPLY ATTENUATION / CONSTRAINTS } FIX

• THE MAXIMUM LENGTH



$V_s = 24 V$

$V_{min} = 9 V$

$I_{min} = 20 mA$

} BY CONNECTED DEVICES

$R_{eime} = \frac{V_s - V_{min}}{I_{min}} = \frac{24 V - 9 V}{20 mA} = \frac{15 V}{20 mA} = 750 \Omega$

$L_{max} = \frac{R_{eime} - R_{row sup}}{\text{resist. of line}} = \frac{750 \Omega - 50 \Omega}{40 \Omega/km} \approx 15.9 km$

A SINGLE DEVICE CAN BE CONNECTED AT A DISTANCE OF 15.9 km

• THE NUMBER OF CONNECTED DEVICES

$V_{bus} = 15 V$

$R_{p.s.} = 50 \Omega$

$I_{max} = \frac{15 V}{50 \Omega} = 300 mA$

↑  
max current with a certain number of devices at a distance

Max number of devices :

$N = \frac{I_{max}}{I_{d. min}} = \frac{300 mA}{20 mA} = 15$

• LENGTH CONSIDERING < TALKER / PUBLISHER → generates a signal with  $V_{pp} = 0.75 V$  max RECEIVERS / LISTENERS

↳ each is able to decode a signal with  $V_{pp} = 0.15 V$  min

$A_{tt max} = 20 \log \left( \frac{V_{pub min}}{V_{list min}} \right) = 20 \log \left( \frac{0.75}{0.15} \right) \sim 14 dB$

$L_{max} = \frac{A_{tt max}}{A_{tt min}} = \frac{14 dB}{3 dB/km} = 4.7 km$

↑  
minimal attenuation considering the specifications of the bus

↑  
Maximum distance for ideal cable

↓  
Specification of the protocol : the maximum sum cannot exceed a total length of 1300 m

**BUS ACCESS** → IS MANAGED WITH 2 LEVELS OF COMMUNICATION:

• **SCHEDULED COMMUNICATION** → MANAGED ACCORDING TO A DETERMINISTIC TABLE CALLED LAS (= LINK ACTIVE SCHEDULER)

DEVICES ON A FIELDBUS COULD BE

← BASIC DEVICES WITHOUT LAS CAPABILITIES

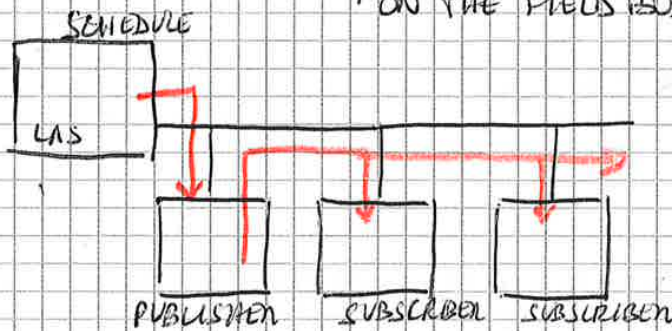
→ LINK MASTER DEVICES THAT ARE CAPABLE OF BECOMING THE LAS  
↓  
IN THE BUS CONTROLLER

→ DEVICES ARE IDENTIFIED BY MEANS OF AN ADDRESS

→ ONCE YOU'VE IDENTIFIED YOUR BUS AND THE TIME, YOU KNOW THE TRANSMISSION RATE

↓  
SO YOU CAN BUILD A DETERMINISTIC TABLE

↓  
SCHEDULED COMMUNICATION IS USED FOR THE REGULAR CYCLIC TRANSFER OF DATA AMONG DEVICES ON THE FIELDBUS



ON THE BUS THERE'S A CONTROLLER THAT HAS THE CAPABILITY TO MANAGE THE TRANSMISSION WHICH CAN BE  
↓  
SCHEDULED      UNSCHEDULED

SCHEDULED COMMUNICATION IS THE HIGHEST PRIORITY ACTIVE FOR THE LAS

↓  
ONCE THE DEVICE A RECEIVES, IT BECOMES THE PUBLISHER. THE OTHERS ARE SUBSCRIBERS. THE PUBLISHER RECEIVES A DATA MESSAGE AND TRANSMITS IT TO OTHERS

