



Corso Luigi Einaudi, 55 - Torino

Appunti universitari

Tesi di laurea

Cartoleria e cancelleria

Stampa file e fotocopie

Print on demand

Rilegature

NUMERO: 1540A -

ANNO: 2015

A P P U N T I

STUDENTE: Meli

MATERIA: Meccanica delle Macchine + Eserc. Prof. Pastorelli

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IL NOME DEL PROFESSORE, SERVE SOLO PER IDENTIFICARE IL CORSO.**

ES 1 | 1.15

$a_0 = 6 \text{ m/s}^2$

$g = 9 \text{ m/s}^2$

$\alpha = 15^\circ$

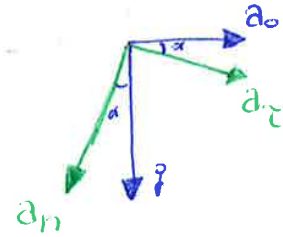
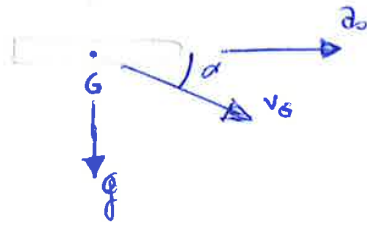
$v_0 = 15000 \text{ km/h} = 4166.7 \text{ m/s}$

$\rho = ?$

$a_r = ?$

$\omega = ?$

$\vec{a} = ?$



$$\begin{cases} \vec{a} = a_n \cos \alpha + a_t \sin \alpha \\ \vec{a}_0 = -a_n \sin \alpha + a_t \cos \alpha \end{cases}$$

$$g = a_n \cos \alpha + a_t \sin \alpha - a_n \frac{\sin \alpha}{\cos \alpha} \Rightarrow a_n = \frac{g \cos \alpha}{\cos \alpha - \tan \alpha}$$

$$a_t = \frac{a_0}{\cos \alpha} - a_n \tan \alpha = 4 \text{ m/s}^2$$

$$\begin{cases} g = a_n \cos \alpha + a_t \sin \alpha \\ a_0 = -a_n \sin \alpha + a_t \cos \alpha \end{cases} \Rightarrow \begin{cases} g = a_n \cos \alpha + (a_0 + a_n \sin \alpha) \tan \alpha \\ a_t = \frac{a_0 + a_n \sin \alpha}{\cos \alpha} \end{cases}$$

$$a_n (\cos \alpha + \sin \alpha \tan \alpha) = g - a_0 \tan \alpha \Rightarrow a_n = 7.14$$

$$a_t = 8.12$$

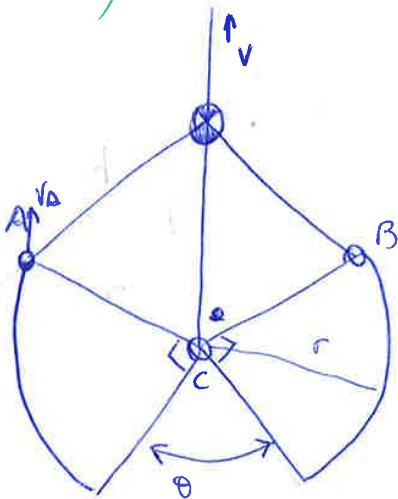
$\vec{a} = \vec{a}_n + \vec{a}_t$

$a_n = v^2 / \rho \Rightarrow \rho = 2431.53 \text{ km}$

$a_t = \omega \rho \Rightarrow \omega = 3.339 \cdot 10^{-6} \text{ rad/s}$

$\omega = v / \rho = 0.0017 \text{ rad/s}$

ES 2 | 1.27



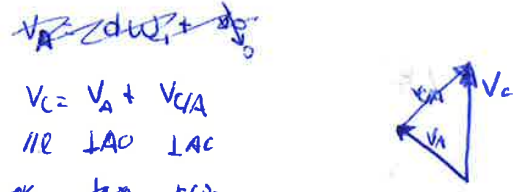
$v_0 = 0.3 \text{ m/s} = v$

$\theta = 45^\circ$

$\omega = ?$

$r = 0.5 \text{ m}$

$AO = BO = d = 0.6 \text{ m}$



$\beta = 69.5^\circ$

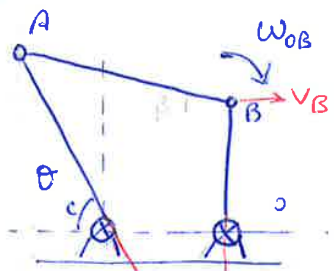
$\frac{AO}{\sin \beta} = \frac{AC}{\sin \alpha} \Rightarrow \sin \alpha = 0.77 \Rightarrow \alpha = 50.35^\circ$

$v_c = v_a \sin \alpha + v_{c/a} \cos \alpha$

$v_c = v_a + \omega r$

$\frac{v_c}{\sin(\alpha + \beta)} = \frac{\omega \cdot r}{\sin(\frac{\pi}{2} - \alpha)} \Rightarrow \omega = 0.43 \text{ rad/s}$

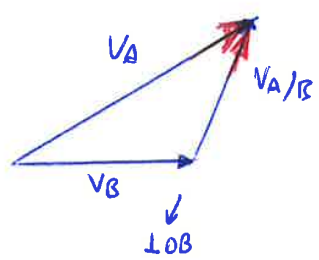
ES 04
1.42



$\omega_{OB} = 0,6 \text{ rad/s}$
 $\tan \theta = 4/3 \Rightarrow \theta = 53,1^\circ$
 $OB = 0,12 \text{ m}$
 $CA = 0,2 \text{ m}$
 $OC = 0,12 \text{ m}$
 $\omega_{AC} = ?$
 $\dot{\omega}_{AC} = ?$

$AB = \sqrt{(AC \sin \theta - OB)^2 + (AC \cos \theta + OC)^2} = 0,243 \text{ m}$
 $\beta = \arcsin \left(\frac{AC \sin \theta - OB}{AB} \right) = 9,47^\circ$

$v_B = \omega_{OB} \cdot OB = 0,072 \text{ m/s}$
 $v_A = v_B + v_{A/B}$
 $v_A = \omega_{AC} \wedge AC$
 $v_A = v_B + v_{A/B}$
 $\perp AC \quad \perp OB \quad \perp AB$
 $? \quad \omega_{OB} \quad ?$



$BD = OB + \frac{OC}{\tan(90-\theta)} = 0,22 \text{ m}$
 $v_B = DB \omega_{AB} \Rightarrow \omega_{AB} = 0,327 \text{ rad/s}$

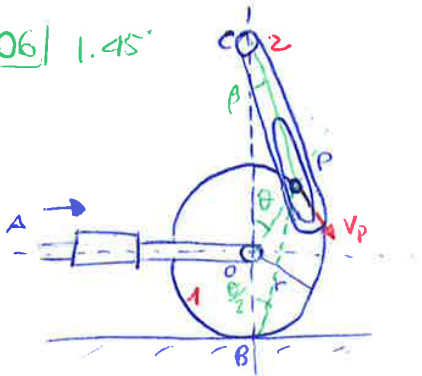
$v_A = v_B + \omega_{AB} \cdot AB$
 $AD = AC + \frac{OC}{\sin(90-\theta)} = 0,4 \text{ m}$
 $v_A = AD \omega_{AB} = 0,1028 \text{ m/s}$
 $\omega_{AC} = v_A / OB = 0,856 \text{ rad/s}$
 $v_A = v_B + \frac{\omega_{AB} \cdot AB}{v_{A/B}} = 0,0508 \text{ m/s}$

$a_{Bn} = v_B^2 / OB = 0,0432$
 $a_{Bt} = \dot{\omega}_{OB} \cdot OB = 0$ perché $\dot{\omega}_{OB} = 0$

$a_A = a_{Bn} + a_{B/A}$
 \downarrow
 $a_n + a_t$
 $\perp BA \quad \perp BA$
 $? \quad ?$
 $v_{A/AC} \quad \omega_{AC} \wedge AC$
 $a_n + a_t$
 $\perp BA \quad \perp BA$
 $? \quad ?$
 $v_{A/AC} \quad \omega_{AC} \wedge AC$



06/ 1.45'



$v = 2 \text{ m/s}$
 $r = 0,1 \text{ m}$
 $OC = 0,2 \text{ m}$
 $\omega_2?$
 $\dot{\omega}_2?$
 $\theta = 30^\circ$

$v = v_0 = \omega_1 r \Rightarrow \omega_1 = 20 \text{ rad/s}$

$v_p = v_0 + v_{p/O}$
 $\perp CP \perp CO \perp OP$
 $?$

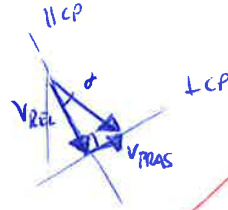


$CP = \sqrt{r^2 + r^2 - 2r^2 \cos \theta} = 0,123 \text{ m}$

$\beta: \frac{r}{\sin \beta} = \frac{CP}{\sin \theta} \Rightarrow \beta \sin \theta = 0,406 \Rightarrow \beta = 23,98^\circ$

$BP: 2r \cos \theta/2 = 0,143 \text{ m}$
 $v_p = \omega_1 BP = 3,86 \text{ m/s}$

$v_p = v_{rel} + v_{trase}$
 $\perp BP \parallel CP \perp CP$
 $ok \quad ? \quad \omega_2 CP$

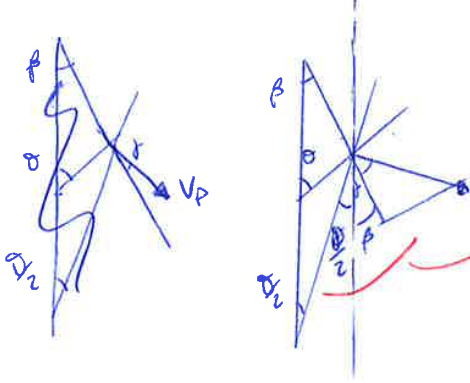


$\delta = 90 - \frac{\theta}{2} - \beta = 54,02^\circ$

$\Rightarrow v_{tr} = v_p \sin \delta = 3 \text{ m/s}$

$\Rightarrow v_{tr} = \omega_2 CP \Rightarrow \omega_2 = 24,4 \text{ rad/s}$

$v_{rel} = v_p \cos \delta = 2,43 \text{ m/s}$

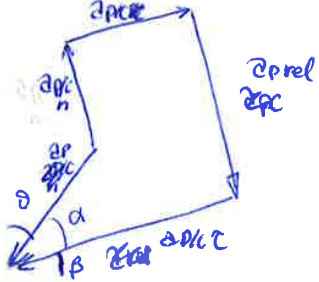
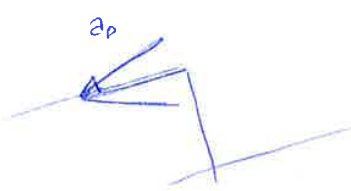


$a_p = a_{rel} + a_{tr} + a_{pc}$

$a_p = a_{p/O} + a_{p/O} + a_{p/O}$
 $\omega_1 OP \quad \omega_1 = 0$

$\perp CP$
 $?$

$a_{p/C} + a_{p/C} + 2\omega_2 v_{rel}$
 $\parallel \omega_2 CP \quad \perp CP$
 $\omega_2 CP \quad \omega_2 CP$



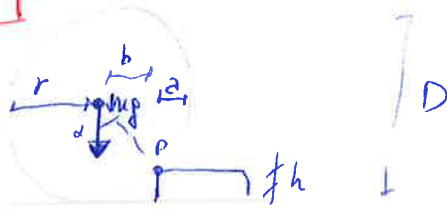
$\alpha = 90 - \beta - \delta = 36,02^\circ$

$a_{p/C} = a_p \cos \alpha + a_{pc} = 150,9$

$\dot{\omega}_2 = \frac{a_{p/C}}{PC} = 1227,1 \text{ rad/s}$

ES 0,9 (2.31) |

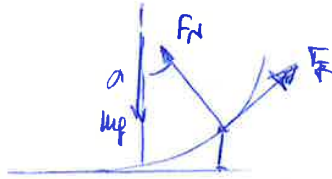
$D = 0,9 \text{ m}$
 $\mu = 30 \text{ kg}$
 $C = ?$
 $h = 0,09 \text{ m}$
 $f_a = ?$



$P = 222 \text{ (} \frac{0,27}{0,31} \text{; } 0,09 \text{)}$

$\sum \tau: C - \mu p b = 0$
 $\Rightarrow C = 64,07 \text{ Nm}$
 $C = 79,38 \text{ Nm}$

$(r-h)^2 + (r-a)^2 = r^2$
 $\Rightarrow 0,1296 + r^2 + a^2 - 2ra = r^2$
 $a^2 - 2ra + 0,1296 = 0$



$\frac{2r \pm \sqrt{4a^2 - 4 \cdot 0,1296}}{2}$
 $\frac{0,9 \pm 0,54}{2} \Rightarrow a = 0,18 \text{ m}$
 $b = 0,27 \text{ m}$

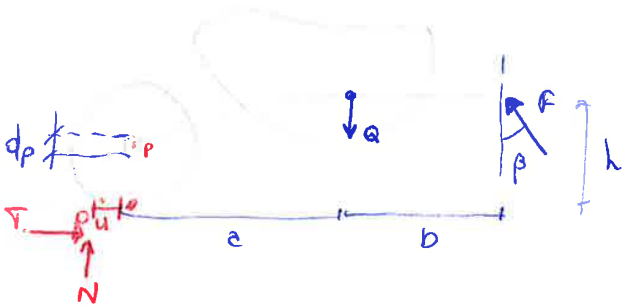
$\alpha = \arctan\left(\frac{b}{r-h}\right) = 36,87^\circ$

$F_N = \mu p \cos \alpha$
 $F_T = \mu p \sin \alpha$
 $F_T = F_N f$

$\mu p \sin \alpha = \mu p \cos \alpha \cdot f \Rightarrow f = \tan \alpha = 0,75$

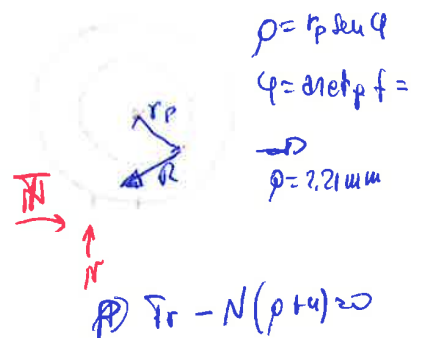
Ok!

ES 10) (2.32)

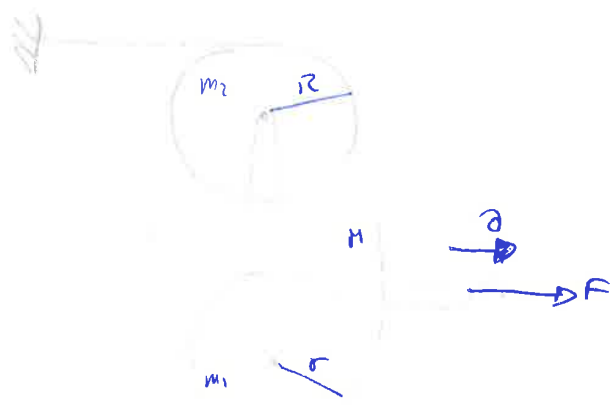


$Q = 900 \text{ N}$
 $a = 0,6 \text{ m}$
 $b = 0,5 \text{ m}$
 $h = 0,8 \text{ m}$
 $D = 0,4 \text{ m}$
 $u = 0,01 \text{ m}$
 $d_p = 0,025 \text{ m } 25 \text{ mm} \Rightarrow r_p = 0,0125$
 $f_p = 0,18$
 $F = ? \quad v = \cos \beta$
 $\beta = ?$

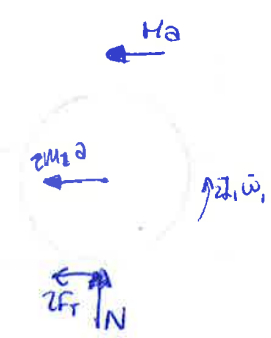
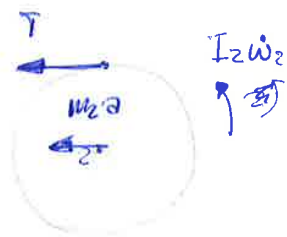
$N - Q = F \cos \beta \Rightarrow$
 $\rightarrow F \sin \beta = T$
 $\sum \tau: Q(a+u) + F \cos \beta (a+b) - F \sin \beta h = 0$
 $\sum \tau: T r - N(p+u) = 0 \Rightarrow T = N \frac{(p+u) r}{r}$
 $Q(a+u) + (N-Q)(a+b) - \frac{N(p+u) r}{r} = 0$
 $N = 424,1 \text{ N}$
 $T = 25,3 \text{ N}$
 $F = 476,6 \text{ N}$
 $\beta = 3,12^\circ$



ES 13 (3.35)



- $R = 0,5m$
- $m_2 = 50kg$
- $\rho_2 = 0,42m$
- $M = 100kg$
- $m_1 = 15kg$
- $\rho_1 = 0,3m$
- $F = 400$
- $r = 0,4m$
- $a = ?$



$$\dot{\omega}_1 = \omega_2 \frac{r}{R}$$

$$\dot{\omega}_2 = a/R$$

$$F - T - (m_2 + M + 2m_1)a = 0 \Rightarrow -2F = 0$$

$$2) T R = I_2 \omega_2^2$$

$$1) 2F r = 2 \left(\frac{1}{2} m_1 \rho_1^2 \omega_1 \right)$$

$$F - \frac{m_2 \rho_2^2 \omega_2}{R} - (m_2 + M + 2m_1)a - \frac{2m_1 \rho_1 \dot{\omega}_1}{r} = 0$$

$$\Rightarrow a = \frac{F}{k_f \left[\frac{m_2 \rho_2^2}{R} + (m_2 + M + 2m_1) + \frac{2m_1 \rho_1^2}{r^2} \right]} = \frac{400}{252,5} = 1,57 \frac{m}{s^2}$$

ES 14 (3.39)



- $l = 0,3m$
- $m_A = 1,5kg$
- $m_B = 4kg$
- $\rho_B = 0,09m$
- $n_0 = 300 \text{ giri/min}$
- $b = 0,06m$

$$\frac{1}{2} (m_B \rho_B^2) n_0^2 + \frac{1}{2} \left(\frac{1}{2} m_A b^2 \right) n_0^2 + 2m_A \rho_B^2 =$$

$$\frac{1}{2} m_B \rho_B^2 n^2 + \frac{1}{4} m_A (l^2) n^2 =$$

$$\frac{1}{2} \cdot 2 \cdot \frac{1}{2} m_A \left(\frac{l^2}{12} + (\frac{l}{2} + b)^2 \right) =$$

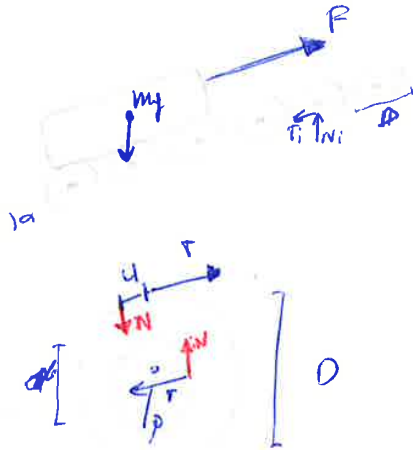
$$\Rightarrow n = 169,5 \text{ giri/min}$$

$$\frac{1}{2} (m_B \rho_B^2) n_0^2 + \frac{1}{4} \cdot 2 \cdot (m_A b^2) n_0^2 + 2m_A \rho_B^2 =$$

$$= \frac{1}{2} m_B \rho_B^2 n^2 + \frac{1}{4} \cdot 2m_A \left(\frac{l^2}{12} + (\frac{l}{2} + b)^2 \right) \Rightarrow$$

Col momento angolare...

Problema 18 (d.9)



$\alpha = 5^\circ$
 $D = 0.3m$
 $d = 0.05m$
 $f = 0.08$
 $u = 1.25 \text{ mm}$
 $\eta = ?$

~~$F - \mu f \sec \alpha - \sum \tau_i = 0$~~
 ~~$\sum N_i - \mu f = 0$~~

$f - \mu f \sec \alpha - \sum \tau_i = 0$
 $\sum N_i - \mu f \cos \alpha = 0$

$\varphi = \arctan(f)$
 $\rho = \frac{d}{2} \sec \varphi$

$\sum \tau_i = N u + N \rho - T \frac{D}{2} \Rightarrow \tau = N \left(\frac{u + \rho}{D/2} \right)$
 $T = N \cdot 0.0025 \cdot 211$

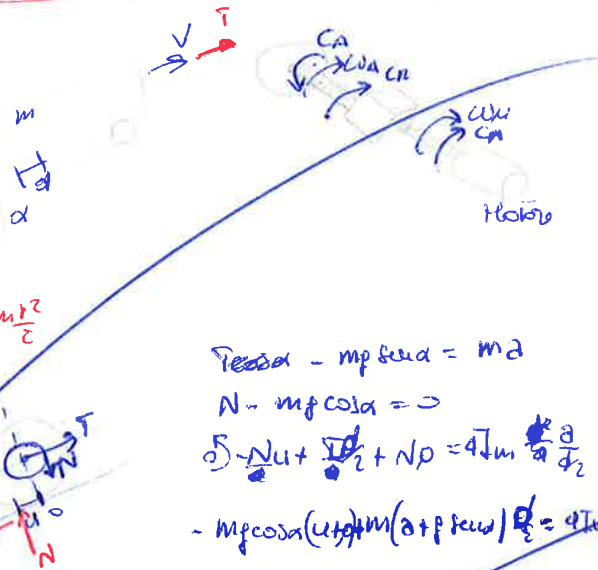
$N = \mu f \cos \alpha \Rightarrow T = m \cdot 0.08 \cdot \cos 5^\circ \cdot 211$

~~$F = m \cdot 0.85 - m \cdot 0.08 \cdot \cos 5^\circ \cdot 211$~~

$F = m \cdot 0.85 - m \cdot 0.2m$

$\eta = \frac{L u \tau}{L \text{svolto}} = \frac{\mu f \sec \alpha \cdot \rho}{F \cdot u} = \frac{0.85 \cdot 211}{1.06} = 80.10\%$

Es 19 (d.13)



$I_m = \frac{m r^2}{2}$

$T \sec \alpha - m g \sec \alpha = m a$

$N = m g \cos \alpha = 0$

$\sum N u + \sum \tau + N \rho = 4 I_m \frac{a}{D/2}$

$- m g \cos \alpha (u + \rho) + m (a + f \sec \alpha) \frac{D}{2} = 4 I_m \frac{a}{D/2} \Rightarrow$

$\Rightarrow m g \cos \alpha (u + \rho) + \mu f \sec \alpha \frac{D}{2} = (4 \frac{I_m}{D/2} + m) a \Rightarrow a = 0.222 \text{ m/s}^2 \Rightarrow T = 5096.7 \text{ N}$

$m = 2000 \text{ kg}$

$d = 0.7 \text{ m}$

$\alpha = 10^\circ$

~~$u = 900 \text{ mm/s}$~~ $u = 900 \text{ mm/s}$

$D = 1.28 \text{ m}$

$u = 15 \text{ mm/s}$

$I_A = 25 \text{ kg m}^2$

$I_m = 0.15 \text{ kg m}^2$

$\tau = \frac{W_a}{W_m} = \frac{1}{36} \quad \eta = 0.75$

1) $V = 18 \text{ km/h}$ P?

2) $W_H = ?$

$T_0 = ? \quad C_0 = 2C_r$

1.406

7458.6W

$P_A = \frac{1000}{22} V = 16.51 \text{ kW} \quad 25.483 \text{ kW}$

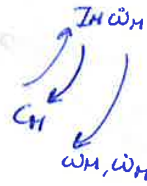
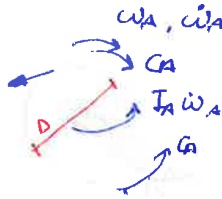
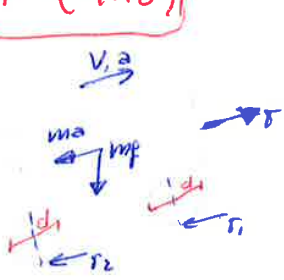
$W_A = V \frac{D}{2} \Rightarrow C_r = \frac{P_A}{W_A} = 326.88 \text{ N/m}$

$W_m = \frac{W_a}{\tau} = 180 \text{ rad/s}$

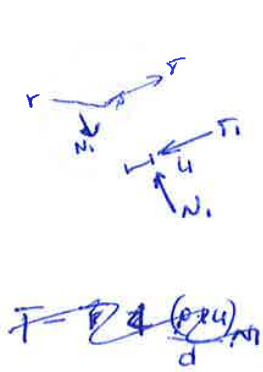
$\frac{P_A}{P_H} = \eta \Rightarrow P_H = \frac{P_A}{\eta} = 33.34 \text{ kW} \Rightarrow C_H = 188.76 \text{ N/m}$

$P_A = \eta P_H \Rightarrow T_0 V = \eta 24 \text{ kW} \Rightarrow T_0 = 10198.52 \text{ N}$

Es 19 (4.13)



- $m = 2400 \text{ kg}$ $d = 1.28 \text{ m}$
- $I_A = 25 \text{ kgm}^2$
- $I_H = 0.15 \text{ kgm}^2$
- $\eta = \frac{w_A}{w_H} = \frac{1}{36}$ $\eta = 0.275$
- $d = 0.7 \text{ m}$
- $\rho = 3 \text{ mm}$
- $u = 15 \text{ mm}$
- $P_H = ?$ $\alpha = 0$ $v = 18 \text{ km/h}$
- $w_H = ?$
- $T_0 \setminus C_0 = 2C_H, v = 0$



$$\begin{cases} T_1 = \frac{2(\rho+u)N_1}{d} \\ T_2 = \frac{2(\rho+u)N_2}{d} \\ T - T_1 - T_2 - mp \sin \alpha = m a \Rightarrow T = mp \left[\sin \alpha + \frac{2(\rho+u) \cos \alpha}{d} \right] + m a \\ N_1 + N_2 - mp \cos \alpha = 0 \end{cases}$$

$$C_A = T_A \frac{D}{2} + I_A \dot{\omega}_A$$

$$\dot{\omega}_A = \frac{v}{r}$$

$$C_H = \frac{C_A}{\eta} + 2 I_H \dot{\omega}_H$$

$$P_A = P_H \eta$$

$$C_H = \frac{C_A}{\eta} + 2 I_H \frac{v}{r}$$

$$P_A = \eta P_H$$

~~$$C_A \omega_A = \eta \left[C_H \frac{\omega_A}{\eta} \right] \Rightarrow C_H = C_A \frac{\omega_A}{\eta}$$~~

$$C_H = \frac{C_A}{\eta}$$

$$\dot{\omega}_H = \frac{\dot{\omega}_A}{\eta}$$

$$C_A \omega_A = \eta \left[C_H \frac{\omega_A}{\eta} + 2 I_H \frac{\omega_A}{\eta} \right] \Rightarrow \frac{C_A \tau}{\eta} + I_H \frac{\dot{\omega}_A}{\eta} = C_H \Rightarrow \frac{C_A \tau}{\eta} + I_H \frac{\dot{\omega}_A}{\eta} = C_H$$

$$F_A \Rightarrow \left(T_A \frac{D}{2} + I_A \dot{\omega}_A \right) \frac{\tau}{\eta} + I_H \frac{\dot{\omega}_A}{\eta} = C_H \quad \text{ma } \dot{\omega}_H = 0 \text{ se } v = 5 \text{ m/s}$$

$$\Rightarrow C_H = mp \left[\sin \alpha + \frac{2(\rho+u) \cos \alpha}{d} \right] \frac{D}{2} \cdot \frac{\tau}{\eta} = 125.1 \text{ Nm}$$

$$\omega_H = \frac{\omega_A}{\eta} \quad \omega_A = v/D_2 \Rightarrow \omega_H = 281.75 \text{ rad/s}$$

$$C_0 = \left(T_A \frac{D}{2} + I_A \dot{\omega}_A \right) \frac{\tau}{\eta} + I_H \frac{\dot{\omega}_A}{\eta} = mp \left[\sin \alpha + \frac{2(\rho+u) \cos \alpha}{d} \right] \frac{D}{2} \frac{\tau}{\eta} + I_H \frac{\dot{\omega}_A}{\eta} + \frac{2 I_H \dot{\omega}_A}{\eta}$$

$$\downarrow 2C_H$$

$$(m a + I_A \dot{\omega}_A) \frac{\tau}{\eta}$$

$$\Rightarrow \omega_A = 0.88 \text{ rad/s}^2 \Rightarrow a = 0.563 \text{ m/s}^2 \Rightarrow T_0 = 6626.7 \text{ N}$$

$$2C_0 = \frac{\tau}{\eta} \left\{ I_A \dot{\omega}_A + \frac{D}{2} \left(mp \left[\sin \alpha + \frac{2(\rho+u) \cos \alpha}{d} \right] + m a \right) \right\} + I_H \frac{\dot{\omega}_A}{\eta}$$

$$2 \cdot 6626.7 = (261 + 5.4 \dot{\omega}_A + 0.29 \dot{\omega}_A + \frac{90}{2000} \dot{\omega}_A) \Rightarrow \dot{\omega}_A = 1281.29 \Rightarrow a = 203 \text{ m/s}^2 \Rightarrow T = 10149 \text{ N}$$

ES 1.11

$$a = 5 - 0,2v^2$$

$$t_f = ?$$

$$v = 7,5 \text{ m/s}$$

$$S_f =$$

$$v_0 = 0$$

$$a = (5 - 1,25) = 3,75 \text{ m/s}^2$$

$$v = v_0 + at \rightarrow t = 0,67 \text{ s}$$

$$S_f = \frac{1}{2} a t_f^2 = 0,833 \text{ m}$$

$$a = \frac{dv}{dt} \rightarrow dt = \frac{dv}{a(v)}$$

$$t_f = \int_0^{v_f} \frac{dv}{5 - 0,2v^2} =$$

$$S_f = \frac{1}{2} a t_f^2 = 0,833 \text{ m}$$

$$a_0 = 5 \text{ m/s}^2 \quad 0,2 v^2 = c$$

$$t_f = \int_0^{v_f} \frac{dv}{a_0 - cv^2} = \int_0^{v_f} \frac{dv}{\frac{a_0}{c} - v^2}$$

$$\sqrt{\frac{a_0}{c}} = v$$

1.2

$$a = 4 - 0,5t$$

$$S = 100 \text{ m}$$

$$t = ?$$

$$v_0 = 0$$

$$t = \frac{-a \pm \sqrt{a^2 - 4bc}}{2a} \quad \text{considero l'istante in cui } a=0 \rightarrow t^* = 8 \text{ s}$$

$$v^* = \int_0^{t^*} a(t) dt = \int_0^8 (4 - 0,5t) dt = \left(4t - 0,5 \frac{t^2}{2} \right)_0^8 = 32 - 16 = 16 \text{ m/s}$$

$$S^* = \int_0^{t^*} v(t) dt = \int_0^8 \left(4t - \frac{t^2}{4} \right) dt = \left(2t^2 - \frac{t^3}{12} \right)_0^8 =$$

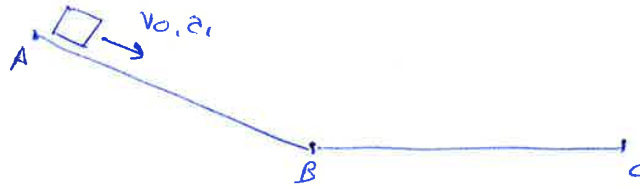
$$= 128 - \frac{128}{3} = \frac{256}{3} = 85,33 \text{ m}$$

$$S - S^* = 14,67 \text{ m} = \Delta S \rightarrow \Delta t = v^* t \rightarrow t = 0,916 \text{ s}$$

$$\rightarrow t_{\text{tot}} = t^* + t = 8,916 \text{ s}$$

1.7

- $v_0 = 1.2 \text{ m/s}$
- $a_1 = 3 \text{ m/s}^2$
- $a_2 = ?$
- $t_2 = ?$
- $s_1 = 3 \text{ m}$
- $s_2 = 3.6 \text{ m}$



AB:
$$\begin{cases} s_1 = \frac{1}{2} a_1 t^2 + v_0 t \\ v_1 = v_0 + a_1 t \end{cases} \Rightarrow 3 = 1.5 t^2 + 1.2 t \Rightarrow 1.2 t + 1.5 t^2 - 3 = 0$$

$$4.107 \text{ m/s} = v_1 \leftarrow \frac{-1.2 \pm 4.4}{3} = 1.069 \text{ s}$$

BC:
$$\begin{cases} s_2 = \frac{1}{2} a_2 t_2^2 + v_1 t_2 \\ v_2 = v_1 + a_2 t_2 \rightarrow v_0 - \frac{v_1}{a_2} = t_2^2 \end{cases}$$

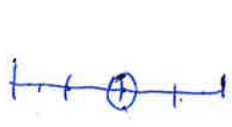
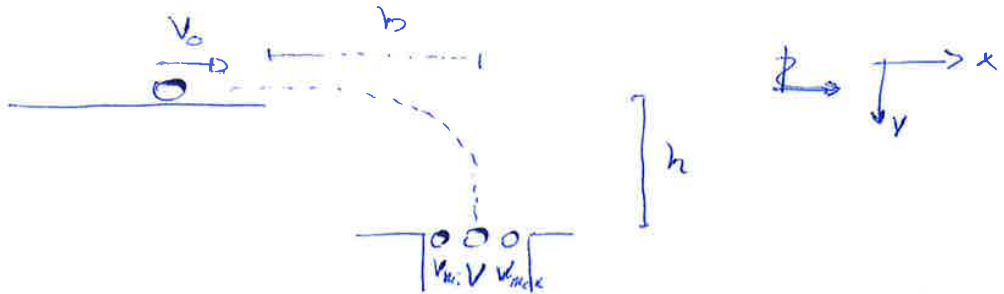
$$s_2 = \frac{1}{2} a_2 \left(\frac{v_1}{a_2} \right)^2 + v_1 \left(-\frac{v_1}{a_2} \right) \Rightarrow s_2 = \frac{1}{2} \frac{v_1^2}{a_2} - \frac{v_1^2}{a_2} \Rightarrow$$

$$\rightarrow s_2 = -\frac{1}{2} \frac{v_1^2}{a_2} \rightarrow a_2 = -\frac{1}{2} \frac{v_1^2}{s_2} = -2.7 \text{ m/s}^2$$

$$t_2 = 1.632 \text{ s}$$

1.12

- $d = 0.02 \text{ m}$
- $D = 0.08 \text{ m}$
- $v_{\text{min}} = ?$
- $v_{\text{max}} = ?$
- $h = 0.09 \text{ m}$
- $b = 0.12 \text{ m}$



$$\rightarrow D: \begin{cases} x = v_{0x} t \\ y = v_{0y} t + \frac{1}{2} g t^2 \end{cases}$$

$$v_{0y} = \frac{v_{0y}}{v_{0x}} = \tan(\alpha)$$

$$\frac{h}{b} = \tan(\alpha) \rightarrow \tan(\alpha) = 0.75$$

$$\begin{cases} x = v_{0x} t \\ y = v_{0x} \tan(\alpha) t + \frac{1}{2} g t^2 \end{cases}$$

Se $x = \left(\frac{D}{2} - \frac{3d}{2} \right) \rightarrow \frac{D}{2} - \frac{3d}{2} = v_{0x} t$

$$h = v_{0x} \tan(\alpha) t + \frac{1}{2} g t^2$$

$$v_{0x} = \frac{b \tan(\alpha)}{t}$$

$$h = \frac{b \tan(\alpha)}{t} \tan(\alpha) t + \frac{1}{2} g t^2 \rightarrow h = \frac{b \tan^2(\alpha)}{t} + \frac{1}{2} g t^2$$

$$t = 0.129 \text{ s} \rightarrow v_{0x} = 0.978 \text{ m/s}$$

$$v = 0.98 \text{ m/s}$$

Se $x = \frac{D}{2} + \frac{3d}{2} \rightarrow c_2 = v_{0x} t$

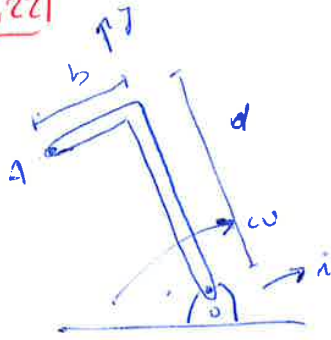
$$h = v_{0x} \tan(\alpha) t + \frac{1}{2} g t^2 \rightarrow$$

$$\rightarrow h = \frac{c_2}{t} \tan(\alpha) t + \frac{1}{2} g t^2 \rightarrow t = 0.0875 \text{ s}$$

$$\rightarrow v_{0x} = 0.8 \text{ m/s} \rightarrow v = 1 \text{ m/s}$$

CINEMATICA CORPI RIGIDI

1.22



~~$\omega = 2 \text{ rad/s}$~~

$\dot{\omega} = 2 \text{ rad/s}^2$

$v_A = ?$ | $\omega = 3 \text{ rad/s}$
 $a_A = ?$

$b = 0,3 \text{ m}$

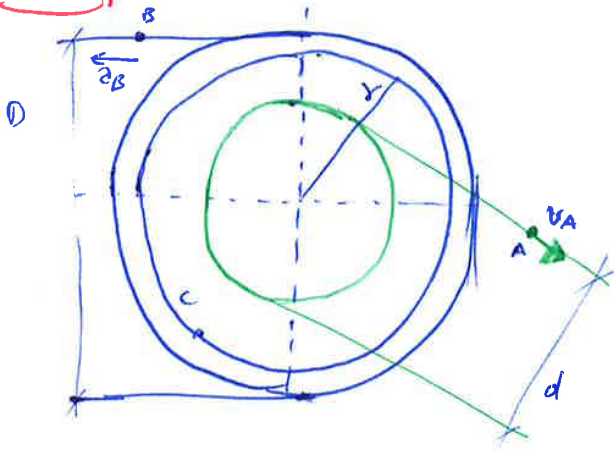
$d = 0,4 \text{ m}$

$OA = d\mathbf{j} - b\mathbf{i} + d\mathbf{j}$

$v_A = \omega \times OA = -0,9\mathbf{i} + 1,2\mathbf{j} \text{ rad/s}$

$a_A = \dot{\omega} \times OA + \omega^2(OA) = -0,6\mathbf{i} + 0,8\mathbf{j} + 0,27\mathbf{i} + 3,6\mathbf{j}$
 $= -1,9\mathbf{i} - 4,2\mathbf{j} \text{ rad/s}^2$

1.24



$v_A = 24 \text{ m/s}$

$a_B = 35 \text{ m/s}^2$

$a_C = ?$

$D = 0,2 \text{ m}$

$d = 0,15 \text{ m}$

$r = 0,36 \text{ m}$

~~c) $a_C = a_B \cdot r = 12,6 \text{ m/s}^2$~~

~~$a_n = \frac{v_A^2}{r} =$~~

→ c) $a_C = a_B \cdot r = 31,5 \text{ m/s}^2$

$a_n = \omega_A^2 \cdot r = 256 \text{ m/s}^2$

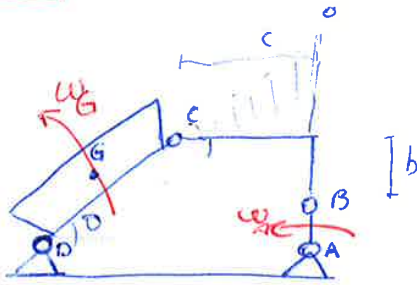
$a_B = a_B / D/2 = 87,5 \text{ rad/s}^2$

$\omega_A = v_A / d/2 = 26,67 \text{ rad/s}$

~~a_C~~

1.36

CINETICI SUI ARTICOLATI

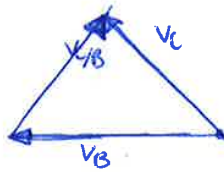


$DC = d = 0,36 \text{ m}$
 $c = 0,2 \text{ m}$
 $b = 0,1 \text{ m}$
 $a = AB = 0,8 \text{ m}$
 $\omega_A = 120 \text{ rpm/min}$
 $\omega_B = ?$

$V_B = V_A + V_{B/A} = 0 + \frac{2\pi \cdot 120}{60} \cdot a = 1 \text{ rad/s}$

$CB = \sqrt{c^2 + b^2} = 0,26 \text{ m}$

$V_C = V_B + V_{C/B}$
 $\perp CD \quad \perp AB \quad \perp CB$
 $\omega_B \cdot d \quad \omega_A \cdot a \quad ? \cdot CB$



$\omega_A \cdot AB = \omega_B \cdot CB$
 $\omega_B = \frac{\omega_A \cdot AB}{CB} = 3,25 \text{ rad/s}$
 $V_C = \omega_B \cdot CB = \frac{\omega_A \cdot AB \cdot CB}{CB} = 2,57 \text{ rad/s}$

$\theta = \arcsin \frac{a+b}{d} = 30^\circ$

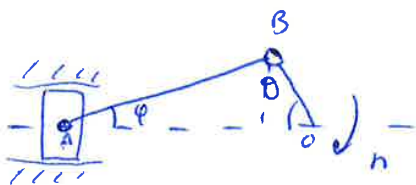
$OC = \frac{c}{\cos \theta} = 0,277 \text{ m}$

$V_C : OC = \omega_B : OB \rightarrow V_C = \frac{\omega_B \cdot OC}{OB} = 1,16 \text{ m/s}$

$OB = b + \tan \theta \cdot c = 0,238 \text{ m}$

$\Rightarrow \omega_B = 3,22 \text{ rad/s}$

1.37



$AB = L = 0,35 \text{ m}$
 $CB = r = 0,125 \text{ m}$
 $\omega = 157,08 \text{ rad/s} \quad \omega_{OB} = 157,08 \text{ rad/s}$

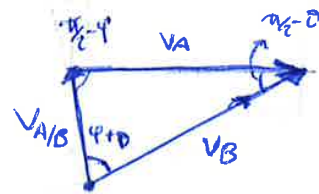
$\theta = 60^\circ$

$V_A = ?$
 $a_A = ?$
 $\omega_{AB} = ?$
 $\alpha_{AB} = ?$

$L \sin \varphi = r \sin \theta \rightarrow \varphi = 18,02^\circ$

$V_B = V_A + \omega_{OB} \cdot r = 19,6 \text{ m/s}$

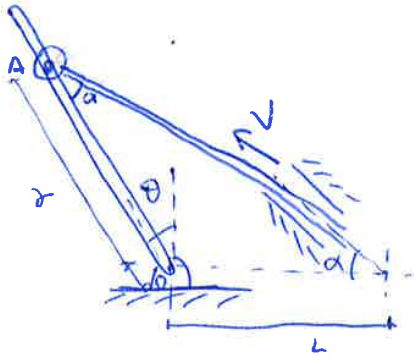
$V_A = V_B + V_{A/B}$
 $\perp AO \quad \perp AB$
 $\perp OB \quad \omega_{B/A} \cdot AB$
 $\omega_{OB} \cdot r$



$29,4 \text{ rad/s} = \omega_{BA} \leftarrow V_{B/A} = 10,3 \frac{\text{m}}{\text{s}} \leftarrow \frac{V_{B/A}}{\sin(\frac{\pi}{2} - \theta)} = \frac{V_B}{\sin(\frac{\pi}{2} - \varphi)} = \frac{V_A}{\sin(\varphi + \theta)} \rightarrow \omega_{BA} = 20,17 \text{ rad/s}$

$\omega_{BA} = \frac{V_B - V_A}{AB} = -7,77 \text{ rad/s}$

1.44



$\alpha = 30$
 $V = 4 \text{ m/s} = \text{cost}$
 $\dot{r}?, \ddot{r}?$
 $\ddot{\theta}?, \theta = 30'$
 $L = 0,3 \text{ m}$

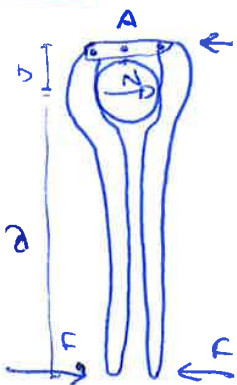
~~$V_A = V_{\text{rad}} + V_t$~~
 ~~$V_{\text{rad}} = V \cdot \cos \alpha = \dots$~~
 ~~$V_t = V \cdot \sin \alpha$~~

$V_A = V_r + V_t$
 $V_r = V \cos \alpha = 3,464 \text{ m/s}$
 $V_t = V \sin \alpha = 2 \text{ m/s} \rightarrow V_t = \omega r \rightarrow \omega = 6,67 \text{ rad/s}$

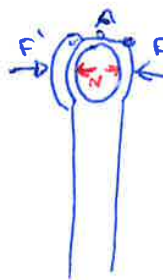
~~$a_A = 0 = a_r + a_t + a_c$~~
 $a_A = 0 = \underbrace{\omega^2 r}_{a_r} + \underbrace{\dot{\omega} r}_{a_t} + \underbrace{\omega \wedge \omega r}_{a_c} - \omega^2 r$
 $\Rightarrow \dot{\omega} r = 2 \omega r$
 $\Rightarrow \dot{\omega} = \frac{2 \omega r}{r} = 13,34 \text{ rad/s}^2$
 $a_n = \omega^2 r = 13,3 \text{ m/s}^2$
 ~~$\ddot{r} = 2 \omega^2 r$~~

EQUILIBRIO STATICO DELLE FORZE.