• **UNSCHEDULED COMMUNICATION** → CAN BE PERFORMED BETWEEN THE TRANSMISSION OF SCHEDULED MESSAGES

↓  
THE LAS SENDS A PASS-TOKEN (PT) MESSAGE TO EACH DEVICE WHICH HAS THE POSSIBILITY TO SEND DATA THAT AREN'T IN SCHEDULING

THE LAS HAS A LIST → LIVE LIST → THAT ALLOWS TO KNOW THE ACTIVE DEVICES

## PROFIBUS PA = MODIFIED VERSION OF THE FIELDBUS

→ BUS WITH 2 WIRES (SHIELDED TWISTED PAIR CABLE) FOR BOTH SUPPLY VOLTAGE AND SIGNAL

→ DATA TRANSMISSION:

- DIGITAL DIFFERENTIAL SIGNALS, BIT-ASYNCHRONOUS MANCHESTER ENCODING

- 8-BIT CHARACTER (≠ FROM FIELDBUS)

- DATA PACKET WITH 16-BIT CRC (ADDED TO PREAMBLE START-STOP) (ALLOWS A GOOD PRECISION)

→ FIXED TRANSMISSION RATE: 31.25 kbit/s

→ LINE AND TREE TOPOLOGY WITH TERMINATION

→ NUMBER OF STATIONS (> THAN FIELDBUS)

↳ UP TO 32 WITHOUT REPEATERS

UP TO 126 (MAX 4 REPEATERS)

↑  
WHEN YOU HAVE A LONGER LENGTH OF THE BUS

THE CHOICE OF THE BUS A PART FROM ELECTRICAL CHARACTERISTICS, COULD BE REPRESENTED ACCORDING TO THE MANAGED PROCESS.

IF  $\theta$ , THE ORIENTATION ANGLE OF THE CONSIDERED AREA WITH RESPECT TO THE SOURCE;

$$E_e = \frac{I_e \cos \theta}{d^2}$$

IRRADIANCE CHANGES WITH RESPECT TO THE ANGULAR OBSERVATION (COSINE LAW)

**SOLID ANGLE**  $\rightarrow \Omega$ , REPRESENTS A PART OF AN OBSERVER'S VISUAL FIELD



P: OBSERVER (OUR EYE)  
r: RADIUS

$$\Omega = \frac{A}{r^2}$$

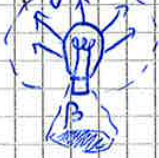
[sr]  $\rightarrow$  STERADIAN  
RATIO BETWEEN AREA OF OBSERVATION & SQUARE OF RADIUS

IT'S INDEPENDENT ON  $r$ ! VALUE OBTAINED ONCE YOU'VE DEFINED THE AREA YOU WANT TO SEE TRANSMIT

IF TOTAL VISUAL FIELD IS A SPHERE  $\Omega = \frac{4\pi r^2}{r^2} = 12.57$  sr

NO SOLID ANGLE IS GREATER THAN THIS IT'S THE MAXIMUM SOLID ANGLE  $\rightarrow$  FOR AN ISOTROPIC SOURCE

if we have an isotropic source except a cone shadow with angle  $\beta$



$$A = 2\pi \left(1 - \cos\left(\frac{\beta}{2}\right)\right) r^2 = 2\pi \left(1 - \cos\left(\frac{360 - \beta}{2}\right)\right) r^2$$

$$\Omega = 2\pi \left(1 - \cos\left(\frac{360 - \beta}{2}\right)\right)$$

$\leftarrow$  if source is isotropic

**PHOTOMETRIC QUANTITIES**

(PERCEIVED BY HUMAN EYES)

• **LUMINOUS INTENSITY**,  $I_v$  [cd]  $\rightarrow$  REPRESENTS LIGHT INTENSITY OF AN OPTICAL SOURCE AS PERCEIVED BY THE HUMAN EYE

$$1 \frac{W}{sr} = 683 \text{ cd} \quad (@ 555 \text{ nm})$$

• **LUMINOUS FLUX**,  $\Phi_v$  [lm]  $\rightarrow$  REPRESENTS THE LIGHT POWER OF AN OPTICAL SOURCE AS PERCEIVED BY HUMAN EYE

$$1 \text{ cd} = 1 \text{ lm/sr}$$

$$I_v = \frac{\Phi_v}{sr}$$

• **ILLUMINANCE**,  $E_v$  [lux]  $\rightarrow$  REPRESENTS THE LUMINOUS FLUX INCIDENT PER UNIT AREA

$$1 \text{ lux} = 1 \text{ lm/m}^2$$

USED TO CHARACTERIZE ILLUMINATION CONDITIONS (DISTANCE IS AN IMPORTANT QUESTION)