2.1

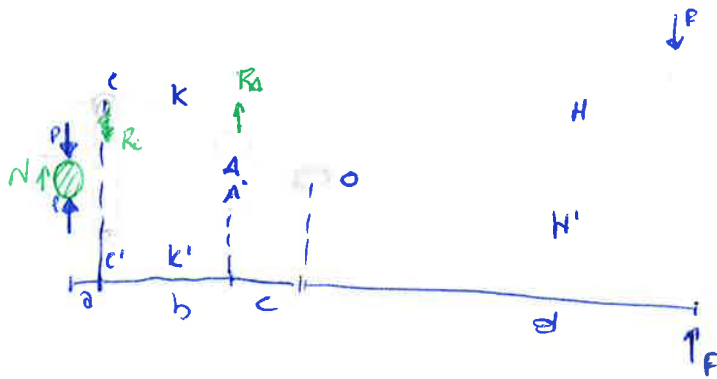


$F = 20 \text{ N}$
 $a = 0,125 \text{ m}$
 $b = 0,02 \text{ m}$
 $N = ?$
 $R_A = ?$



$\sum F_x = 0 \rightarrow N - F - F = 0 \rightarrow N = 2F = 40 \text{ N}$
 ~~$R_A = ?$~~
 $R_A + F - N = 0 \rightarrow R_A = 12 \text{ N}$

2.20



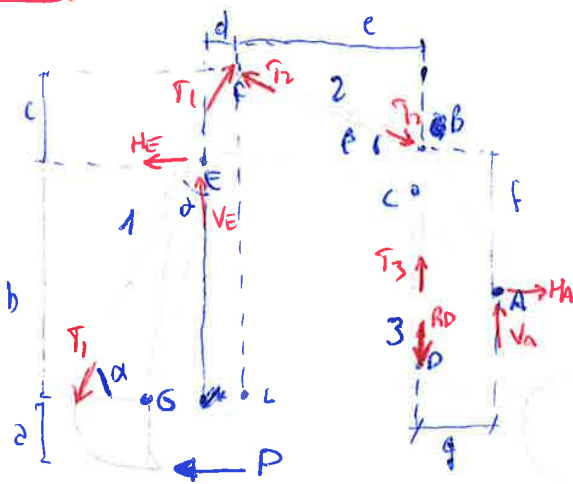
$a = 0.02m$
 $b = 0.06m$
 $c = 0.03m$
 $d = 0.18m$
 $P = ?$
 $F = 150N$

$N = P/2$
 $N \cdot a = R \cdot b$
 $R = ?$

$P \cdot a = R \cdot b \rightarrow P = \frac{R \cdot b}{a} = 2700N$

$F \cdot d = R \cdot c \rightarrow R = \frac{F \cdot d}{c}$

2.21



$P = 10kN$ $b = 2.4m$ $d = 0.3m$
 $a = 0.9m$ $c = 1.2m$ $e = 2.1m$
 $f = 1.5m$ $\varphi = 45^\circ$ $T_1? T_2? T_3?$
 $R_A? R_E?$

$\alpha = \arctan \frac{c+db}{a+\frac{c}{\varphi}(b+c)}$

$\beta = \arctan \frac{c}{e} = 29.74^\circ$

$T_1 \cos \alpha = P \rightarrow T_1 = \frac{P}{\cos \alpha} = 11.18kN$

$\sum M_A: P(a+b+f) + R_D \cdot f = 0 \rightarrow R_D = -20000N$

$\rightarrow H_A - P = 0 \rightarrow H_A = 10kN \rightarrow R_A = 22.36kN$

$\uparrow V_A + R_D = 0 \rightarrow V_A = 20kN$

$T_3 - R_D = 0 \rightarrow T_3 = 20000N$

$\sum T_1 (\cos \alpha + \sin \alpha)$

$\sum T_1 \cos \alpha + T_1 \sin \alpha = T_2 \cos \beta - T_2 \sin \beta = 0$

$T_1 (\cos \alpha + \sin \alpha) = T_2 (\cos \beta - \sin \beta) \rightarrow T_2 = \dots$

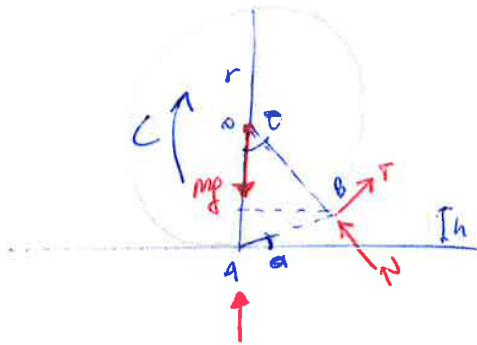
$\sum T_2 (d \cos \beta + c \sin \beta) - P(a+b) = 0$
 $\rightarrow T_2 = 27713N$

$V_E = F_2 \sin \beta = 13747N$

$H_E = P + T_1 \cos \beta = 34063N$

$\rightarrow R_E = 36732N$

2.311



$r = 0,45 \text{ m}$ $C?$

$m = 30 \text{ kg}$

$h = 0,09 \text{ m}$

frin / no slittamento?

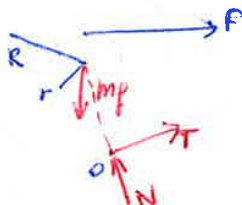
~~$AB \sin \alpha = AB \cos \alpha$~~

$D = 2r \cos\left(\frac{r-h}{r}\right) \Rightarrow \theta = 36,87$

$\int m g (\sin \theta) \cdot r = C = 79,38 \text{ Nm}$

$\int m g \cos \theta - T = 0$
 $\int m g \cos \theta - N = 0$
 $\Rightarrow f N = T \Rightarrow f = \frac{\sin \theta}{\cos \theta} = 0,75$

2.321



1a

$R = 0,750 \text{ m}$

$r = 0,45 \text{ m}$

$m = 200 \text{ kg}$

$\alpha = 15^\circ$

$f = ?$ $f_a = 0,4$

$T = ?$

$\rightarrow F \cos \alpha - m g \sin \alpha + F_f = 0$
 $\uparrow N - m g \cos \alpha - F \sin \alpha = 0 \rightarrow N = m g \cos \alpha + F \sin \alpha \rightarrow F_f = f(m g \cos \alpha + F \sin \alpha)$
 $\Rightarrow F \cos \alpha - m g \sin \alpha + f(m g \cos \alpha + F \sin \alpha) = 0$
 $F(\cos \alpha + f \sin \alpha) = m g(\sin \alpha - f \cos \alpha) \rightarrow F = 1182,1 \text{ N}$

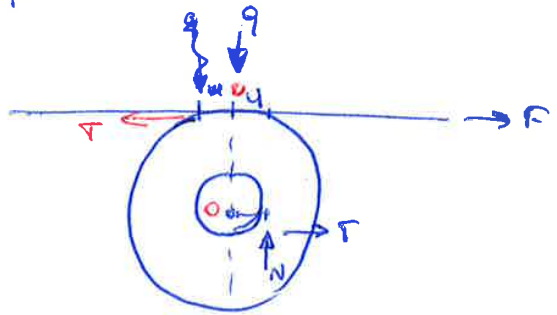
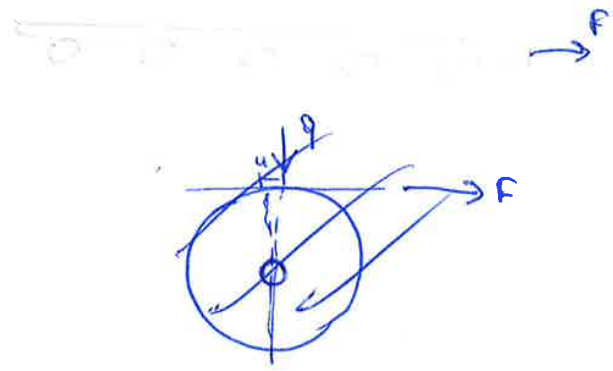
$\rightarrow F = 324,2 \text{ N} \rightarrow F_f = 124,8 \text{ N}$

$\Rightarrow N = 1978,3 \text{ N}$

$\Rightarrow T = 194 \text{ N} < f N$

2.36

- $l = 90 \text{ m}$
- $d = 0,12 \text{ m}$
- $d_p = 0,03 \text{ m}$
- $f_p = 0,035$
- $q_m = 20 \text{ kg/m}$
- $u = 0,0004 \text{ m}$
- $F = ?$

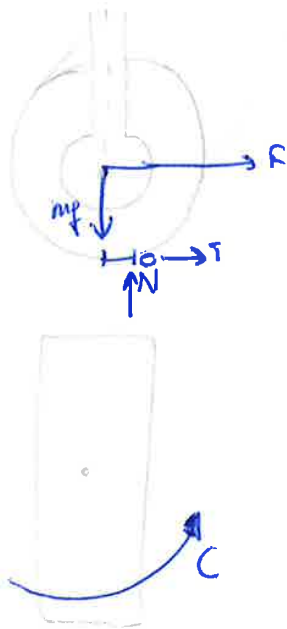


$F =$
 $R = T = 0$
 $N - q l = 0 \rightarrow N = 17640 \text{ N}$
 $\sum \frac{F d}{2} = (T u + q) \cdot l \rightarrow F = 155,46 \text{ N}$
 ~~$F = 155,46 \text{ N}$~~
 $N f_p = T$
 $\sum \frac{F d}{2} - q l (u + p) = 0 \rightarrow F = 271,86 \text{ N}$

$\rho = \frac{d p}{2} \sin \varphi$
 $\varphi = \arctan(f_p)$
 $\Rightarrow \rho = 0,0005247 \text{ m}$

2.38

- $L = 2,5 \text{ m}$
- $d = 1,5 \text{ m}$
- $m = 8000 \text{ kg}$
- $u = 0,02 \text{ m}$
- $f = 0,4$
- $F = ? \quad \omega = 0$
- $C = ?$



$F_A = \frac{f m p}{2}$
 $C = F_A \cdot \frac{L}{2} = 19612 \text{ Nm}$

$\sum \frac{F d}{2} - N u = 0 \rightarrow F = 2090,69 \text{ N}$

~~$F = T = 0$~~
 $N - m f = 0$
 ~~$f A = T$~~
 ~~$\frac{f N}{2} = T$~~
 $f N = T$
 ~~$F = T$~~
 $N = u l p$
 $\frac{d M}{d x} = \frac{f N}{u L} \cdot \frac{L}{2} dx = \dots$
 $\frac{d^2 M}{d x^2} = \frac{N}{u L} \cdot \frac{L^3}{8 \cdot 4 \cdot 3} = 5,131 \cdot 10^6 \text{ Nm}$

3.4

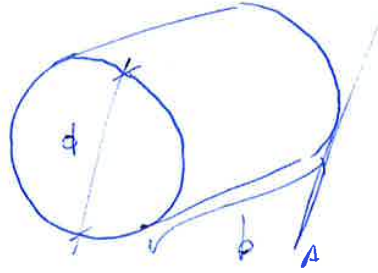
3.1

$\rho = 2750 \text{ kg/m}^3$

$d = 0,2 \text{ m}$

$b = 0,03 \text{ m}$

$I_A = ?$



$M = \rho \cdot \pi \frac{d^2}{4} \cdot b$

$I_C = \left(M \frac{d^2}{4} \right) \cdot \frac{1}{8}$

$I_A = M \rho \frac{\pi d^4 b}{32} + M \frac{d^2}{4}$

$= 0,0129 + 0,0259$
 $= 0,0388 \text{ kgm}^2$

3.4

$m = 75 \text{ kg}$

$M_T = 750 \text{ kg}$

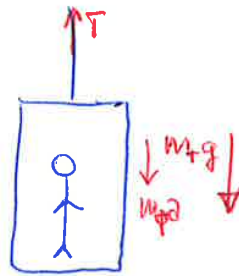
$\Delta t = 35$

$v_0 = 0$

$T_0 = 8300 \text{ N}$

$R = ?$

$V = ?$



$R = T - m_T g = R = 950 \text{ N} \rightarrow a = 1,267 \text{ m/s}^2$

$\Rightarrow V = v_0 + at = 3,8 \text{ m/s}$

$R = m(a + g) = 830 \text{ N}$

3.10

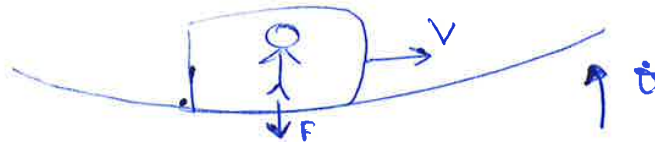
$m = 55 \text{ kg}$

$V = 266,67 \text{ m/s}$

$r = ?$

$\dot{\theta} = ?$

$F = 800 \text{ N}$



$F = m(g + a) \rightarrow a_n = 4,75 \text{ m/s}^2$

$a = \frac{V^2}{r} \rightarrow r = 14985,47 \text{ m} \rightarrow \dot{\theta} = V/r = 0,0178 \text{ rad/s}$

3.13

$m = 150 \text{ kg}$

$\alpha = 30^\circ$

$v_0 = 4 \text{ m/s}$

$\Delta t = 4 \text{ s}$

$\Delta P = 600 \text{ W}$

$P_0 = 0$

P_{cost}

$t_1 = ? \quad v_0 = 0$

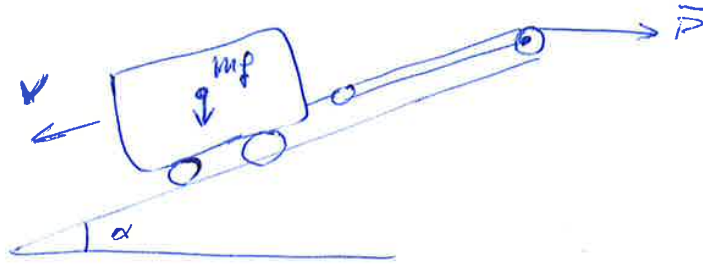
$t_2 = 8 \text{ s} \quad v = ?$

p varia linearmente nel tempo

$P_0 = 0 \quad P_4 = 600$

$P = c \Delta t$

$c = 150 \frac{\text{N}}{\text{s}}$



$$\bar{P} = \frac{1}{\Delta t} \int_0^{\Delta t} P dt = \bar{P} = \frac{1}{\Delta t} \int_0^{\Delta t} c t dt = \frac{1}{4} \cdot c \frac{t^2}{2} = \frac{1}{4} \cdot c \frac{16}{2} = 300 \text{ W}$$

$t_0 = 4 \text{ s}$

~~$\sum \vec{P} - m g \sin \alpha = m a \rightarrow$~~

$\sum P - m g \sin \alpha = m a$

$a = \frac{\sum P}{m} - g \sin \alpha$

$t_2 = 8 \text{ s}$

~~$\sum P - m g \sin \alpha = m a \rightarrow a = 3,14 \text{ m/s}^2$~~

$v = -v_0 + \int_0^t (\frac{\sum P}{m} - g \sin \alpha) dt = v_0 + \frac{c}{2m} t^2 - g \sin \alpha t = 0$

Equation for finding time t

3.17

$m = 0,5 \text{ kg}$

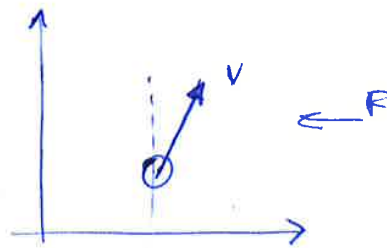
$v = 3 \text{ m/s}$

$\alpha = 30^\circ$

$\theta = 60^\circ$

$F = 0,6 \text{ N}$

$t = ? \quad x = 0$



$\uparrow: v \cos \alpha \quad t = 0 \quad y$

$\rightarrow: v \sin \alpha t - \frac{1}{2} \left(\frac{F}{m}\right) t^2 = 0$

$1,5t - 0,6t^2 = 0$

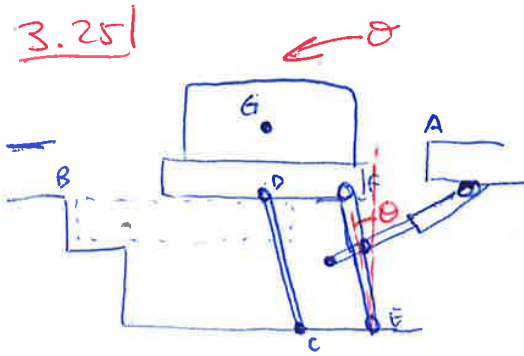
~~$t = 1,58 \text{ s}$~~

$t = 2,5 \text{ s}$

$t \left(v \sin \alpha - \frac{1}{2} \frac{F}{m} t \right) = 0$
 (with $t=0$ and $t=2,5 \text{ s}$)

$t = 2,5 \text{ s} \rightarrow y = 6,495 \text{ m}$
 $x = 0$

3.251



$$\theta(t) = \frac{\pi}{6} \left(1 - \cos \frac{\pi t}{2} \right)$$

$$F_D = ? \text{ in } t=0, \theta=0$$

$$t=1$$

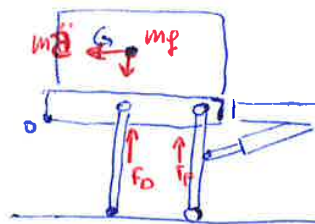
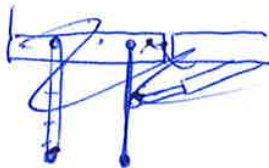
$$m = 200 \text{ kg}$$

$$DC = FE = l = 1.2 \text{ m}$$

$$CE = DF = b = 0.6 \text{ m}$$

$$h = DG = 0.48 \text{ m}$$

1) $t=0, \theta=0 \quad \dot{\theta} = \frac{\pi}{6} (1-1) = 0 \rightarrow \dot{\theta} = 0$



$$\sum F_D b + F_F b - mgb = 0$$

$$\uparrow F_D + F_F = mg$$

$$\rightarrow mgb + F_F b - mgb = 0$$

$$\dot{\theta} = \frac{\pi}{6} \cdot \frac{\pi}{2} \sin \frac{\pi t}{2} = \frac{\pi^2}{12} \sin \frac{\pi t}{2}$$

$$\ddot{\theta} = + \frac{\pi^2}{12} \cdot \frac{\pi}{2} \cos \frac{\pi t}{2} = \frac{\pi^3}{24} \cos \frac{\pi t}{2}$$

$$a = l \ddot{\theta} = 1.55 \text{ m/s}^2$$

$$\sum F_D b + F_F b - mgb + Fh = 0$$

$$\rightarrow ma = F$$

$$\uparrow F_D + F_F = mg$$

$$\Rightarrow mgb + F_F b - mgb + Fh = 0$$

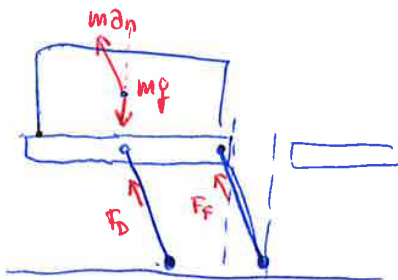
$$\Rightarrow F_F = \frac{Fh}{b} = 247.67 \text{ N}$$

$$\rightarrow F_D = 1712.33 \text{ N}$$

2) $t=1 \rightarrow \theta = \frac{\pi}{6} \left(1 - \cos \frac{\pi}{2} \right) = \frac{\pi}{6}$

$$\dot{\theta} = \frac{\pi^2}{12} \sin \frac{\pi}{2} = \frac{\pi^2}{12} \text{ rad/s} \rightarrow v = 0.99 \text{ m/s}$$

$$\ddot{\theta} = \frac{\pi^3}{24} \cos \left(\frac{\pi}{2} \right) = 0 \rightarrow a_t = 0 \quad a_n = \dot{\theta}^2 l = 1.17 \text{ m/s}^2$$



$$\rightarrow F_D \sin \theta + F_F \sin \theta + m a_n \sin \theta = 0$$

$$\uparrow F_D \cos \theta + F_F \cos \theta = mg + m a_n \cos \theta$$

$$\sum \vec{F} = F_D \cos \theta \cdot b - mgb + m a_n \cos \theta \cdot b - m a_n \sin \theta \cdot b = 0$$

$$F_D \cos \theta - 1960 + 202.64 - 117 = 0 \rightarrow F_D = 2164.0 \text{ N}$$

F_F =

3.49

$r = 0,375 \text{ m}$

$m = 41 \text{ kg}$

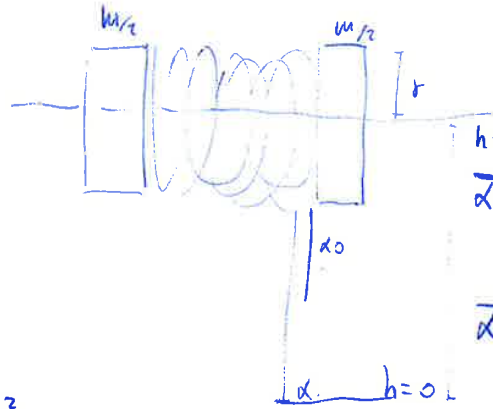
$\rho = 0,3 \text{ m}$

$l = 18 \text{ m}$

$q = 3,08 \text{ kg/m}$

$x_0 = 0,6 \text{ m}$

$x = 6 \text{ m} \rightarrow \omega = ?$



Inizio:

$q \cdot x_0 \cdot \bar{x}_0$ ENI. pot

$h = x + r$
 $\bar{x}_0 = (h - r - x_0) / 2$

fine: ~~$q \cdot x_0 \cdot x_0 \bar{x}$~~ $+ \frac{1}{2} I \omega^2$
 $\bar{x} = (h + r) / 2$

$I_{cm} = m \rho^2 = 3,69 \text{ kg m}^2$

$I_m = q l \cdot r^2 = 7,79 \text{ kg m}^2$

$m' = q l$

$m_{TOT} = m + m'$

$q m_{TOT} h + q (x_0 q) \bar{x}_0 = q (x q) \bar{x} + \frac{1}{2} I \omega^2 \rightarrow \omega = \sqrt{\frac{2 q (x_0 \bar{x}_0 - x \bar{x})}{I}}$

~~$\sqrt{2 q (m_{TOT} h + x_0 q \bar{x}_0 - x q \bar{x})} = \omega \rightarrow \omega = 31,1 \text{ rad/s}$~~

~~$6,4 \cdot 2 \cdot 10^3 - 5,3 \cdot 10^3$~~

$q m_{TOT} h + q m_0 \bar{x}_0 = q m_x \bar{x} + \frac{1}{2} I \omega^2 + \frac{1}{2} q (l - x) (\omega r)^2$

~~$6,4 \cdot 2 \cdot 10^3 - 5,3 \cdot 10^3 = 5,7 \cdot 10^3 \omega^2 + 7,80 \omega^2$~~

?

3.55

$m = 1500 \text{ kg}$

$x = 0,15 \text{ m}$

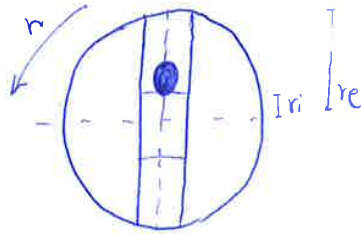
$v_0 = 1,1 \text{ m/s}$

$k_2 = ?$

$\frac{1}{2} m v_0^2 = \frac{1}{2} k_2 x^2 \rightarrow k_2 = 82288 \rightarrow \begin{cases} k_1 = 41144 \text{ N/m} \\ k_2 = 41144 \text{ N/m} \end{cases}$

363

- $r_e = 0,2 \text{ m}$
- $n = 1000 \text{ giri/min}$
- $r_i = 0,05 \text{ m}$
- $v_i = 0$
- $v_e = ?$



$$\omega = \frac{1000 \cdot 2\pi}{60} = 104,72 \text{ rad/s}$$

$$\frac{d}{dt} \int_{r_i}^{r_e} \omega^2 r^2 dr \rightarrow F = m a_n \rightarrow L = \int_{r_i}^{r_e} m a_n r dr = \int_{r_i}^{r_e} m \omega^2 r^2 dr$$

$$L = \frac{1}{2} m \omega^2 (r_e^2 - r_i^2)$$

$$\rightarrow \left(\frac{d}{dt} \int_{r_i}^{r_e} \omega^2 r^2 dr \right) = \frac{1}{2} \omega^2 (r_e^2 - r_i^2)$$

$$m L = \Delta E_c = \int_{r_i}^{r_e} m \omega^2 r^2 dr$$

$$L = \int_{r_i}^{r_e} m \omega^2 r^2 dr \rightarrow m \omega^2 \frac{r_e^2 - r_i^2}{2}$$

$$\Delta E_c = \frac{m v_e^2}{2}$$

$$\Rightarrow \frac{m \omega^2 (r_e^2 - r_i^2)}{2} = \frac{m v_e^2}{2} \Rightarrow v_e = 20,28 \text{ m/s}$$

4.1

TRASMISSIONE DEL TORO

- $f = 400 \text{ Hz}$
- $i = \text{poli} = 8$
- $n = 6000 \text{ giri/min} \rightarrow \omega = 628,31 \text{ rad/s}$
- $C_H = \frac{\Delta p_0}{2\pi} - k \omega^2$
- $\Delta = \text{cavità?}$
- $p_0 = 21 \text{ MPa}$
- $k = 0,0001 \text{ N ms}^2/\text{rad}^2$

- $\Delta_1 ? \setminus W_1 = 30 \text{ kW}$
- $\Delta_2 ? \setminus W_2 = 10 \text{ kW}$

$$W = C_H \cdot \omega = \left(\frac{\Delta p_0}{2\pi} - k \omega^2 \right) \omega$$

$$W_1 = \left(\frac{\Delta p_0}{2\pi} - k \omega^2 \right) \omega \rightarrow$$

$$W_1 = (\Delta 3342255,8 - 39,477) \omega$$

$$48,747 = \Delta 3342255,8 - 39,477 \rightarrow$$

$$\rightarrow \Delta = 7,60973 \cdot 10^{-5} \text{ m}^3$$

$$W_2 = (\Delta 3342255,8 - 39,477) \omega$$

$$15,816 + 39,477 = \Delta 3342255,8 \rightarrow$$

$$\rightarrow \Delta = 1,6573 \cdot 10^{-5} \text{ m}^3$$

4.7

$C_1 = (C_0 - k\omega_1)$

$C_0 = 30 \text{ Nm}$

$k = 0,1 \text{ Nm/s/rad}$

$C_2 = 100 \text{ Nm}$

$\tau = ? \setminus \omega_H = \max \begin{cases} \omega_1? \\ \omega_2? \end{cases}$

$(C_0 - k\omega_1)\omega_1 = C_2\omega_2$

$\omega_2 = \tau \omega_1$

$C_0\tau - k\omega_1\tau = C_2\tau\omega_1$

$\frac{C_1}{C_2} = \tau$

~~$C_0 - k\omega_1 = \tau C_2$~~

$C_1 = \tau C_2$

$\omega_1 = \frac{C_0}{k} - \frac{C_2\tau}{k}$

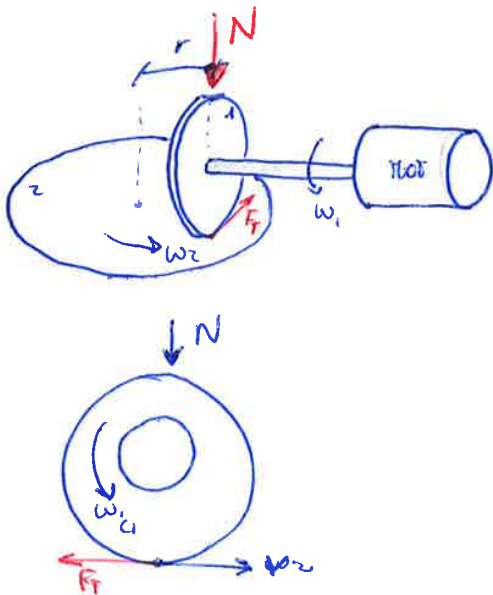
$W = \frac{C_2\tau}{k}(C_0 - C_2\tau) \rightarrow W \text{ e' max se } \frac{dW}{d\tau} = 0$

$\Rightarrow W = \frac{C_2 C_0 \tau - C_2^2 \tau^2}{k} \Rightarrow \frac{1}{k}(C_2 C_0 - 2C_2^2 \tau) = 0 \rightarrow C_2 C_0 = 2C_2^2 \tau \rightarrow \tau = 0,15$

~~$C_1 = \tau C_2 \rightarrow 15 \rightarrow (30 - 0,1\omega_1) = 15 \rightarrow 2 - 0,1\omega_1 = 0 \rightarrow \omega_1 = 300 \text{ rad/s}$~~

$\rightarrow \frac{300 \cdot 60}{2\pi} = \omega_1 = \frac{C_0}{k} - \frac{C_2\tau}{k} = \omega_1 = 150 \text{ rad/s} \rightarrow n_1 = 1432,4 \text{ giri/min}$

4.8



$N = 1000 \text{ N}$

$d_1 = 0,1 \text{ m}$

$W = 368 \text{ W cost}$

$C_2 = k\omega_2^2$

$k = 9 \cdot 10^{-4} \text{ Nm/s}^2/\text{rad}^2$

$f = 0,2$

$r = ? \setminus F_t \leq fN$

Suppongo $\tau = 1$

$W = C_2\omega_1 = k\omega_2^3$

~~$\rightarrow \omega_2 = 1059,4 \text{ rad/s}$~~

~~$v_2 = r\omega_2$~~

$368 = k\omega_2^3 \rightarrow \omega_2 = 74,72 \text{ rad/s}$

~~$Nr = Ft \cdot d_1/2$~~

$Nr = F_t \cdot d_1/2$

$F_t v = W \rightarrow F_t \omega_2 r = W$

$\rightarrow F_t = \frac{W}{\omega_2 r}$

$Nr = \frac{W}{\omega_2 r} \cdot d_1/2 \rightarrow r^2 = \frac{W d_1}{2\omega_2 N} = 0,0002479 \text{ m}$

$F_t r = C_2 \rightarrow F_t = \frac{k\omega_2^2}{r} \rightarrow$

$F_t \leq fN \rightarrow fN = \frac{k\omega_2^2}{r} \rightarrow r = \frac{k\omega_2^2}{fN} = 0,02478 \text{ m}$

$$\sum \vec{F} \cdot \vec{u}_p - F_L \cos \alpha \sin \beta + F_L \cos \alpha \cos \beta + F_a \cos \beta = 0$$

$$\rightarrow F_L \cos \alpha + F_a \cos \beta - F_L \cos \beta = 0$$

$$F_L = (F_L \cos \alpha + F_a \cos \beta) \cdot \frac{1}{\cos \beta} \rightarrow m_p g - \text{tpf} (F_L \cos \alpha + F_a \cos \beta) + F_L \sin \alpha + F_a \sin \beta = 0$$

$$F_L = \frac{m_p g}{\cos \beta}$$

4.13

$$m = 2400 \text{ kg}$$

$$\alpha = 10^\circ$$

$$D = 128 \text{ cm}$$

$$I_H = 0.15 \text{ kgm}^2$$

$$\tau = \frac{W_A}{W_H} = 1/36$$

$$z = 0.75$$

$$d = 0.7 \text{ m}$$

$$\rho = 9003 \text{ kg/m}^3$$

$$u = 0.15 \text{ m/s}$$

$$V = 5 \text{ m/s}$$

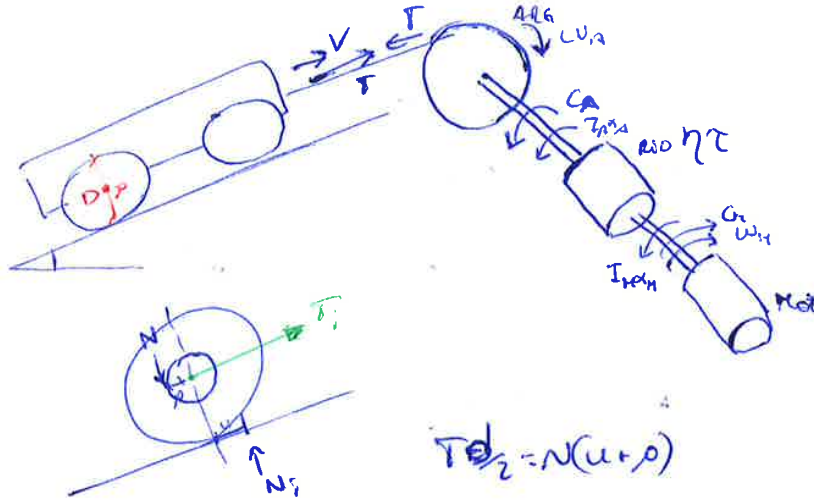
$$P \text{ in } H \setminus V = \text{cost}$$

$$W_H = ?$$

$$T_0 = ?$$

$$G_0 = 2C_H$$

$$I_A = 25 \text{ kgm}^2$$



$$T \frac{D}{2} = N(u + 0)$$

$$C_H = T \frac{D}{2}$$

$$(C_H + I_A \frac{a}{D}) \tau = \eta (-I_H \frac{a}{D} + G_H)$$

$$P \text{ in } T$$

$$T - m_p g \sin \alpha - f_i = m a$$

$$N_i - m g \cos \alpha = 0$$

$$\alpha_A = \frac{a}{D/2} \quad \alpha_H = \frac{a}{D}$$

$$W_A = \frac{1}{2} D a \quad W_H = W_A \tau$$

$$\rightarrow T = m_p g \left[\sin \alpha + \frac{z(u+u) \cos \alpha}{d} \right] + m a$$

$$\left[T \frac{D}{2} + z I_A \frac{a}{D} \right] \tau = \eta \left[-I_H \frac{a}{D} + G_H \right] \rightarrow$$

$$\rightarrow \left\{ m_p g \left[\sin \alpha + \frac{z(u+u) \cos \alpha}{d} \right] + m a \right\} \frac{D}{2} + z I_A \frac{a}{D} \tau = \eta \left[-I_H \frac{a}{D} + G_H \right]$$

condiz. regime $\rightarrow V = \text{cost.} \quad a = 0 \rightarrow \frac{T}{\eta} m_p g \frac{D}{2} \left(\sin \alpha + \frac{z(u+u) \cos \alpha}{d} \right) = G_H = 125,042 \text{ Nm}$

$$P_H = G_H \cdot \frac{V}{D} = 125,042 \cdot \frac{5}{0.64} = 9767,3 \text{ W} \quad P_H = G_H \cdot \frac{V}{D} \cdot \frac{1}{\tau} = 125,042 \cdot \left(\frac{5}{0.64} \cdot 36 \right) = 9767,3 \text{ W} \quad W_H = 281,25 \text{ rad/s}$$

$$\left\{ m_p g \left[\sin \alpha + \frac{z(u+u) \cos \alpha}{d} \right] + m a \right\} \frac{D}{2} + z I_A \frac{a}{D} \tau = \eta \left[-I_H \frac{a}{D} + G_H \right]$$

$$G_0 = 2C_H$$

$$50,0858 = 84.11 \rightarrow$$

$$\rightarrow a = 1,88 \text{ m/s}^2$$

$$\rightarrow T_0 = 525743 + 2400 \cdot 1,88 = 9767 \text{ N}$$

4.201

$G_0 = 170 \text{ Nm}$
 $C_0 = k \omega_1^2$
 $k = 7 \text{ MN s}^2$

$\tau = 1/6$

$I_1 = 0,0045 \text{ kg m}^2$

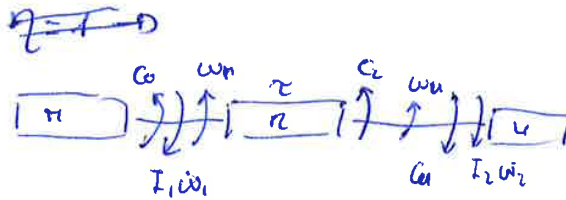
$I_2 = 0,7 \text{ kg m}^2$

$H_p \left\{ \begin{array}{l} I_R \approx 0 \\ \eta = 1 \end{array} \right.$

$\omega_H = ?$
 $\omega_U = ?$ } regime

$\Delta \theta_A = ? \quad \omega_0 = 0 \quad \omega_A = \omega_H / 2$

$C_M = ? \quad \omega_A = \omega_H / 2$



$\eta = d \rightarrow \frac{C_1}{C_2} = \tau = \frac{\omega_2}{\omega_1} = \frac{\dot{\omega}_2}{\dot{\omega}_1}$

$C_1 = C_M - I_1 \dot{\omega}_1$

$C_2 = C_U + I_2 \dot{\omega}_2$

in condizioni di regime

$C_2 = C_U = 1570 \text{ Nm}$ $\frac{d\omega}{dt} = 0 \rightarrow \dot{\omega} = 0$

$C_2 = k \omega_2^2 = \frac{C_1}{\tau} \rightarrow \omega_2 = \sqrt{\frac{C_1}{\tau k}} = 16,56 \text{ rad/s}$

$\omega_1 = \tau \cdot \omega_2 = 265 \text{ rad/s}$

~~$\Delta \theta = \omega_1 \Delta t + \frac{1}{2} \dot{\omega}_1 \Delta t^2$~~ ~~$\rightarrow \Delta t =$~~

$\frac{\omega_H}{2} = \omega_1 \Delta t \rightarrow \dot{\omega}_1 = \frac{\omega_H}{2 \Delta t}$



~~$d\theta = \omega dt$~~ $C_2 = C_U + I_2 \dot{\omega}_2$

$\tau = \frac{C_1}{C_U} = \frac{\dot{\omega}_U}{\dot{\omega}_1} = C_1 \dot{\omega}_1 = C_U \dot{\omega}_U \rightarrow I_1 \dot{\omega}_1^2 = I_2 \dot{\omega}_U^2 \rightarrow I_U = I_1 \left(\frac{\dot{\omega}_1}{\dot{\omega}_U} \right)^2$

$I_U = \frac{I_1 C_U}{\tau^2} + I_2 = 1,852 \text{ kg m}^2$

$C_2 - C_U = I_U \frac{d\omega}{dt}$ $d\theta = \omega dt$

$dt = \frac{I_U d\omega}{C_2 - C_U} \rightarrow d\theta = \frac{k \omega d\omega}{C_2 - C_U} \rightarrow \theta = \int_0^{\omega_A} \frac{k \omega d\omega}{C_2 - C_U} = \frac{k \omega d\omega}{C_2 - k \omega^2} \rightarrow$

$\rightarrow \frac{I_U}{2k} \ln(C_2 - k \omega_A^2) \Big|_0^{\omega_A} \rightarrow \frac{I_U}{2k} \ln \left[\frac{C_2}{C_2 - k \left(\frac{\omega_H}{2} \right)^2} \right] = 0,038 \text{ rad}$

$\omega_f = \omega_H / 2$

$\theta_1 = \theta / \tau = 0,608 \text{ rad}$

$\dot{\omega} = \frac{C_2 - k \omega^2}{I_U} = 277,6 \text{ rad/s}^2 \rightarrow \omega_1 = \frac{\omega_f}{\tau} = 1241,1 \text{ rad/s}^2$

$C_1 = G_0 - I_1 \dot{\omega}_1 = 64 \text{ Nm}$

4.271

$C_M = 15000 + 4665 \sin(30) \text{ Nm}$

$C_u = 15000 + 2000 \sin \theta \text{ Nm}$

$I = 1000 \text{ kgm}^2$

$\omega = 62.8 \text{ rad/s}$ quando $\theta = \frac{\pi}{2} \text{ rad}$

$\frac{dw}{d\theta} = ?$

$\bar{P} = ?$

$\frac{dw}{dt} = \frac{C_M - C_u}{I} \Rightarrow 4665$

$\Rightarrow 4665 \sin(30) - 2000 \sin \theta$

$d\theta = \omega dt$

$\Rightarrow \int_{\omega_0}^{\omega} \omega d\omega = \int_{\frac{\pi}{2}}^{\theta} (4665 \sin(30) - 2000 \sin \theta) d\theta \Rightarrow \frac{\omega^2}{2} - \frac{\omega_0^2}{2} = -1.555 \cos(30) + 2 \cos \theta$

$\bar{E} = \bar{P} = C_M \cdot \omega_0 \rightarrow 15000 \cdot 62.8 = 942.5 \text{ kW}$

$\theta = \frac{\pi}{2} \text{ rad} \rightarrow C_M = 11335 \text{ Nm}$

$C_u = 2000 \text{ Nm}$

$\Delta L = 67.665 \text{ Nm}$

$\epsilon = \frac{\Delta L}{L} = 0.000168$

$w = \sqrt{\frac{(3665 \sin(30) - 2000 \sin \theta)}{I \epsilon}}$

$\frac{dw}{d\theta} = \frac{1}{2I\epsilon} \cdot (10995 \cos(30) - 2000 \cos \theta)^{\frac{1}{2}}$

$= \frac{1}{2I\epsilon} \cdot (10995 \cos(30) - 2000 \cos \theta)^{-\frac{1}{2}}$

4.28

$\tau = 30:1 \rightarrow \frac{C_1}{C_2} = \frac{1}{30}$

$C_u = n_u^2 (3048 - 381 \sin(2\theta_u) + 763 \cos(2\theta_u)) \text{ Nm}$

$C_r = 500 - 0.026 n_r^2 \text{ Nm}$

$I_r = 10 \text{ kgm}^2$

$I_u = 1000 \text{ kgm}^2$

$\bar{n}_u = 2 \text{ rev/s}$ se $\theta_u = k\pi$

$\frac{dw_u}{d\theta_u} = ?$

$H_p \quad \epsilon \ll 1 \rightarrow \bar{n}_u \approx n_u$

$15000 - 12197 - 1524 \sin(2\theta) + 3052 \cos(2\theta) = \frac{dw_u \cdot \omega}{d\theta}$

$\int_0^{\theta_u} (-0.3052 \cos(2\theta) + 0.1524 \sin(2\theta)) d\theta = \int_{\omega_u}^{\omega} \omega d\omega$

$(-0.3052 \sin(2\theta) - 0.1524 \cos(2\theta)) = \frac{\omega^2}{2} - \frac{\omega_u^2}{2}$

$(-0.3052 \sin(2\theta) - 0.1524 \cos(2\theta)) = \omega^2$

4.35

a)

$P = 2 \cdot 10^4 \text{ W}$

$h = 0,8 \text{ m}$

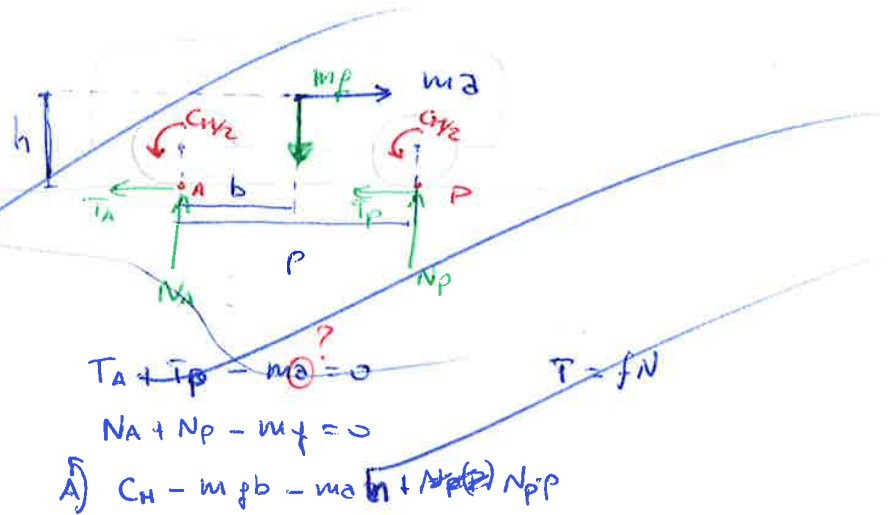
$b = 1,1 \text{ m}$

$f_s = 0,5$

$a_{\text{max}}?$ \ (a moti motori a)

$a_{\text{max}}?$ \ (moti motori sul b)

$a_{\text{max}}?$ \ (moti motori post b)



$T_A + T_P - m a = 0$

$N_A + N_P - m g = 0$

$\sum \tau: C_H - m g b - m a (h + N_P) = 0$

$T = f N$

4.37

$m = 500 \text{ t} = 5 \cdot 10^5 \text{ kg}$

$v = \text{cost} = 20 \text{ m/s}$

$t_{p0} = 0,01 \rightarrow \Delta \theta = 0,573$

$R = R_0 + k v^2$

$R_0 = 18000 \text{ N}$

$k = 25 \text{ N s}^2/\text{m}^2$

$T = ?$

$W = ?$

$\eta = 1$

$T = 0 \rightarrow \dot{x}?$

$\Delta s \rightarrow v = 0$

$T - R - m g \sin \theta = 0 \rightarrow T = 76997,5 \text{ N} \rightarrow W = 1539,95 \text{ kW}$

$R = 18000 + 10000 = 28000$

~~$T = 0 \rightarrow R = m g \sin \theta \rightarrow m a \rightarrow a = 0,154 \text{ m/s}^2$~~

$\frac{1}{\Delta v} \int_0^v R dv = \frac{1}{\Delta v} \int_0^v (R_0 + k v^2) dv = \frac{1}{\Delta v} \left(R_0 v + \frac{k v^3}{3} \right)$