• **SPECTRAL RESPONSE** → DESCRIBES THE PHOTODIODE SENSITIVITY TO OPTICAL RADIATION OF DIFFERENT WAVELENGTHS

↓  
ONLY A SMALL PART OF THE OPTICAL RADIATION SPECTRUM IS RECEIVED BY THE SENSOR (OUR EYES FOR EXAMPLE)

↙ IT'S A RELATIVE MEASURE

CALCULATED NORMALIZING THE OUTPUT WITH RESPECT TO THE OUTPUT OF MAXIMUM SENSITIVITY

• **SENSITIVITY** → PROVIDED DEPENDING ON THE OUTPUT TYPE:

- OUTPUT UNITS PER UNITS OF ILLUMINANCE FOR SENSOR WITH SPECTRAL RESPONSE IN THE VISIBLE RANGE (PHOTODIODE → A/LUX)  
(PHOTODIODES → V/LUX)
- OUTPUT UNITS PER UNITS OF INCIDENT RADIATION (A/W)

• **NOISE** → EXPRESSED BY MEANS OF NEP (= NOISE EQUIVALENT POWER)

→ USUALLY PROVIDED AS LIGHT LEVEL REQUIRED TO OBTAIN A SNR OF UNITY

→ IS THE RATIO BETWEEN OUTPUT NOISE CURRENT FOR 1Hz BANDWIDTH

MAXIMUM ABSOLUTE SENSITIVITY (@ ap)

$$NEP = \frac{\text{noise current [A/}\sqrt{\text{Hz}}]}{\text{absolute sensitivity [A/W]}} \quad [\text{W}/\sqrt{\text{Hz}}]$$

↘ EXPRESSES THE MINIMUM DETECTABLE INPUT POWER OF A PHOTODIODE

# RELIABILITY BASIC CONCEPTS - PART 1

**RELIABILITY** = EXPECTED LIFETIME OF A DEVICE IN DEFINED CONDITIONS  
 WHAT FUNCTIONALITIES IT HAS AND ITS BEHAVIOUR FOR A CERTAIN TIME INTERVAL  
 IT HAS TO BE AS LONG AS POSSIBLE (IT DEPENDS ON THE SYSTEM)

IT'S EXPECTED THAT DIFFERENT CONDITIONS AFFECT THE LIFETIME  
 QUANTITATIVE PARAMETERS  $\rightarrow$  ARE RANDOM VARIABLES, BY EMPLOYING THE BASICS OF PROBABILITY THEORY

WE HAVE TO DISTINGUISH BETWEEN  $\left. \begin{array}{l} \rightarrow \text{NON REPAIRABLE} \\ \rightarrow \text{REPAIRABLE} \end{array} \right\}$  SYSTEMS

WE REFER TO PROBABILITY BECAUSE WE HAVE TO REFER TO THE POPULATION OF THE DEVICES AND NOT TO A SINGULAR DEVICE

## RELIABILITY FOR NOT REPAIRABLE COMPONENTS

NON REPAIRABLE SYSTEMS  $\rightarrow$  SYSTEMS DESIGNED FOR NOT BEING REPAIRABLE THEIR LIFETIME DEPENDS ON NON REPAIRABLE COMPONENTS.

NOT REPAIRABLE COMPONENTS  $\rightarrow$  HAVE A LIFE CYCLE CALLED **REPAIR-TO-FAILURE PROCESS**



THE DEVICE STARTS IN THE WORKING STATE AND AT A CERTAIN TIME INSTANT A FAILURE OCCURS

WE'VE A FAILURE TRANSITION AND THE COMPONENT GOES TO THE FAILURE STATE.