$= \left(R_0 v + k \frac{v^3}{3} \right) / \Delta v = (18000 + 3333,33 \text{ N}) = 21333,33 \text{ N}$

$-R - m g \sin \theta = m a \rightarrow a = -0,14067 \text{ m/s}^2$

$\Delta s = v_0 t + \frac{1}{2} a t^2$

$0 = v_0 + a t \rightarrow t = 142,17 \text{ s}$

$\Delta s = 1421,87 \text{ m}$

$$2 v^2 \frac{d}{2} + \frac{m p d}{2} f v^2 + \frac{k x^2}{2} V = \frac{7}{2} G - \frac{m p d}{2} f v_0$$

$$0,1338 v^2 + 0,01784 v^2 + 9,31 V = 665 - 167,442 \rightarrow V = 33,15 \text{ m/s}$$

$$a = ? \quad v_0 = 0 \rightarrow R = 0, \quad u = \frac{g}{2} f v_0$$

$$\epsilon p \approx 0,06 \rightarrow \theta = 3,434^\circ$$

$$\tau = 0,075$$

$$C_R = m p u \cos \theta = m p \frac{g}{2} f v_0 \cos \theta$$

$$C_R = m p \sin \theta \frac{g}{2} + m p x \frac{g}{2} + m p \frac{g}{2} f v_0 \cos \theta \rightarrow \frac{C_R}{\tau} = m p g$$

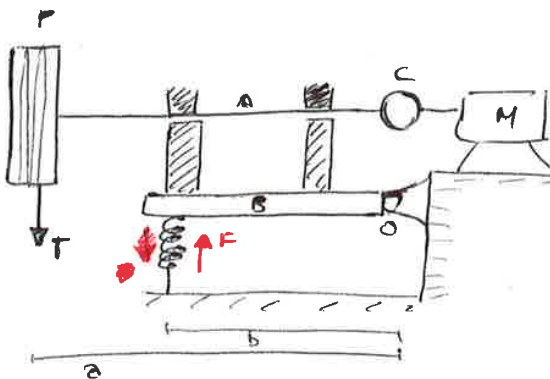
$$C_R = \frac{\tau C_R}{\tau} = 17,5 \cdot 7,89 \cdot 291266,67$$

$$\rightarrow x = \frac{930,43}{455} = 2,045 \text{ m/s}^2$$

$$= \frac{\tau C_R}{\tau d}$$

GIUNTI

S.11



$$k = 40 \text{ N/mm} \rightarrow 40000 \text{ N/m}$$

$$T = 2500 \text{ N}$$

$$a = 1,2 \text{ m}$$

$$b = 1 \text{ m}$$

$$\Delta \omega = \omega_{\max} - \omega_{\min}$$

$$n_{\max} = 3000 \text{ rpm} \rightarrow 314 \text{ rad/s}$$

$$F b = T a \rightarrow F = 3000 \text{ N}$$

$$\rightarrow F = k \Delta x \rightarrow \Delta x = 0,075 \text{ m}$$

$$\Delta x : b = \Delta \epsilon : a \rightarrow \Delta \epsilon = 0,09 \text{ m}$$

$$\alpha = \arcsin \frac{\Delta x}{a} \rightarrow \alpha = 4,3^\circ$$

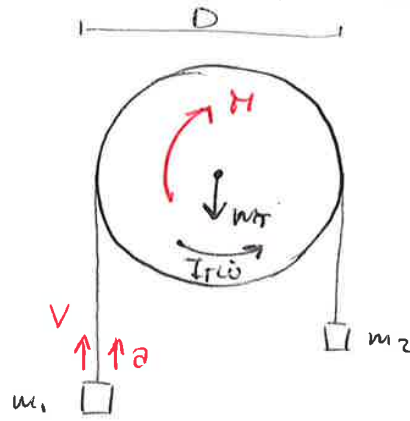
$$\omega_{\max} = \frac{\omega_H \cdot \cos \alpha}{\cos \alpha} = 315 \text{ rad/s}$$

$$\omega_{\min} = \omega_H \cos \alpha = 313,12 \text{ rad/s}$$

$$\Delta \omega = 1,94 \text{ rad/s}$$

5.6) FLESSIBILI

- $m_1 = 500 \text{ kg}$
- $m_2 = 150 \text{ kg}$
- $D = 1.2 \text{ m}$
- $\rho = 0.5 \text{ m}$
- $m_2 = 300 \text{ kg}$
- $H = ? \quad a_1 = 1.2 \text{ m/s}^2$
- $W = ? \quad \text{se } v_1 = 2.4 \text{ m/s}$
- $C_R = 80 \text{ Nm}$



~~$m_1 f + m_2 f =$~~

$$-C_R + H - m_1 f D_2 + m_2 f D_2 = \frac{1}{2} (m_1 \rho^2) \dot{\omega} + (m_1 - m_2) a$$

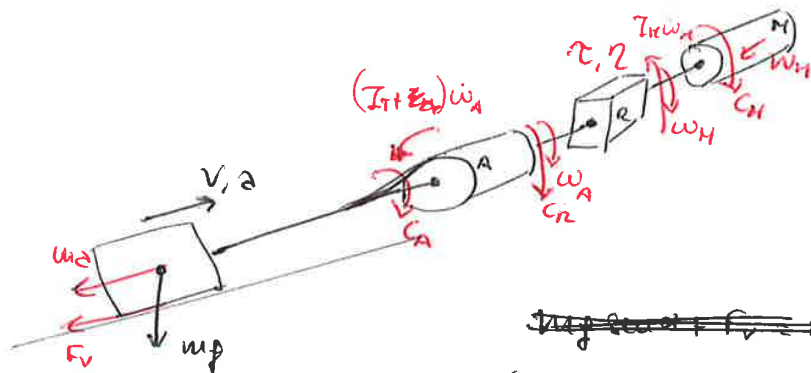
$$\dot{\omega} = 2a/D_2 \Rightarrow H = \text{~~1363 Nm~~ 1363 Nm}$$

$$W = H v = \text{~~3312 W~~ 3312 W}$$

$$H - C_R - m_1 f D_2 + m_2 f D_2 = 2m_1 \rho^2 \dot{\omega} + (m_1 + m_2) a = 0 \rightarrow H = 1907 \text{ Nm} \rightarrow W = 7628 \text{ W}$$

5.7)

- $m = 14 \text{ t}$
- $\alpha = 3^\circ$
- $d = 1 \text{ m}$
- $r = 1/40$
- $\eta = 0.85$
- $I_T = 230 \text{ kg m}^2$
- $I_M = 1.8 \text{ kg m}^2$
- $F_V = 1150 \text{ N}$
- $C_H? \quad W_H?$
- $v = 1.5 \text{ m/s}$
- $a = 0.1 \text{ m/s}^2$



~~$m g \sin \alpha + F_V = m a$~~

$$C_A = (m_0 + F_V + m g \sin \alpha) D/2 = 49865.24 \text{ Nm}$$

$$C_R = C_A + (I_T + I_R) \frac{a}{D/2} = 49911.1 \text{ Nm}$$

$$C_H = \frac{I}{\eta} C_R = 144,46 \text{ Nm}$$

$$W_R = 3 \text{ rad/s} \Rightarrow W_H = \text{~~437.38~~ 120 rad/s}$$

$$C_R = C_A + I_T \frac{a}{D/2} = 49911.24 \text{ Nm}$$

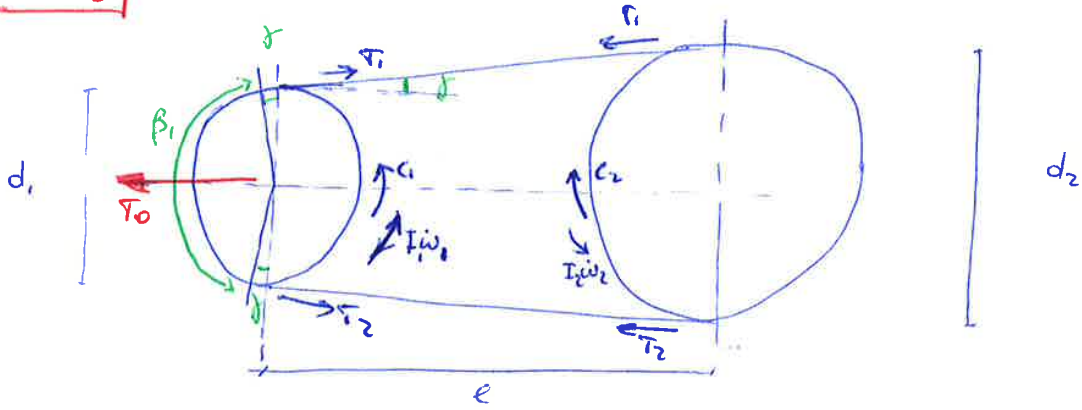
~~$\eta C_H = (C_R + I_T \frac{a}{D/2}) \frac{D}{2}$~~

$$\eta C_H = C_R r + I_M \frac{2a}{D} = 161.4 \text{ Nm}$$

$$W_H = 120 \text{ rad/s}$$

$$\Rightarrow W = 161.49 \cdot 120 = 19366.73 \text{ W}$$

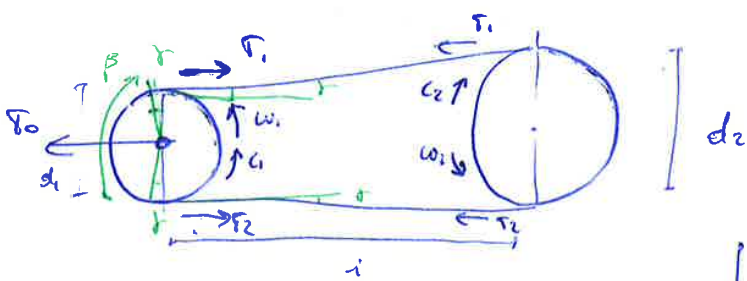
5.13



$d_1 = 1\text{ m}$
 $d_2 = 1,8\text{ m}$
 $l = 7,6\text{ m}$
 $f = 0,17$
 $T_1 = 40\text{ kpm}^2$
 $T_2 = 65\text{ kpm}^2$
 $\eta = 1$
 $\partial \text{max}_1 = ?$ se ho C_1
 $\partial \text{max}_2 = ?$ se ho C_2
 $T_0 = 60000\text{ N}$
 $C_R = 0 \rightarrow C_1 = 0, C_2 = 0$

$\gamma = \arcsin\left(\frac{d_2 - d_1}{2l}\right) = 3,018^\circ$
 $\beta = \pi - 2\gamma = 173,966^\circ$
 $T_1 \cos \gamma + T_2 \cos \gamma = 2T_0$
 $T_2 e^{f\beta} \cos \gamma + T_2 \cos \gamma = T_0 - T_1 = \frac{T_0}{\cos \gamma} (1 + e^{f\beta})^{-1}$
 $\frac{T_1}{T_2} = e^{f\beta}$
 $T_2 = 160758,43\text{ N}$
 $T_1 = 269365,80\text{ N}$
 $T_2 = 89739,51\text{ N}$
 $T_2 = 4,09 \cdot 10^9\text{ N}$
 $T_1 = 7,52 \cdot 10^9\text{ N}$
 $\sum M_0 = T_1 \cos \gamma d_1 + T_2 \cos \gamma d_2 + I_1 \omega_1 = 0$
 $\omega_1 = 1355,71\text{ rad/s}$
 $378,64\text{ rad/s}$
 $\omega_2 = 419,57\text{ rad/s}$

5.14



$d_1 = 0,3\text{ m}$
 $d_2 = 0,9\text{ m}$
 $l = 1,2\text{ m}$
 $q = 0,6\text{ kpm}$
 $f = 0,26$
 $T_0 = 1200\text{ N}$
 $\beta = ?$
 $W_{\text{max}} = ?$
 $\omega = 78,54\text{ rad/s}$

$\gamma = \arcsin\left(\frac{d_2 - d_1}{2l}\right) = 14,98^\circ$
 $\beta = 151,02^\circ$
 $v = \omega \cdot \frac{d_1}{2} = 11,78\text{ m/s}$

$\begin{cases} \frac{T_1 - qv^2}{T_2 + qv^2} = e^{f\beta} \rightarrow T_1 = qv^2 \frac{(T_2 + qv^2)e^{f\beta}}{T_2 + qv^2} \\ T_1 \cos \gamma + T_2 \cos \gamma = 2T_0 \end{cases}$

$W_{\text{max}} = T_1 v + T_2 v = 0$
 $\rightarrow [qv^2 \frac{(T_2 + qv^2)e^{f\beta}}{T_2 + qv^2} + T_2] \cos \gamma = 2T_0 \rightarrow T_2 = 854,94\text{ N}$
 $qv^2 (e^{f\beta} + 1) \cos \gamma = 2T_0 - qv^2 (1 + e^{f\beta}) \cos \gamma \rightarrow T_2 = 747,45\text{ N}$
 $\rightarrow T_1 = 1731,4\text{ N}$
 $\Rightarrow W = 11590,857\text{ W}$
 $8944,9\text{ W}$

5.21

$z_1 = 18$

$C_1 = 50 \text{ Nm}$

$C_2 = k \omega_2^2$

$k = 0,02 \text{ Nm}^2/\text{rad}^2$

$z_1 = ? \setminus n_1 \approx 800 \text{ rpm} \rightarrow 83,77 \text{ rad/s}$

$z_2 \rightarrow n_2 = ? \quad W = ?$

$H_p = \eta = 1$

$\tau = \frac{\omega_2}{\omega_1} = \frac{C_1}{C_2} = \frac{z_1}{z_2}$

$C_1 = \tau C_2 \rightarrow C_1 = \tau k \omega_2^2$

$\tau = 0,3562 = \frac{z_1}{z_2} = 50,53 \approx 51$

$\Rightarrow C_1 = \tau k \omega_2^2 \rightarrow \omega_2 = \sqrt{\frac{C_1}{k \tau}} = 84,16 \text{ rad/s}$

$W = k \omega^2 = 11923 \text{ W}$

In piano (p)

5.22

$W = 7 \text{ kg kW}$

$n_1 = 1800 \text{ rpm/min}$

$\tau = 0,11$

$m = 3 \text{ mm}$

$\theta = 20^\circ$

$i = 0,24435 \text{ m}$

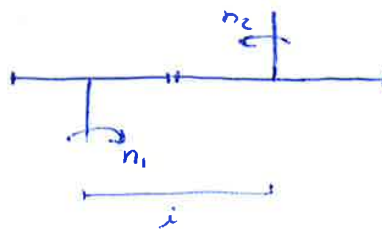
$z_1 = ?$

$z_2 = ?$

$z_p = ?$

$b = ?$

$f_{\text{max}} = 120 \text{ N/mm} = 120 \cdot 10^3 \text{ N/m}$



$\omega_1 = n_1 \frac{2\pi}{60} = 188,5 \text{ rad/s}$

$\Rightarrow C_1 = 37,136 \text{ Nm}$

$Q = C_1 / r_1 = 1650,495 \text{ N}$

$Q = F \cos \theta \rightarrow F = 1756,42 \text{ N}$

$b \cdot f = F \Rightarrow b = \frac{F}{f} = 0,0146 \text{ m}$

$m = \frac{P}{z} = \frac{2\pi r}{z} \Rightarrow P =$

$\Rightarrow P = 9,424 \text{ mm}$

$= 2\pi \frac{r}{z} = 2\pi \frac{r_2}{z_2}$

$\left\{ \begin{aligned} \frac{r_1}{r_2} &= \frac{z_1}{z_2} \Rightarrow \\ r_1 + r_2 &= 242,5 \text{ mm} \end{aligned} \right.$

$\Rightarrow r_1 + r_2 = 242,5 \text{ mm}$

$\Rightarrow i = \frac{11}{10} r_2 \Rightarrow r_2 = 225 \text{ mm}$

$\Rightarrow r_1 = 22,5 \text{ mm}$

$\Rightarrow z_1 = \frac{P}{m} \frac{2\pi r_1}{P} = 15$

$z_2 = 150$



$\sum \mathcal{M}_z \rightarrow R_{Az} - A r_1 - R_{Az} d = 0 \rightarrow R_{Az} = -1953,8N$

$\sum \mathcal{M}_z \rightarrow R_{Ay} + R_{Ay} d = R_{Ay} = 5189,8$

$R_A = 5505,14N$

$R_B = 8174,81N$

$R_x = -A = -5892,7N$

5.28

$r_1 = 44mm$

$r_2 = 260mm$

$d = 75$

$\alpha_n = 20^\circ$

$f = 0,05$

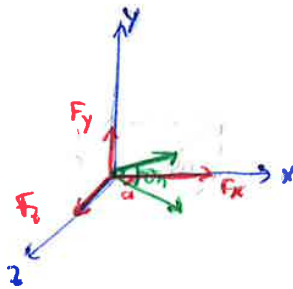
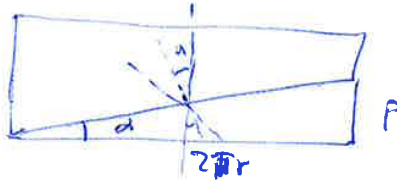
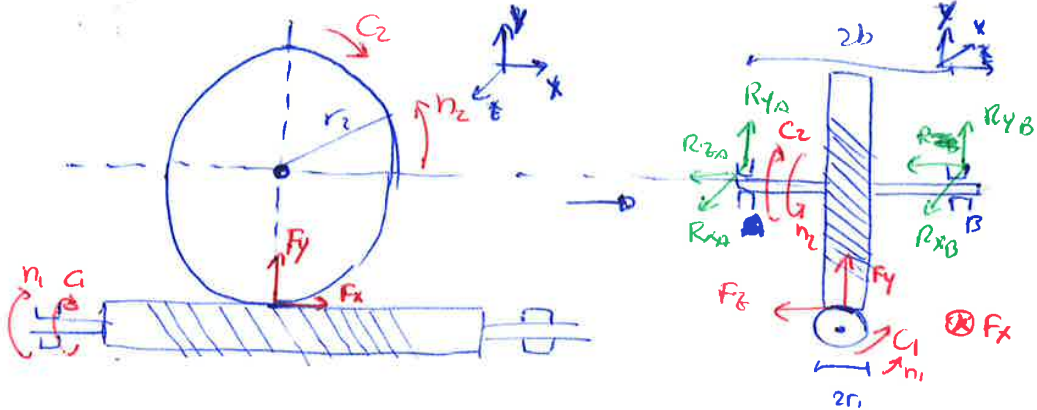
$b = 115mm$

$R_A = ?$

$R_B = ?$

$W = 4000W$

$n_1 = 1000rpm/min$



$$\begin{cases} F_x = F(\cos \alpha_n \cos \alpha - f \sin \alpha) \\ F_y = F \sin \alpha_n \\ F_z = F(\cos \alpha_n \sin \alpha + f \cos \alpha) \end{cases}$$

$F_z = \frac{W}{\omega_1}$

$C_1 = \frac{W}{\frac{n_1}{60}} = 381,97Nm$

$F_z = C_1 r_1 = 8681,18N$

$\rightarrow F_y = \frac{F_z \sin \alpha_n}{(\cos \alpha_n \sin \alpha + f \cos \alpha)} = 6710,73N$

$F_x = \frac{F(\cos \alpha_n \cos \alpha - f \sin \alpha)}{(\cos \alpha_n \sin \alpha + f \cos \alpha)} = 16295,51N$

A) // y) $-R_{xB} z_b + F_x b = 0 \rightarrow R_{xB} = 8147,5N$

B) // x) $+R_{xA} z_b - F_x b = 0 \rightarrow R_{xA} = 8147,5N$

A) // y) $R_{yB} z_b - F_z z_b + F_{yB} + C_1 = 0 \rightarrow R_{yB} = 675,51N$

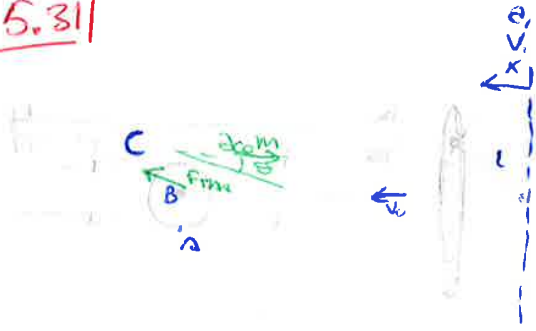
B) // x) $+R_{yA} z_b + F_{yB} + F_z z_b - C_1 = 0 \rightarrow R_{yA} = -6031,13N$

$F_z + R_{yA} = 0 \rightarrow R_{yA} = -8681,18N$

$R_A = 15486,47N$

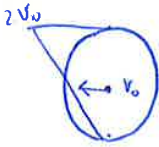
$R_B = 10396,83N$

5.31



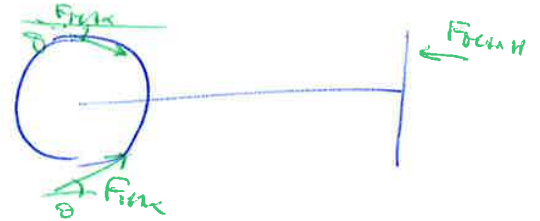
$x = l \sin(\omega t)$ $x = l \sin(\omega t)$
 $\omega = 31.4 \text{ rad/s}$
 $\theta_0 = 20^\circ$
 $m = 50 \text{ kg}$
 $v_0 = 0.1 \text{ m/s} \rightarrow v_{MAX} \rightarrow \sin(\omega t) = 1$
 $x_{C0} = ?$ $F_{MAX CB} = ?$
 $v_{C0} = ?$ $F_{MAX H} = ?$
 $a_{C0} = ?$

$x = l \sin(\omega t)$
 $v = \omega l \cos(\omega t)$ $v_{MAX} \rightarrow \cos = 1 \Rightarrow \omega t = 0 \rightarrow t = 0$
 $a = -\omega^2 l \sin(\omega t)$

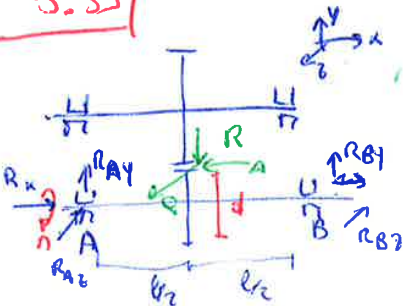


$x_{C0} = 2r = 2 \frac{v_0}{\omega} = 6.366 \cdot 10^{-3} \text{ m}$
 $v_{C0} = 2v = 2\omega l = 0.7 \text{ m/s}$
 $a_{C0} = -2\omega^2 l = -2\omega v_0 = 6.28 \text{ m/s}^2$

$F_{MAX} = \frac{200 \text{ m}}{\cos 20} = 334.32 \text{ N}$
 $F_{MAX H} = \frac{F_{MAX} \cos 20}{2} = 628.3 \text{ N}$



5.33



$W = 15 \text{ kW}$
 $\omega = 94.2 \text{ rad/s}$
 $d = 0.048 \text{ m}$
 $\theta_n = 20^\circ$
 $\alpha = 18.166^\circ$
 $r = 0.08 \text{ m}$

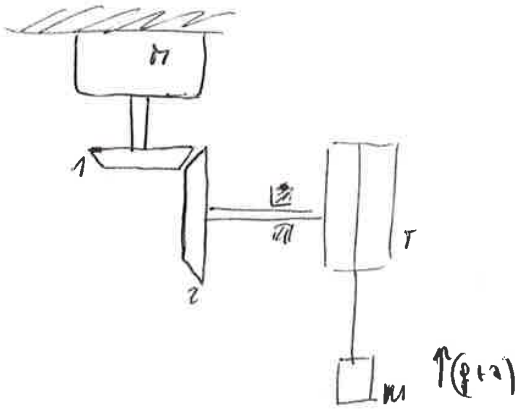
$C = \frac{W}{\omega} \rightarrow Q = 2C/d \rightarrow \Delta A = Q \cdot d$
 $\rightarrow \Delta R = \frac{W}{\omega} \cdot \frac{1}{\cos \theta_n}$
 $Q = 6639.87 \text{ N}$
 $A = 1976.8 \text{ N}$
 $R = 2518.5 \text{ N}$

$3315.6 \text{ N} = R_{A0} \leftarrow B) // y: R_{Ay} \cdot l - Q \cdot l_2 = 0 \rightarrow R_{Ay} = \frac{Q}{2}$
 $3315.6 \text{ N} = R_{B0} \leftarrow A) // y: R_{By} \cdot l - Q \cdot l_2 = 0 \rightarrow R_{By} = \frac{Q}{2}$
 $1852.3 \text{ N} = R_{Ay} \leftarrow B) // z: A \cdot d_2 + R_{Ay} \cdot l - R_{By} \cdot l = 0$
 $666.2 \text{ N} = R_{By} \leftarrow A) // z: R_{By} \cdot l - R_{Az} \cdot d_2 = 0$

$R_A = \sqrt{R_{Ax}^2 + R_{Ay}^2 + R_{Az}^2} = 4281.6 \text{ N}$

$R_B = \sqrt{R_{By}^2 + R_{Bz}^2} = 3381.9 \text{ N}$

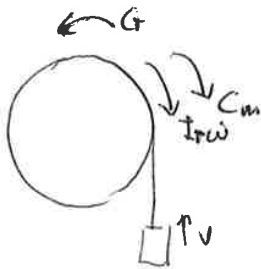
5.401



$h = 0,8 \mu \rightarrow v = 0 \rightarrow 2 \text{ m/s}$
 $\varphi_1 ? \varphi_2 = ?$
 $\theta = ?$
 $C_H = ?$
 $z_1 = 17$
 $z_2 = 46$
 $d = 0,8 \text{ m}$
 $I_T = 9 \text{ kg m}^2$
 $m = 50 \text{ kg}$

$v = \omega r \rightarrow \omega = \frac{v}{r}$
 $\frac{1}{2} \omega^2 = h = \frac{1}{2} \omega^2 r^2 =$
 $= h = \frac{1}{2} \frac{v^2}{r^2} t^2 = \omega t = 0,25$
 $\Rightarrow \omega = 2,5 \text{ rad/s}$

\uparrow
 $\omega_T = 6,25 \text{ rad/s}^2$
 $C_H \Rightarrow$
 $C_H = m(g + a) \frac{d}{2} + I_T \omega_T =$
 $= 302,25 \text{ N m}$

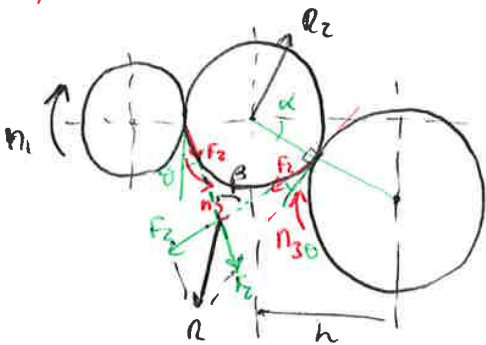


$\omega_2 = \omega_T$
 $\tau = \frac{z_1}{z_2} = 0,369 \rightarrow \omega_1 = 16,91 \text{ rad/s}^2$

$\frac{z_1}{z_2} = \frac{\sin \varphi_1}{\sin \varphi_2} \Rightarrow \frac{\sin \varphi_1}{\sin(\varphi_2 - \varphi_1)} \Rightarrow \tan \varphi_1 \Rightarrow \varphi_1 = 20,25^\circ$
 $\varphi_2 = \varphi_2 - \varphi_1 \Rightarrow \varphi_2 = 67,75^\circ$

$\frac{C_H}{G} = \tau \Rightarrow C_H = \tau G = 111,53 \text{ N m}$

Rotismi



$r_2 = \frac{m z_2}{2} = 28,29 \text{ mm} \approx 28 \text{ mm}$

$C_2 = W / \omega_2 = 18,69 \text{ N m}$

$\Rightarrow F_2 = C_2 / r_2 \cos \theta = 736,76 \text{ N}$

$\alpha = \frac{r_2 \sin \theta}{r_2 + r_3} \Rightarrow 65,96^\circ$

$R = R_2 = 2 F_2 \cos \beta / 2 = 887,2 \text{ N}$

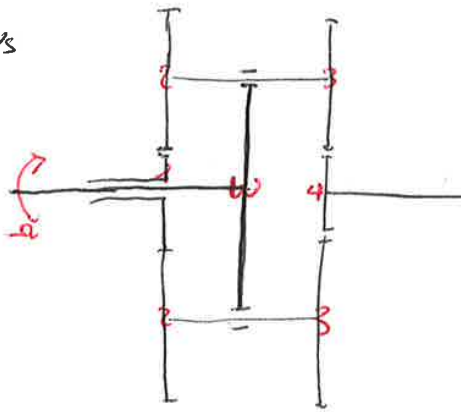
$W = 3 \text{ kW}$
 $n_1 = 1725 \text{ rpm}$
 $z_1 = 16$
 $z_2 = 18$
 $z_3 = 22$
 $D = 20^\circ$
 $h = 0,055 \text{ m}$
 $n_2 = ?$
 $n_3 = ?$
 $V = ?$
 $m = 3 \text{ mm}$

$\frac{n_2}{n_1} = \frac{z_1}{z_2} \Rightarrow n_2 =$
 $n_2 = 1533,33 \text{ rpm}$
 $\frac{n_3}{n_2} = \frac{z_2}{z_3} \Rightarrow n_3 = 383 \text{ rpm}$
 V_2
 $r_1 = \frac{m z_1}{2} = 24 \text{ mm}$
 $\Rightarrow V = n_1 \frac{2\pi r_1}{60}$
 $= 4,33 \text{ m/s}$
 $r_3 = 0,108 \text{ m}$

$\beta = -[(180 - \alpha) + 2(90 - \theta)] + 360 \Rightarrow \beta = 105,96^\circ$

5.48

$n_p = 800 \text{ psi} / \text{mm} = 83,73 \text{ rad/s}$
 $W = 8 \text{ kNm}$
 $z_1 = 20$
 $z_2 = 24$
 $z_4 = 24$
 $\omega_4 = ?$
 $C_1 = ?$
 $\omega_1 = 0$



$z_1 + z_2 = z_3 + z_4$
 $\Rightarrow z_3 = 20$

$\tau = \frac{\omega_4 - \Omega}{\omega_1 - \Omega} = \begin{pmatrix} -z_1 \\ z_1 \end{pmatrix} \begin{pmatrix} -z_3 \\ z_3 \end{pmatrix}$

$\omega_1 = 0 \rightarrow \tau = 0,6944$

$\Rightarrow \tau = \frac{\omega_4 - \Omega}{-\Omega} \Rightarrow$

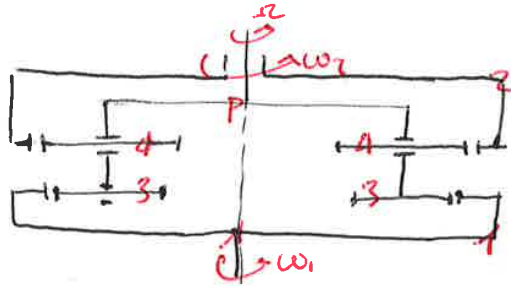
$\Rightarrow \omega_4 = 25,58 \text{ rad/s}$

$C_p = \frac{W}{\Omega} = 95,54 \text{ Nm}$

$C_p \Omega = C_1 \omega_4 \Rightarrow 317,74 \text{ Nm} = C_1 \rightarrow C_1 = C_4 - C_p = 217,2 \text{ Nm}$

5.49

$z_1 = 40$
 $z_3 = 14$
 $z_4 = 18$
 $\Omega = 418,65 \text{ rad/s}$
 $W = 4000 \text{ Nm}$
 $\tau = ?$
 $\omega_2 = ?$ se $\omega_1 = 0$
 $\omega_1 = ?$ se $\omega_2 = 0$
 $C_1 = ?$ $C_2 = ?$



$z_1 - z_3 = z_2 - z_4 \rightarrow z_2 = 40$

$\tau = \frac{\omega_2 - \Omega}{\omega_1 - \Omega} = \begin{pmatrix} z_1 \\ z_1 \end{pmatrix} \begin{pmatrix} z_2 \\ z_2 \end{pmatrix}$

$\tau = 0,145 \Rightarrow 1,1688$

~~se $\omega_1 = 0 \rightarrow \omega_2 = 358,71 \text{ rad/s}$~~

~~se $\omega_2 = 0 \rightarrow \omega_1 = -2505,97 \text{ rad/s}$~~

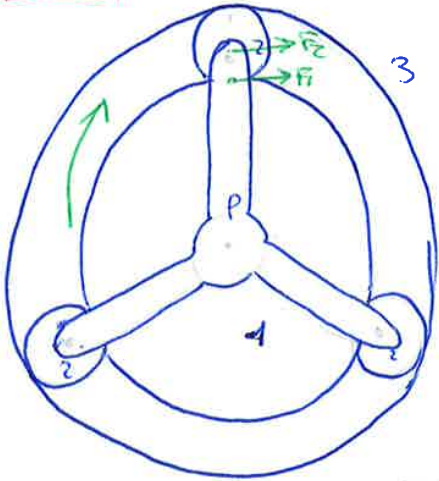
se $\omega_1 = 0 \rightarrow \omega_2 = 47,67$
 $\omega_2 = 70,69 \text{ rad/s}$

se $\omega_2 = 0 \rightarrow \omega_1 = 60,46 \text{ rad/s}$

$C_2 = C_p = \frac{W}{\Omega} = 9,55 \text{ Nm}$

$C_2 \neq C_1 + C_p = 0$

5.561



$r_1 = 14$
 $c_1 = 16 \text{ Nm}$
 $r_2 = 21$
 $w_3 = 0$
 $m = 4 \text{ mm}$
 $T = ? \text{ MP}$
 $F_2 = ?$
 $C_3 = ?$

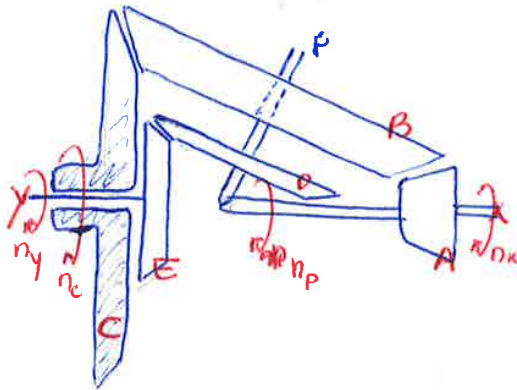
$r_1 = \frac{2m}{2} = 28 \text{ mm}$
 $r_2 = 42 \text{ mm}$
 $r_3 = 112 \text{ mm}$
 $\rightarrow \text{Pr} = 70 \text{ mm}$

$\left(\frac{-r_1}{28} \quad \frac{r_2}{r_3} \right) \cdot T_w = \frac{w_3 - \epsilon}{w_1 - \epsilon} \Rightarrow$
 $\downarrow -0,25 \quad \Rightarrow \frac{\epsilon}{w_1} = \frac{T_w}{T_w - 1} = 0,2$

$C_1 w_1 = C_p \epsilon \rightarrow C_p = 80 \text{ Nm}$
 $F_2 = -\frac{C_p}{r_2} = 380,45 \text{ Nm}$

5.57

$w_c = 0$
 $w_k = 650 \text{ pi}/\text{min}$
 $r_A = 18$
 $r_B = 55$
 $r_C = 60$
 $r_D = 24$
 $r_E = 28$
 $n_y = ?$



$T_{w1} = \frac{n_c - n_p}{n_a - n_p} = \frac{r_A}{r_B} \cdot \frac{r_D}{r_E} = -0,3$

$t_{w_nA} - t_{w_nP} = -n_p \rightarrow$
 $\rightarrow n_p = \frac{t_{w_nA}}{(t_w - 1)} = 150 \text{ rpm/omega}$

$t_{w1} = \frac{n_y - n_p}{n_x - n_p} = \left(-\frac{r_A}{r_B} \right) \left(\frac{r_D}{r_E} \right) = -0,2805$

$t_{w_nX} - t_{w_nP} + n_p = n_y = -1,75 \text{ rpm/omega}$

$n_p = \frac{t_{w1}}{t_{w1} - 1} n_x \quad n_y = (1 - t_{w2}) n_p + t_{w2} n_x \rightarrow n_y = \left(\frac{t_{w1}}{t_{w1} - 1} - \frac{t_{w2} t_{w1}}{t_{w1} - 1} + t_{w2} \right) n_x$
 $= \frac{(t_{w1} - t_{w2} t_{w1} + t_{w1} t_{w2} - t_{w2})}{t_{w1} - 1} n_x \rightarrow n_y = \frac{t_{w1} - t_{w2}}{t_{w1} - 1} n_x$

per far sì che n_y sia in senso opposto a $n_x \rightarrow n_y < 0 \rightarrow t_{w1} - t_{w2} > 0$

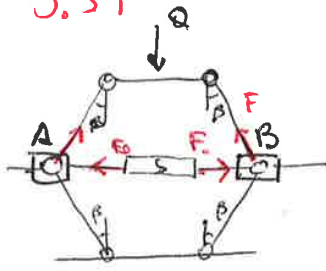
$\Rightarrow -\frac{r_A}{r_C} + \left(\frac{r_A}{r_B} \cdot \frac{r_D}{r_E} \right) > 0 \rightarrow \frac{r_A}{r_C} > -\frac{r_A r_D}{r_B r_E} \rightarrow r_C > -\frac{r_C r_D}{r_B} \rightarrow r_C > \frac{r_C r_D}{r_B}$

$\Rightarrow r_C < 26,18 \rightarrow \text{MP } r_E = 26 \rightarrow \Delta r_E = r_D - r_E = 2$

$\bar{t}_1 = \left(\frac{r_A}{r_B} \cdot \frac{r_D}{r_E} \right) = -0,30209 \rightarrow n_y = \frac{t_{w1} - t_{w2}}{t_{w1} - 1} = 1,0489 \text{ rpm/omega}$

$$F = P / \cos(\alpha + \varphi) \quad \left. \begin{array}{l} \\ C = \mu F \sin(\alpha + \varphi) \end{array} \right\} \rightarrow C = \frac{P \mu \sin(\alpha + \varphi)}{\cos(\varphi + \alpha)} \rightarrow F \tan(\alpha + \varphi) \quad \text{etc!}$$

5.59



Q = 10000 N
 P = 4 mm
 d = 19 mm
 f = 0,15
 β = 35°
 C_s = ?
 17,35%

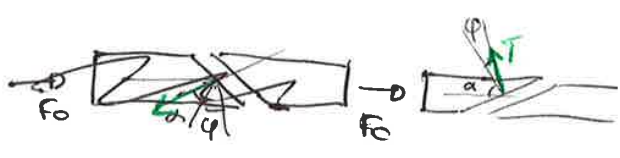
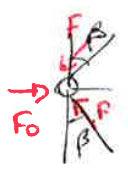
$$Q - 2F \cos \beta = 0 \rightarrow F = 6103,87 \text{ N}$$

$$F_{co} = 2F \sin \beta = 0 \rightarrow f_{co} = 2F \sin \beta = 7002,1 \text{ N}$$

$$C = 2f_{co} \frac{d}{2} \tan(\alpha + \varphi) = 1458 \text{ N} \approx 29,16 \text{ Nm}$$

$$\arctan f = \varphi = 8,531^\circ$$

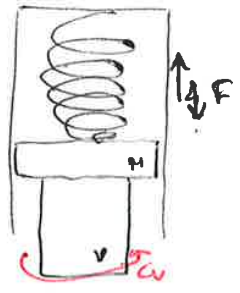
$$\alpha = \arctan\left(\frac{P}{d}\right) = 3,834^\circ$$



$$F = P \tan(\alpha + \varphi)$$

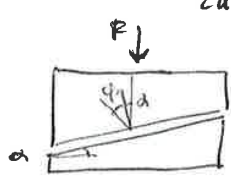
5.61

k = 8 · 10³ N/m
 d = 18 mm
 p = 7 mm
 f = 0,16
 F = 140 N, n = ?
 C_v = ?
 C_{scorico}



$$F = k \Delta x \rightarrow \Delta x = 0,0175 \text{ m} \rightarrow h = 0,3095 \cdot 2\pi$$

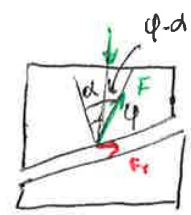
$$2\pi r = 0,0565 \text{ m}$$



$$\alpha = \arctan \frac{p}{d} = 7,056^\circ$$

$$\varphi = \arctan(f) = 9,09^\circ$$

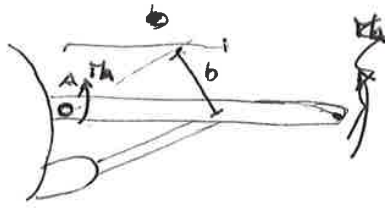
$$C_v = P \frac{d}{2} \tan(\alpha + \varphi) = 0,365 \text{ Nm}$$



$$C_{scorico} = P \frac{d}{2} \tan(\varphi - \alpha) = 0,0447 \text{ Nm}$$

$$F_r = F \tan(\varphi - \alpha)$$

5.68

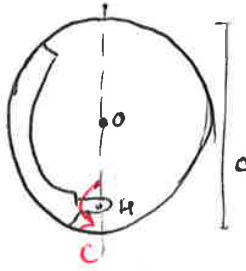


$p = 10 \text{ MW}$
 $\eta = 0.90$
 $l = 480 \text{ mm}$
 $t = 6 \text{ s}, v = \omega r t$
 $\eta_r = 0.92$
 $C_H = 20 \text{ Nm}$
 $b = 1.25 \text{ m}$
 $M_H = 2000 \text{ Nm}$
 $\tau = ?$
 $W_H = ?$
 $W = ?$

$v = \frac{p}{c} = 0.08 \text{ m/s}$
 $v = \omega r \rightarrow \omega = \frac{v}{r} = 50.265 \text{ rad/s}$
 $\rightarrow \tau = \frac{M_H}{\omega} = 0.00159 \text{ ?}$
 $F = \frac{M_H}{b} = 1600 \text{ N}$
 $E_{WH} = \frac{Fv}{\eta_r} = 1595.1 \text{ W}$
 $\rightarrow W_H = 77.29 \text{ rad/s}$
 $\rightarrow \tau = \frac{W}{W_H} = 0.6503$

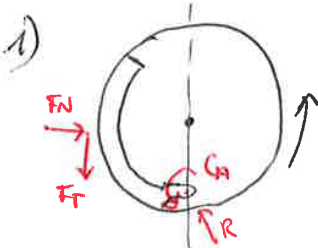
FRENI

8.69



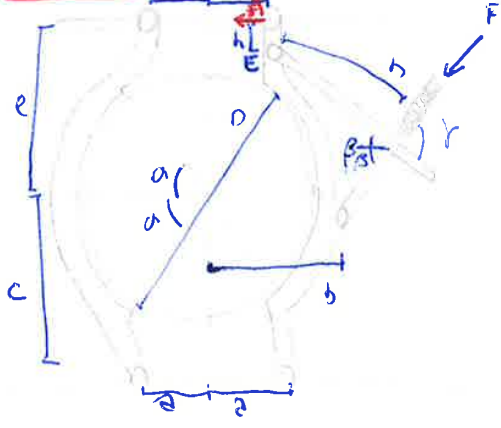
$d = 0.6 \text{ m}$
 $OH = 0.2 \text{ m}$
 $f = 0.25$
 $C_G = ?$
 $C_A = ?$
 $M_f = 2000 \text{ Nm}$

$C = f \frac{h}{b - f} \left(\frac{F d}{2} \right)$
 $h = 2OH$



$M_f = F_T \frac{d}{2} \rightarrow F_T = \frac{6666.67}{0.3} = 22222.22 \text{ N} \rightarrow F_N = 26666.67 \text{ N}$
 $A) \uparrow C_A - F_N OH + F_T \frac{d}{2} = 0 \rightarrow C_A = 3333.33 \text{ Nm}$
 $A) \downarrow C_A + F_N OH + F_T \frac{d}{2} = 0 \rightarrow C_G = 7333.33 \text{ Nm}$

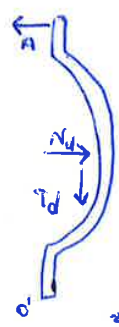
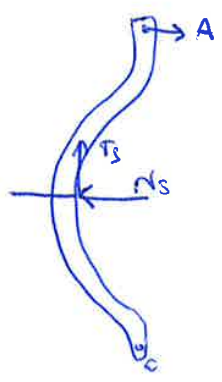
5.77



$f = 0,3$
 $a = 114 \text{ mm}$
 $b = 0,3 \text{ m}$
 $c = 0,228 \text{ m}$
 $D = 0,38 \text{ m}$
 $e = 0,13 \text{ m}$
 $h = 0,076 \text{ m}$
 $\alpha = 45^\circ$
 $\beta = 30^\circ$
 $\gamma = 40^\circ$
 $F = 7 \text{ kN} = 7000 \text{ N}$
 verso orario

~~$F_b \cos \beta + F_b \sin \beta - Ah = 0$~~
 $F_b \cos \beta + F_b \sin \beta - Ah = 0$
 $A = F \sin \beta$