THE POSSIBLE RANDOM VARIABLE IS THE TIME INSTANT WHEN THE FAILURE OCCURS

$z$  = TIME TO FAILURE

$\rightarrow$  RANDOM VARIABLE  $\rightarrow$  WE'VE TO INVESTIGATE ABOUT THE PROBABILITY DISTRIBUTION

$\downarrow$  ACCORDING TO THIS SCHEME

**RELIABILITY** = THE PROBABILITY THAT A COMPONENT WILL SATISFACTORILY PERFORM ITS INTENDED FUNCTION UNDER GIVEN CIRCUMSTANCES FOR A SPECIFIED PERIOD OF TIME

= PROBABILITY THAT TIME TO FAILURE IS GREATER THAN  $t$

$$R(t) = P\{z > t\} \Rightarrow \begin{cases} R(0) = 1 \\ \lim_{t \rightarrow \infty} R(t) = 0 \\ R(t) \text{ NOT INCREASING FUNCTION} \end{cases}$$

BUT IT CAN  $\rightarrow$  BE CONSIDERED CONSTANT AT CERTAIN TIME INSTANTS

**UNRELIABILITY** = THE PROBABILITY THAT A COMPONENT GOES IN THE FAILURE STATE BEFORE THE TIME  $t$

$$F(t) = P\{z < t\}$$

$\rightarrow$  CUMULATIVE PROBABILITY DISTRIBUTION OF  $z$

## BATHUB CURVE OF ELECTRONIC COMPONENTS (SHAPE OF A BATHTUB)



**BURN-IN PERIOD** → HIGH HAZARD-RATE. EVEN IF THE COMPONENT IS NEW IT HAS AN HIGH RATE TO GO TO THE FAILURE STATE (POOR RELIABILITY). THE FAILURE RATE RAPIDLY DECREASES: THIS PERIOD IS CHARACTERIZED BY INFANT MORTALITY (WEAK PART OF THE POPULATION). MANUFACTURER PROVIDES WARRANTY.

THE MANUFACTURER USUALLY DOES A BURN-IN TEST → PERFORMED IN FINAL DEVICES IN ORDER TO FIND THE WEAK PART OF THE POPULATION AND ELIMINATE IT.

APPLICATION OF STIMULUS THAT BRING THE FAILURE OF WEAK COMPONENTS.

**USEFUL LIFE PERIOD**  
THE FAILURE RATE IS ALMOST CONSTANT (FAILURES OCCUR IN A RANDOM WAY).

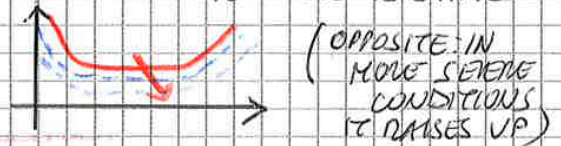
THERE'S NO A DECREASING WHEN  $t$  INCREASES → THERE'S NO MEMORY IN THE DEVICE AND NO DEPENDENCE ON THE TIME IN THE WORKING.

ELECTRONICS COMPONENTS DON'T SUFFER FROM WEAR.

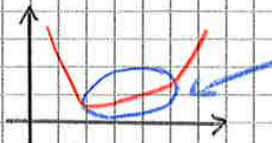
RELIABILITY OF THE COMPONENTS CAN BE IMPROVED BY USING IT IN LESS SEVERE CONDITION.

### DERATING

EFFECT: THE CURVE IS SHIFTED.



## BATHUB CURVE OF MECHANICAL COMPONENTS



DURING THE USEFUL TIME THE FAILURE RATE INCREASES, DUE TO WEAR PHENOMENA.

THE BATH-TUB CURVE → IS A VALID MODEL ONLY IF CERTAIN FAILURES ARE TAKEN INTO ACCOUNT.

EARLY FAILURE

RANDOM FAILURE (IN USEFUL LIFE)

WEAR-OUT FAILURE

→ ITS BEHAVIOUR CAN BE DIFFERENT IF OTHER FAILURES OCCUR.

MISUSE FAILURE

DUE TO UNSUITABLE STIMULI (RESISTOR WHOSE VALUE IS HIGHER THAN MAXIMUM ADMITTED)

DESIGN FAILURE

DUE TO UNSUITABLE DESIGN (DUE TO INTERACTION WITH OTHER COMPONENTS)



## EXPERIMENTAL APPROACH TO RELIABILITY

OFTEN IT'S NOT POSSIBLE TO WAIT FOR RELIABILITY OF A COMPONENT BUT IT'S BETTER TO HAVE AN EXPERIMENTAL APPROACH

$N$  COMPONENTS RANDOMLY SAMPLED ARE SUBJECTED TO A LIFE TEST (STARTING FROM  $t=0$ )  
 [IF SAMPLES NOT RANDOM - MEASURE IS BIASED]