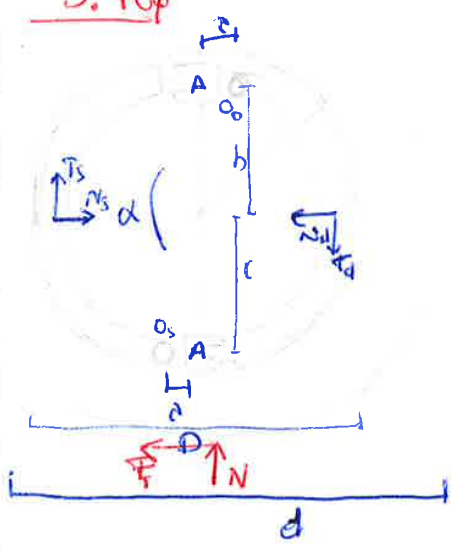
$\circlearrowleft \sum T_s (D_2 - a) - N_s c + A(e + d) = 0 \rightarrow T_s (D_2 - a - c/f) = -A(e + d)$
 $\frac{T_s}{f} = N_s$



$\circlearrowleft \sum T_d (D_2 - a) + N_d c - A(e + c) = 0 \rightarrow$
 $\rightarrow T_d = f N_d$
 $\Rightarrow T_d (D_2 - a + c/f) = A(e + c)$
 $M = (T_d + T_s) D_2 \Rightarrow$
 $\Rightarrow \left[\frac{A(e + c)}{(D_2 - a + c/f)} - \frac{A(e + d)}{(D_2 - a - c/f)} \right] D_2$

$M = \frac{A}{h} (e + c) F D_2 \left[\frac{1}{(D_2 - a + c/f)} - \frac{1}{(D_2 - a - c/f)} \right]$
 $\Rightarrow 0,898 M = F \rightarrow F = 305,42 \text{ N}$

5.78



$d = 0,66 \text{ m}$
 $N = 2000 \text{ N}$
 $f_r = 0,75$
 $\alpha = 0,025 \text{ m}$
 $D = 0,228 \text{ m}$
 $f = 0,3$
 $a = 0,038 \text{ m}$
 $b = 0,086 \text{ m}$
 $c = 0,082 \text{ m}$
 $\alpha = 90^\circ$
 $P_a = ?$
 $P_b = ?$

ANTI ORARIO

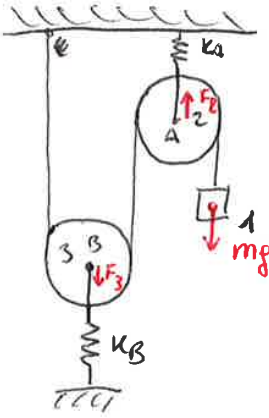
$\sum M: \circlearrowleft$
 $\circlearrowleft \sum P A (b + c) + N_s c - T_s (D_2 - a) = 0$
 $\frac{T_s}{f} = N$
 $\Rightarrow T_s (D_2 - a - c/f) = P A (b + c)$

$\circlearrowright \sum P A (b + c) + N_d (b) + T_d (D_2 - a) = 0$
 $\frac{T_d}{f} = N$
 $\Rightarrow T_d (D_2 - a + b/f) = -P A (b + c)$

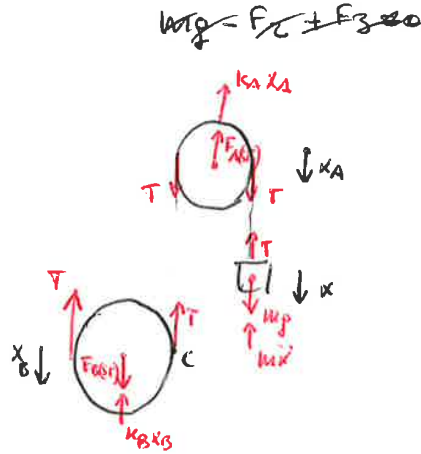
$M = (T_d + T_s) D_2 = -P_r f N \frac{d}{c}$
 $\left[\frac{P A (b + c)}{(D_2 - a - c/f)} - \frac{P A (b + c)}{(D_2 - a + b/f)} \right] D_2 = -495 \rightarrow P = 242 \text{ MPa}$
 $P = 5,309 \text{ MPa}$

orario

VI BRACCIONI LIBERE [6.1]



$m = 10 \text{ kg}$
 $k_A = 1000 \text{ N/m}$
 $k_B = 700 \text{ N/m}$
 $\omega_n = ?$



$k_C = 2 \times k_B$
 $k_A = \frac{k_C + k}{2}$

$$\begin{cases} T + m\ddot{x} = 0 \\ 2T - k_A x_A = 0 \Rightarrow k_A = \frac{2T}{x_A} \\ 2T + k_B x_B = 0 \Rightarrow k_B = \frac{-2T}{x_B} \end{cases}$$

$$\frac{2T}{k_A} = \frac{-4T}{k_B} + x$$

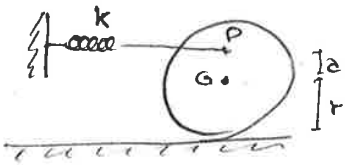
$$\Rightarrow k = \frac{4T}{k_A} + \frac{4T}{k_B}$$

$$\Rightarrow T = x \cdot \left(\frac{4}{k_A} + \frac{4}{k_B} \right)^{-1}$$

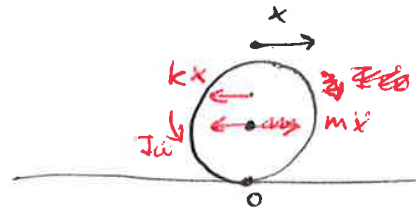
$$\Rightarrow \frac{x}{\frac{4}{k_A} + \frac{4}{k_B}} + m\ddot{x} = 0 \Rightarrow x + \frac{4(k_A + k_B)}{k_A k_B} m \ddot{x} = 0$$

$$4 \frac{k_A + k_B}{k_A k_B} = \frac{1}{\omega_n^2} \Rightarrow \omega_n = \sqrt{\frac{1}{4m \left(\frac{k_A + k_B}{k_A k_B} \right)}} = 3,208 \text{ rad/s}$$

6.2



$I = 0,5 \text{ kg m}^2$
 $m = 20 \text{ kg}$
 $k = 500 \text{ N/m}$
 $r = 0,2 \text{ m}$
 $a = 0,1 \text{ m}$
 $f_n = ? = 2\pi \omega_n$



$\dot{\omega} = \ddot{x} r$

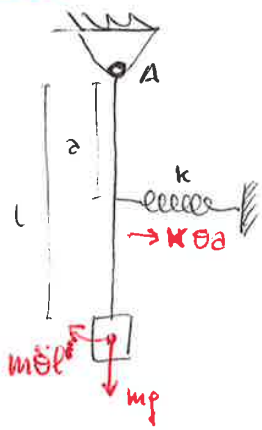
$$0 = I \ddot{\omega} + m \ddot{x} - kx(a+r) \rightarrow \left(\frac{I}{r} + \frac{m}{k} \right) \ddot{x} - kx = 0 \rightarrow \left(\frac{I}{r} + \frac{m}{k} \right) \ddot{x} - kx = 0$$

$$\left(\frac{I}{r} + \frac{m}{k} \right) = \frac{1}{\omega_n^2} \Rightarrow \omega_n = \sqrt{\frac{1}{\frac{I}{rk} + \frac{m}{k}}}$$

$$\frac{I}{r} \ddot{x} + m \ddot{x} - k(a+r)x \rightarrow \left(\frac{I}{r} + m \right) \ddot{x} = k(a+r)x \Rightarrow \omega_n = \sqrt{\frac{k(a+r)}{\frac{I}{r} + m}} = 9,804 \text{ rad/s}$$

$m\ddot{x} + \frac{k \cdot \Delta s}{r} (r+a) + 20\ddot{x} = 0 \rightarrow \omega_n = \sqrt{\frac{k(r+a)^2}{mr^2 + I_0}} = 5,88 \text{ rad/s} \rightarrow f = 0,936 \text{ Hz}$

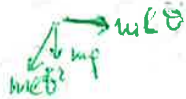
6.5



$T_s = ?$
 $m = 100 \text{ kg}$
 $k = 130 \text{ N/m}$
 $a = 0.2 \text{ m}$
 $l = 1 \text{ m}$

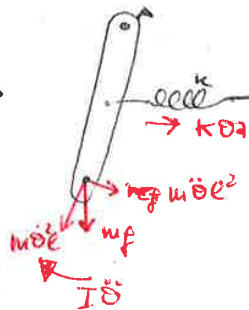
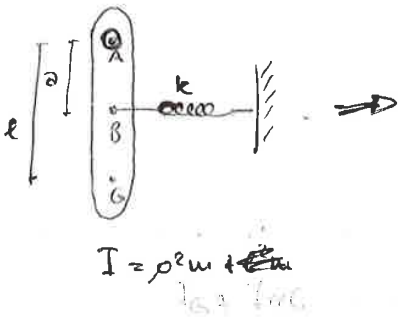
~~$m \ddot{\theta} l^2 - k a^2 \theta = 0 \rightarrow$~~
 ~~$\rightarrow \frac{m l^2}{k a^2} \ddot{\theta} = \theta \rightarrow \omega_n = \frac{1}{\sqrt{\frac{m l^2}{k a^2}}} = 0.228 \text{ rad/s}$~~
 ~~$T_s = \frac{2\pi}{\omega_n} = 27.55 \text{ s}$~~

A) $m \ddot{\theta} l^2 + k a^2 \theta + m g l \theta = 0$
 $m l^2 \ddot{\theta} + (k a^2 + m g l) \theta = 0 \rightarrow$
 $\rightarrow \frac{1}{\omega_n} = \sqrt{\frac{m l^2}{k a^2 + m g l}} = 3.14 \text{ rad/s}$
 $\Rightarrow T_s = \frac{2\pi}{\omega_n} = 2 \text{ s}$



6.6

$m = 3 \text{ kg}$
 $\rho_G = 20.2 \text{ cm}$
 $k = 200 \text{ N/m}$
 $a = 0.5 \text{ m}$
 $l = 1 \text{ m}$
 $f = ?$

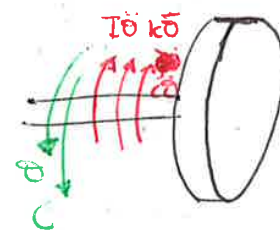
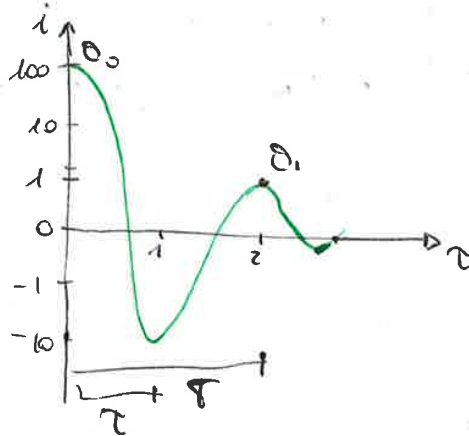


of ω_n
 $k a^2 \theta + m \ddot{\theta} l^2 + m g \rho_G \theta - I \ddot{\theta} = 0$
 $(m l^2 + I) \ddot{\theta} + \theta (k a^2 + m g \rho_G) = 0$
 $\frac{1}{\omega_n} = \sqrt{\frac{m l^2 + I}{k a^2 + m g \rho_G}} = \frac{5.045 \text{ rad/s}}{25.72 \text{ rad/s}}$
 ~~$f = \frac{\omega_n}{2\pi} = 16.62 \text{ Hz}$~~
 $f = \frac{\omega_n}{2\pi} = 0.803 \text{ Hz}$

Hp: piccoli oscillazioni $\sin \theta \approx \theta$

6.7

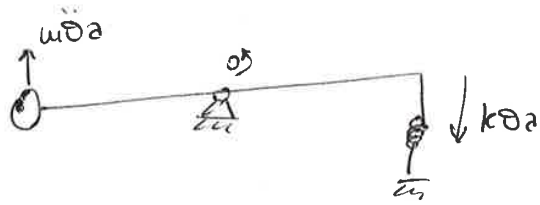
$\ddot{x} + \dots$
 $\ddot{x} = -10$
 $\theta_0 = 40^\circ = i$
 $C = 1.2746 \text{ Nm}$
 $\dot{x}' = -10$
 $\dot{x}'' = +1$
 $\Delta t = 4 \text{ s}$
 $\tau = 25$
 $\zeta = ?$
 $T_0 = ?$ o $\zeta = ?$
 $I = ?$



$I \ddot{\theta} + k \theta + c \dot{\theta} = 0$
 $\theta(t) = \theta_0 e^{-\zeta \omega_n t} \cos(\omega_n \sqrt{1 - \zeta^2} t)$
 $\delta = l u \frac{\theta_1}{\theta_0} = l u \frac{1}{100} = -4.605$
 $\delta = -\frac{2\pi \zeta f}{\sqrt{1 - \zeta^2}} \rightarrow \zeta = \sqrt{\frac{\delta^2}{4\pi^2 + \delta^2}} = 0.591$
 $T = 4 \text{ s} = \frac{2\pi}{\omega_n \sqrt{1 - \zeta^2}} \rightarrow \omega_n = 1.947 \text{ rad/s}$

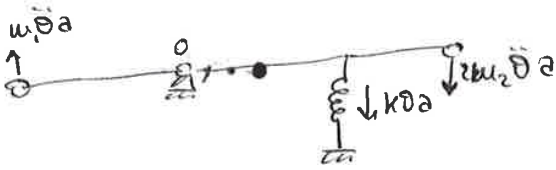
$k = \frac{C}{\theta_0} = 1.826 \cdot 10^6 \text{ Nm/rad}$

del confronto con l'equazione ^{del moto} $\ddot{x} + \dots$ e pu' in forma canonica no $\omega_n = \sqrt{\frac{k}{I}} \rightarrow I = 0.482 \cdot 10^6 \text{ kg m}^2$



$$\mathcal{O} : u_1 \ddot{\theta} + k l \theta = 0$$

$$\frac{u_1}{k} \ddot{\theta} + \theta = 0 \rightarrow \omega_n = \sqrt{\frac{k}{u_1}}$$



$$\mathcal{O} : u_1 \ddot{\theta} + k l \theta + c m_2 \ddot{\theta} = 0$$

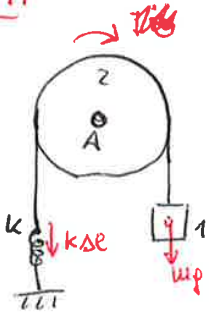
$$\omega_n = \sqrt{\frac{k}{u_1 + c m_2}} = \frac{1}{2} \sqrt{\frac{k}{u_1}}$$

$$\frac{c k}{u_1 + c m_2} = \frac{k}{u_1} \rightarrow c m_1 = u_1 + c m_2$$

$$\rightarrow 3 m_1 = 4 m_2 \rightarrow c = \frac{3}{4} l$$

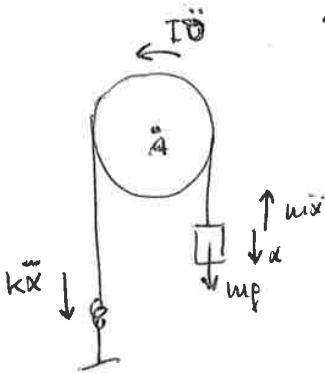
Foto 111.

6.91



$m_A = 0,8 \text{ kg}$
 $m_B = 2 \text{ kg}$
 $d = 0,1 \text{ m}$
 $\rho = 0,04 \text{ m}$
 $k = 5000 \text{ N/m}$
 $T_s = ?$
 $\Delta l_{st} = ?$

STATICO: $k \Delta l_{st} = m_B g \rightarrow \Delta l_{st} = 1,57 \text{ mm}$



$$\mathcal{A} : k x \frac{d}{2} + m \ddot{x} \frac{d}{2} + M \rho^2 \ddot{\theta} \rightarrow k r^2 \ddot{\theta} + u r^2 \ddot{\theta} + M \rho^2 \ddot{\theta} = 0$$

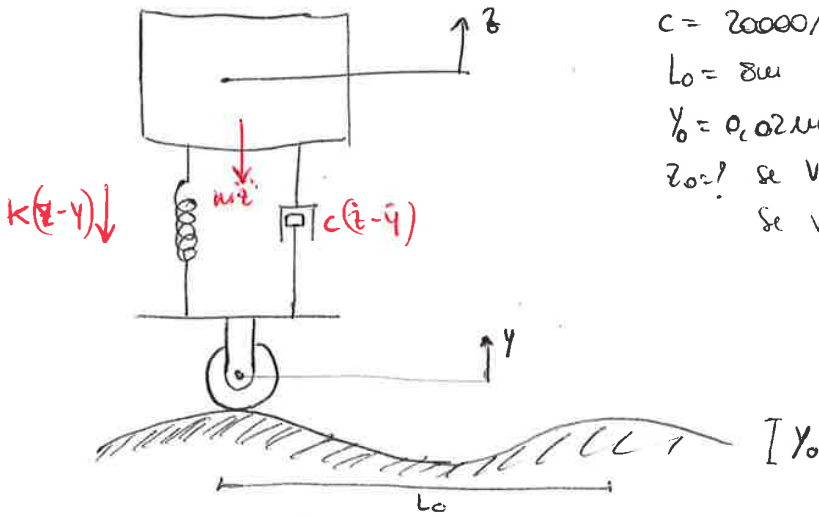
$$\frac{d}{2} \ddot{\theta} = \ddot{x}$$

$$(u r^2 + M \rho^2) \ddot{\theta} + k r^2 \ddot{\theta} = 0$$

$$\rightarrow \omega_n = \sqrt{\frac{k r^2}{u r^2 + M \rho^2}} = 49 \text{ rad/s}$$

$$T = 0,128 \text{ s}$$

6.12



$m = 1000 \text{ kg}$
 $k = 300000 \text{ N/m}$
 $c = 20000 \text{ Ns/m}$
 $L_0 = 8 \text{ m}$
 $y_0 = 0,02 \text{ m}$
 $z_0 = ?$ se $v = 70 \text{ km/h} = 19,44 \text{ m/s} \rightarrow \omega =$
 $\text{se } v = 120 \text{ km/h} = 33,33 \text{ m/s}$
 $\omega_n = \sqrt{\frac{k}{m}} = 17,32 \text{ rad/s}$
 $C = 2\zeta \sqrt{km} \rightarrow \zeta = 0,577$

$kz + c\dot{z} + m\ddot{z} = ky + c\dot{y}$

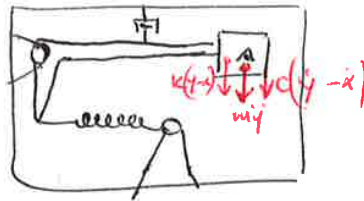
$\frac{z_0}{y_0} = \frac{\sqrt{1 + \frac{4\zeta^2 \omega^2}{\omega_n^2}}}{\sqrt{\left(1 - \left(\frac{\omega}{\omega_n}\right)^2\right)^2 + 4\zeta^2 \left(\frac{\omega}{\omega_n}\right)^2}}$

$f [\text{Hz}] = \frac{v}{L_0} \rightarrow \omega = 2\pi f =$
 $\text{se } v = 19,44 \text{ m/s} \rightarrow \omega_1 = 15,27 \text{ rad/s}$
 $\omega_2 = 26,177 \text{ rad/s}$

$\Rightarrow z_1 = 0,005 \text{ m}$
 $z_2 = 12,04 \frac{y_0 \omega_2}{\omega_n^2} = 0,01858 \text{ m}$

6.13

$f_n = 3 \text{ Hz}$
 $\zeta = 0,5$
 $\omega_n = 18,84 \text{ rad/s}$
 $z_0 = 0,0025 \text{ m}$
 $k_0 = ?$
 $\omega = 180 \text{ rpm/min} = 3 \text{ rad/s} \rightarrow 56,55 \text{ rad/s}$



$\omega = 2\pi f \quad \omega_n = 2\pi f_n = 18,84 \text{ rad/s}$
 $z = y - x$
 $\ddot{z} = \ddot{y} - \ddot{x}$

$m\ddot{z} + c(\dot{y} - \dot{x}) + k(y - x) = 0$

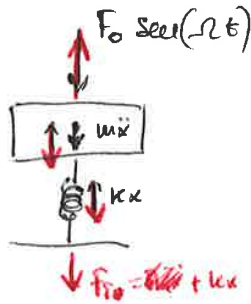
$\frac{m}{k} \ddot{z} + \frac{m\zeta}{k} \dot{z} + z = 0$
 $\frac{1}{\omega_n^2} \ddot{z} + \frac{2\zeta}{\omega_n} \dot{z} + z = 0$

$\frac{\ddot{z}}{\omega_n^2} + \frac{2\zeta}{\omega_n} \dot{z} + z = -\frac{m}{k} \ddot{x}$
 $\frac{\ddot{z}}{\omega_n^2} + \frac{2\zeta}{\omega_n} \dot{z} + z = -\frac{\omega^2}{\omega_n^2} z_0 \cos(\omega t)$

$-\frac{\omega^2}{\omega_n^2} z_0 \cos(\omega t) + \left(\frac{2\zeta}{\omega_n} \omega z_0\right) \sin(\omega t) + z_0 \cos(\omega t) = \frac{\omega^2}{\omega_n^2} z_0 \cos(\omega t)$

6.15

$m = 9000 \text{ kg}$
 $F_0 = 20000 \text{ N}$
 $f_0 = 14 \text{ Hz}$
 $\beta = 0$
 $k = ?$ \ ~~$k = 20000 \text{ N}$~~
 $F_{T0} = 20000 \text{ N} =$



$$F_0 \sin(\Omega t) = m\ddot{x} + kx \rightarrow$$

$$\rightarrow \frac{F_0}{k} \sin(\Omega t) = \frac{m}{k} \ddot{x} + x \rightarrow$$

$\downarrow \frac{1}{\omega_n^2}$

~~$x = X_0 \cos(\Omega t) + A$~~
 ~~$\ddot{x} = -\Omega^2 \cos(\Omega t)$~~

$F_T = kx + m\ddot{x} \rightarrow$
 $\Rightarrow F_T = kx = k X_0 \sin(\Omega t) = F_{T0} \sin(\Omega t) \rightarrow \frac{F_{T0}}{F_0} =$

$$\frac{F_{T0}}{F_0} = \frac{1}{\left| 1 - \frac{\Omega^2}{\omega_n^2} \right|}$$

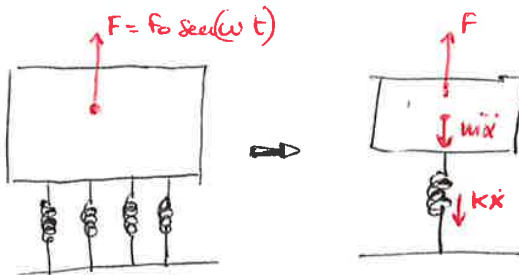
Ma si richiede $F_{T0}/F_0 < 1 \rightarrow \Omega > \sqrt{2} \omega_n$

$$\Rightarrow \frac{F_{T0}}{F_0} = \frac{1}{\frac{\Omega^2}{\omega_n^2} - 1} \Rightarrow \omega_n = 358,87 \text{ rad/s}$$

$$\Rightarrow k = \omega_n^2 m = 322983 \text{ N/m}$$

6.16

$m = 180 \text{ kg}$
 4 molle
 $F_0 = 310 \text{ N}$
 $n_1 = 900 \text{ giri/min}$
 $F_0 = 310 \text{ N}$



$$F_0 \sin(\omega t) = kx + m\ddot{x}$$

$$\frac{F_0 \sin(\omega t)}{k} = x + \frac{m}{k} \ddot{x} \rightarrow \frac{1}{\omega_n^2}$$