$t_i$  - TIME-TO-FAILURE OF THE  $i$ -th COMPONENT

$N_w$  ( $N_b$ ): # OF WORKING (BROKEN) COMPONENTS AT TIME  $t$

$$\hat{R}(t) = \frac{N_w(t)}{N}$$

$$\hat{F}(t) = \frac{N_b(t)}{N} = 1 - R(t)$$

EMPIRICAL EXPECTED LIFE:  $\hat{MTTF} = \frac{1}{N} \sum_{i=1}^N t_i$  OBTAINED AT THE END OF THE TEST


EXPERIMENT CAN ELAPSE IN 2 YEARS  
 LONG EXPERIMENTAL TIME CANNOT BE ACCEPTED BECAUSE OF THE COST OF THE TEST

FOR THIS REASON IN PRACTICE → ACCELERATED LIFE TESTS ARE PERFORMED (ALT)

PARTICULAR MODELS ARE USED TO HAVE ACCELERATION FUNCTIONS

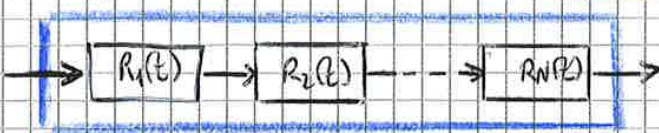
-----  $T = 30^\circ\text{C}$   
 -----  $T = 25^\circ\text{C}$

HAZARD = HIGH ACCELERATED LIFE TESTS  
 INCLUDE TESTS WITH FAST TRANSITIONS  
 APPLIED OR ALSO COMBINED  
 STIMULI (VIBRATION, HUMIDITY)



IN ORDER TO MINIMIZE EXPERIMENTAL TIME

REPRESENTATION AS AN RBS → SERIES CONFIGURATION



$E_i$  = EVENT WHERE  $i$ -TH COMPONENT IS IN THE WORKING STATE

$E$  = THE WHOLE SYSTEM MUST BE IN THE WORKING STATE

! EVENT  $E$  IS TRUE ONLY IF ALL EVENTS  $E_i$  ARE SIMULTANEOUSLY TRUE

$E_i$  ARE STATISTICALLY INDEPENDENT

$$P\{E\} = P\{E_1 \cap E_2 \cap \dots \cap E_N\} = \prod_{i=1}^N P\{E_i\}$$

BY DEFINITION  $P\{E_i\} = R_i(t)$

$$P\{E\} = R(t) = \prod_{i=1}^N R_i(t)$$

SINCE AT  $t_0$   $R_i(t_0) < 1 \Rightarrow R(t_0) < R_{i-min}(t)$

THE RELIABILITY OF THE SYSTEM IS LOWER THAN THE MINIMUM RELIABILITY

THE WEAKEST COMPONENT AFFECTS THE RELIABILITY OF THE WHOLE SYSTEM

FOR EXPONENTIAL RELIABILITY FUNCTIONS (CONNECTED IN SERIES FROM A RBS POINT OF VIEW)

$$R(t) = e^{-(\lambda_1 + \lambda_2 + \lambda_3) t} \rightarrow \text{THE SYSTEM FAILURE RATE IS THE SUM OF THE COMPONENTS FAILURE RATES}$$

$$MTTF = \frac{1}{\lambda} = \frac{1}{\sum \lambda_i}$$

! IN A SERIES CONFIGURATION THE FAILURE RATE INCREASES AS THE NUMBER OF COMPONENTS INCREASES

! MAKE WORSE THE RELIABILITY  
RULE: MINIMIZE THE # OF ELEMENTS ←

PARTS COUNT METHOD → USEFUL FOR SYSTEMS WITH A SERIES CONFIGURATION THAT HAVE

- A VERY LARGE NUMBER COMPONENTS
- COMPONENTS WITH A CONSTANT FAILURE RATE
- COMPONENTS THAT CAN BE GROUPED INTO FEW FAMILIES

↓  
ELECTRONIC BOARD (DIP BOARD, PCB BOARD)

↓  
IN THE SYSTEM,  $K$  DIFFERENT COMPONENT FAMILIES ARE IDENTIFIED, EACH ONE WITH  $n_i$  COMPONENTS WITH CONSTANT FAILURE RATE  $\lambda_i$

$$\lambda_s = \sum_{i=1}^K n_i \lambda_i$$