$F_{T0} = 22 \text{ N} \rightarrow k = ?$
 $A = ?$ se $n = 600 \text{ giri/min}$

$n_1 = 900 \text{ giri/min} \rightarrow \omega = 94,2 \text{ rad/s}$

$F_T = kx = F_{T0} \sin(\omega t)$
 \downarrow
 kx_0

$$\frac{F_{T0}}{F_0} = \frac{1}{\left| 1 - \frac{\omega^2}{\omega_n^2} \right|} \quad \text{Ma } F_{T0}/F_0 < 1 \rightarrow \omega > \sqrt{2} \omega_n$$

$$\Rightarrow \frac{F_{T0}}{F_0} = \frac{1}{\left(\frac{\omega^2}{\omega_n^2} - 1 \right)} \Rightarrow \frac{\omega^2}{\omega_n^2} - 1 = 1/0,071$$

$$F_0' = F_0 \frac{\omega_n^2}{\omega^2} = 137,78 \text{ N}$$

$$\omega^2 = (14,09 + 1) \omega_n^2$$

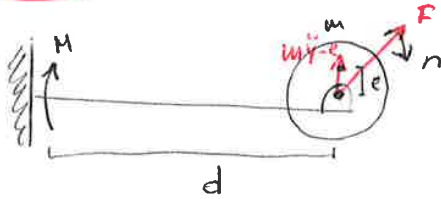
$$\Rightarrow \omega_n = 24,25 \text{ rad/s}$$

$$\Rightarrow \omega_n = \sqrt{\frac{k}{m}} \rightarrow k =$$

$$\Rightarrow k = 105842,2 \text{ N/m}$$

$$\Rightarrow A = \frac{F_0' / k}{\left(\frac{\omega}{\omega_n} \right)^2 - 1} = \frac{90015}{5,706} = 9000,28 \text{ m}$$

6.18



$k = 1940 \text{ N/mm} \rightarrow 1.94 \cdot 10^6 \text{ N/m}$

$m = 160 \text{ kg}$

$e = 0.0025 \text{ m}$

$d = 0.203 \text{ m}$

$A = ?$

$H = ?$

$n = 1000 \text{ rpm/min}$

$F_0 = m \omega^2 e = 4386.5 \text{ N}$

$F = F_0 \sin(\omega t)$

$\omega = \frac{2\pi n}{60} = 104.72 \text{ rad/s}$

$\frac{F_0 \sin(\omega t)}{k} = \frac{m \ddot{y}}{k} + y \rightarrow \omega_n = 110.13 \text{ rad/s} > \omega \rightarrow A = \frac{(F_0/k)}{\left(\frac{\omega_n^2}{\omega^2} - 1\right)} = 0.0219 \text{ m}$

$H_{\text{max}} = k y d = 877.748 + 291.72 \text{ Nm}$

6.19

$h = 0.00086 \text{ m}$

$f_r = ?$

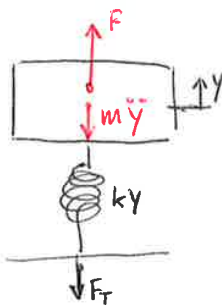
$m = 1200 \text{ kg}$

$n = 450 \text{ rpm/min} \rightarrow 47.1 \text{ rad/s}$

$F_0 = 2300 \text{ N}$

$y_0 = ?$

$F_{T0} = ?$



iniziale levante $mp = kh \rightarrow k = 1.367 \cdot 10^7 \text{ N/m}$

$\Rightarrow \omega_n = \sqrt{\frac{k}{m}} = 106.75 \text{ rad/s} \rightarrow f_0 = 17 \text{ Hz}$

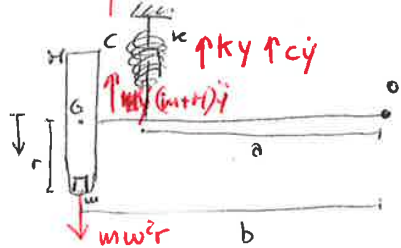
Forces $\frac{F_0 \sin(\omega t)}{k} = \frac{m \ddot{y}}{k} + y$

$H_p = \dot{y} = 0 ; \omega_n > \omega \rightarrow$

$\Rightarrow y_0 = \frac{(F_0/k)}{\left(1 - \left(\frac{\omega}{\omega_n}\right)^2\right)} = 0.2089 \text{ mm}$

$F_{T0} = k \cdot y_0 = 2856 \text{ N}$

6.20



$M = 45 \text{ kg}$

$I_G = 1.4 \text{ kgm}^2$

$k = 8750 \text{ N/m}$

$c = 2600 \text{ N/m}$

$m = 0.25 \text{ kg}$

$r = 0.35 \text{ m}$

$a = 0.6 \text{ m}$

$b = 0.8 \text{ m}$

$\omega_n = ?$

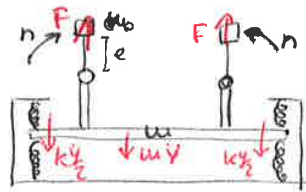
$F = ?$

$y_0 = ?$

$\frac{(I_G + M b^2) \ddot{\theta}}{k a} + \frac{c \ddot{\theta}}{k a} + k a \ddot{\theta} = 0$
 $\Rightarrow \omega_n = 10.13 \text{ rad/s}$

6.23

$m_0 = 1 \text{ kg}$
 $e = 0.012 \text{ m}$
 $k = ? \setminus F_{T0} = 1500 \text{ N} \setminus \omega = 188.4 \text{ rad/s}$
 $m = 10 \text{ kg}$
 $\xi = 0$



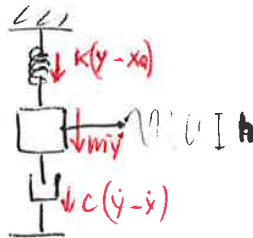
$F = F_0 \sin(\omega t)$
 $F_0 = 2 m \omega^2 e = 851.87 \text{ N}$
 $\frac{F}{k} = \frac{m \ddot{y}}{k} + y$

$\frac{F_{T0}}{F_0} = \frac{1}{|1 - (\frac{\omega}{\omega_n})^2|} \rightarrow \frac{F_0}{F_{T0}} = 0.568 = |1 - \frac{\omega}{\omega_n}| \Rightarrow$
 $\rightarrow \omega_n > \omega \rightarrow 0.568 = 1 - \frac{\omega}{\omega_n} \rightarrow \omega_n = \frac{\omega}{0.432} = 436.02 \text{ rad/s}$
 $\Rightarrow Dk = 1.901 \cdot 10^6 \text{ N/m}$
 $\rightarrow \omega_n < \omega \rightarrow 0.568 = \frac{\omega}{\omega_n} - 1 \rightarrow \omega_n = \frac{\omega}{1.568} = 120.15 \text{ rad/s}$
 $\Rightarrow Dk = 1.44 \cdot 10^5 \text{ N/m}$

$\frac{F_{T0}}{F_0} = \frac{1}{|1 - (\frac{\omega}{\omega_n})^2|} \rightarrow e = \frac{1}{F_{T0}/F_0} = 0.568 = |1 - (\frac{\omega}{\omega_n})^2|$
 $\omega_n > \omega \rightarrow 0.568 = 1 - (\frac{\omega}{\omega_n})^2 \rightarrow \omega_n = \frac{\omega}{0.432} = 286.6 \text{ rad/s} \rightarrow Dk = 8.216 \cdot 10^5 \text{ N/m}$
 $\omega_n < \omega \rightarrow 0.568 + 1 = (\frac{\omega}{\omega_n})^2 \rightarrow \omega_n = \frac{\omega}{1.568} = 150.45 \text{ rad/s} \rightarrow Dk = 7.26 \cdot 10^5 \text{ N/m}$

6.24

$f_0 = 5 \text{ Hz} \rightarrow \omega = 31.4 \text{ rad/s}$
 $x_0 = 0.009 \text{ m}$
 $m = 2 \text{ kg}$
 $k = 1.5 \cdot 10^3 \text{ N/m}$
 $h = 0.024 \text{ m}$
 $c = ? \quad h = 2\gamma_0$



$F \cos t$
 $k y + m \ddot{y} + c \dot{y} = c \dot{x} + k x$
 $y + \frac{c}{k} \dot{y} + \frac{m}{k} \ddot{y} = \frac{c}{k} \dot{x} + x$
 $\frac{1}{\omega_n} \rightarrow \omega = 27.35 \text{ rad/s}$

$x = x_0 \sin(\omega t)$
 $\dot{x} = \omega x_0 \cos(\omega t)$
 $\ddot{x} = -\omega^2 x_0 \sin(\omega t)$
 $y = y_0 \sin(\omega t + \phi)$
 $\dot{y} = \omega y_0 \cos(\omega t + \phi)$
 $\ddot{y} = -\omega^2 y_0 \sin(\omega t + \phi)$

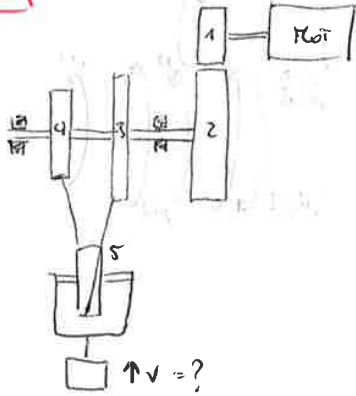
$\Rightarrow y + \frac{2\gamma}{\omega_n} \dot{y} + \frac{y}{\omega_n^2} = \frac{2\gamma}{\omega_n} \dot{x} + x$

$y_0 \sin(\omega t + \phi) + \frac{2\gamma}{\omega_n} (-\omega y_0 \cos(\omega t + \phi)) - \frac{\omega^2}{\omega_n^2} y_0 \sin(\omega t + \phi) =$
 $= -\frac{2\gamma}{\omega_n} \omega y_0 \cos(\omega t) + x_0 \sin(\omega t)$

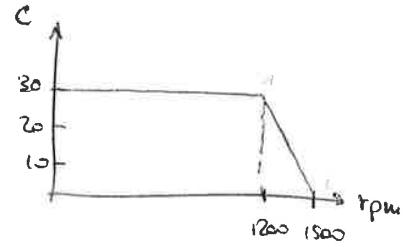
$y_0 \left(1 - \frac{\omega^2}{\omega_n^2} \right) \sin(\omega t + \phi) - \frac{2\gamma \omega}{\omega_n} y_0 \cos(\omega t + \phi) = x_0 \sin(\omega t)$



5.961



- $d_5 = 0,308 \text{ m}$
- $d_4 = 0,3 \text{ m}$
- $z_2 = 61$
- $z_1 = 19$
- $G = 3,5 \text{ Nm}$
- $I_1 = 0,7 \text{ kgm}^2$
- $I_2 = 0,9 \text{ kgm}^2$
- $I_5 \approx 0$
- $d_3 = ?$
- $v = ?$
- $m = ?$
- $a = ?$



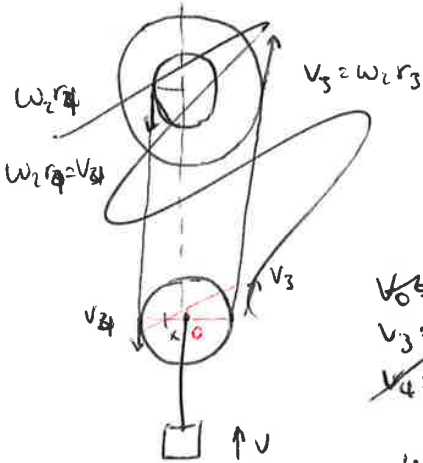
$C_r = 30 \frac{1200}{1400} = 27,14 \text{ Nm}$

$\frac{\omega_1 - \omega_2}{\omega_2 - \omega_3} = \frac{x - x_1}{x_2 - x_1} \Rightarrow$

$\omega = ?$ se $n_r = 1400 \text{ rpm} \rightarrow \omega_r = 146 \text{ rad/s}$

$C_r = 10 \text{ Nm}$

$\tau_{12} = \frac{z_1}{z_2} = 0,311$



$v_3 = \omega_2 r_3 = (r_5 + x) \omega_0$
 $v_4 = \omega_2 r_4 = (r_5 - x) \omega_0$
 $v_0 = \frac{v_4 \times r_3}{r_5} = \frac{v_2 r_3 \times}{r_5}$
 $v_0 = \frac{v_3 \times}{r_5}$

$\omega_0 = \frac{\omega_2 r_3}{r_5 + x} = \frac{\omega_2 r_4}{r_5 - x}$

$v_3 = \omega_2 r_3 =$

$d_5 = r_4 + r_3 \rightarrow r_3 = 0,308 \rightarrow d_3 = 0,316 \text{ m}$

$\omega_2 = \omega_1 \tau = 45,571 \text{ rad/s}$

$v_4 = \omega_2 r_4 = 6,835 \text{ m/s} = \omega_0 (r_5 - x) \rightarrow \omega_0 = v_4 / (r_5 - x)$

$v_3 = \omega_2 r_3 = 7,2 \text{ m/s} = \omega_0 (r_5 + x) \rightarrow v_3 = \frac{v_4}{(r_5 - x)} \cdot (r_5 + x)$

$\Rightarrow v_3 (r_5 - x) = v_4 (r_5 + x) \Rightarrow$

$7,2 \cdot (0,3 - x) = 6,835 \cdot (0,308 + x) \rightarrow x = 0,0041 \text{ m}$

$\rightarrow \omega_0 = 45,589 \text{ rad/s}$

$v_0 = x \omega_0 = 0,187 \text{ m/s}$

$C_1 = C_H - I_1 \omega_1 \omega_0$

$C_2 = \frac{C_1}{\tau_{12}}$

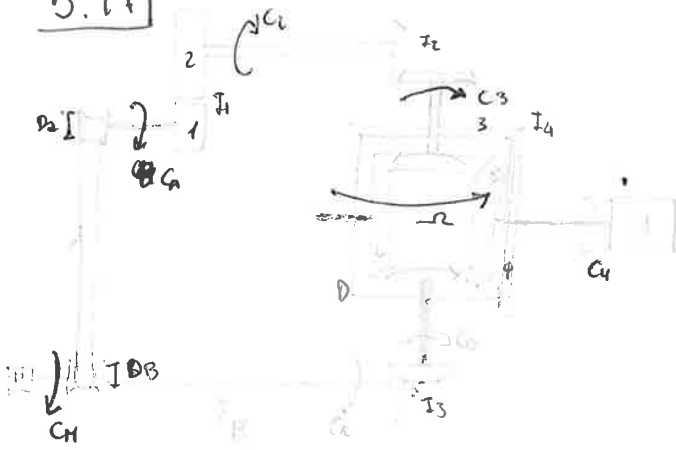
$C_e = C_2 - I_2 \omega_2 \rightarrow F = \frac{C_e}{r_5} = \frac{C_2 - I_2 \omega_2}{r_5}$

$71,43 = C_e = \frac{1}{2} (C_H - I_1 \omega_1 \omega_0) - I_2 \tau \omega_1 \omega_0$ in condizioni di $\omega = \omega_0 + \omega_1 = 0$

$\Rightarrow F = 1073,39 \text{ N} \rightarrow m = 109,96 \text{ kg}$

$F = \frac{C_e}{(r_5 - x)} + \frac{C_e}{(r_5 + x)} = 1074,52 \text{ N} \rightarrow m = 109,65 \text{ kg} \quad m = 94,72 \text{ kg}$

5.97



$$T_1 \begin{cases} z_1 = 15 \\ z_2 = 31 \end{cases} \Rightarrow T_1 = T_2 = 1 \\ T_3 = T_4 = 1$$

$$z_4 = 44, \quad T_4 = 1 \quad \eta = 1 \quad T_D = 1$$

$$z_3 = 21$$

$$C_H = 100 \text{ Nm} \quad C_U = ?$$

$$T_1 = \frac{z_1}{z_2} = 0,4838$$

$$T_2 = 1 \quad \eta = 1 \quad T_{AB} = 1$$

$$T_3 = 1 \quad \eta = 1$$

$$T_4 = 0,9977$$

$$C_H W_B = (C_A W_B + C_B W_B) \rightarrow 2 C_A W_B \rightarrow C_A = C_B = C_H/2$$

$$C_B = C_1 = C_0$$

$$C_A/T_1 = C_2 = C_3$$

$$(C_0 + C_3) = C_4 \rightarrow (C_A/T_1 + C_B)/T_4 = C_4 = C_H \left(\frac{1}{2T_1} + \frac{1}{2} \right) = C_4$$

In condizioni di regime $\omega_1 = \omega_2 = \omega_3 = \omega_4 = \omega$

$$C_3 \omega_3 + C_0 \omega_0 = C_4 \omega_4$$

$$\omega_4 = \tau_4 \omega_1 \quad \tau_4 = \frac{C_0 \omega_0 + \omega_3}{\omega_4} \rightarrow \omega_4 = \tau_4 \frac{\omega_0 + \omega_3}{2}$$

$$C_3 \omega_3 + C_0 \omega_0 = \frac{C_A T_4 \omega_0}{2} + \frac{C_B \omega_3 T_4}{2}$$

$$C_3 \omega_3 + C_0 \omega_0 = \frac{(C_3 + C_0) \tau_4 \omega_0}{2} + \frac{(C_3 + C_0) T_4 \omega_3}{2}$$

$$C_H = C_A + C_B \quad \text{perché } \tau_A = \tau_B \text{ per } \eta = 1$$

$$\frac{C_A}{C_2} = T_1 \rightarrow C_2 = C_A/T_1 = C_3$$

$$C_B = C_1 = C_0$$

$$C_4 = (C_0 + C_3)/T_4 \rightarrow \frac{C_0 + C_3}{C_4} = T_4 \rightarrow \frac{C_A}{T_1} + C_B = C_4$$

$$C_0 = C_1 = C_3$$

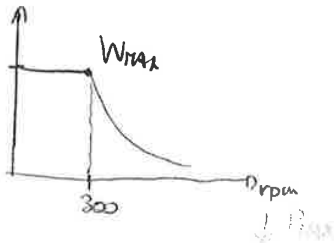
$$C_0 = C_1 + T_1 C_0 = C_A \Rightarrow C_H = (1 + T_1) C_0 \rightarrow C_0 = C_H / (1 + T_1)$$

$$C_B = C_0$$

$$\frac{C_0}{C_4} = \frac{2 C_A}{C_4} = \frac{C_H}{C_4} \Rightarrow \frac{2 C_0}{C_4} = C_H \Rightarrow \frac{2 C_H}{T_4 (1 + T_1)} = 282,57 \text{ Nm}$$

$$C_4 = 120\% C_0 = 339,1 \text{ Nm} \rightarrow C_4 = \frac{2(C_A/T_1 + C_B)}{T_4(1+T_1)}$$

in condizioni di regime le coppie agenti sul rotismo (C_0, C_3) sono uguali $C_0 = C_3 = C_0$



$$W_{max} = G_0 \omega_0 = 1.2 \text{ kW} \rightarrow G_0 = 38,216 \text{ Nm}$$

$$\omega_0 = \omega_H \rightarrow 1.2 \text{ kW} = G_H \omega_H \rightarrow G_H = \frac{G_0}{\frac{\omega_0}{\omega_H}} = \frac{G_0}{2} = 19,108 \text{ Nm}$$

$$G_H = 19,108 \text{ Nm}$$

$$\frac{V_s}{G} = \frac{V_s}{\omega_H} \cdot \frac{\omega_H}{\omega} = \frac{P}{2\pi} \cdot \frac{1}{\omega} \quad \frac{V_s}{\omega_H} = \frac{P}{2\pi}$$

$$\eta = 0,6 = \frac{P V_s}{G_H \omega_H} = \frac{P V_s}{G_H \omega_H} = \frac{P P \omega_H}{G_H \omega_H^2} = 0,6$$

$$\Rightarrow |P| = 206451,69 \text{ N}$$

$$\text{Se } P = P_{max}/2 \quad V_s = \frac{W \eta}{P} = 0,007 \text{ m/s}$$

$$r_1 = \frac{W}{2} \rightarrow r_1 = 0,2425 \text{ m}$$

$$r_2 = 0,0025 \text{ m}$$

$$r_3 = 0,24 \text{ m}$$

$$r_3 = 0,045 \text{ m}$$

$$F_{12} = G_0$$

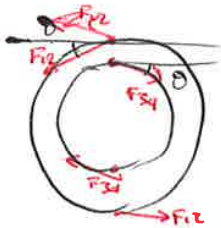
$$F_{34} = \frac{G_H}{2} \cdot \cos \theta = 2144,2 \text{ N}$$

$$\tau_{41} = \frac{r_1}{r_3} = 0,989 \rightarrow \frac{G_H}{G_0} \rightarrow G_0 = 553,33 \text{ Nm}$$

$$F_{34} = \frac{G_H}{2 r_3 \cos \theta} = 1214,11 \text{ N}$$

$$F_{12} = \frac{G_0}{r_1} \cdot \cos \theta = 2144,2 \text{ N}$$

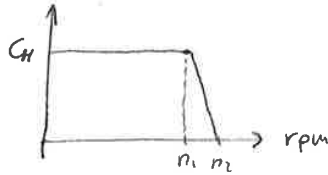
$$F_{12} =$$



$$F_{34} r_3 \cos \theta = F_{12} r_1 \cos \theta \rightarrow F_{12} = 1285,53 \text{ N}$$

5.101

$P_v = 0,005 \text{ MW}$
 $d = 0,055 \text{ m}$
 $\theta = 14,5^\circ$
 $f = 20,11$
 $\beta_2 = 61$
 $\beta_1 = 19$



$\eta_R = 0,97$
 $\eta_1 = 0,98$
 $n_1 = 2400 \text{ rpm}$

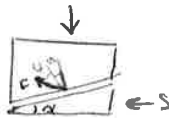
$\omega_H = v \cdot \frac{2\pi}{P_v} = 31,4 \text{ rad/s}$

$n_2 = 2800 \text{ rpm}$
 $m = 2000 \text{ kg}$
 $v = 0,025 \text{ m/s}$

$\alpha = \arctan \frac{P_v}{\pi d}$

$\alpha = \arctan \frac{P_v}{\pi d} = 1,657^\circ$

$\varphi = \arctan \frac{f}{\cos \theta} = 6,277 \cdot 6,482$



$Q = mg$

$C_v = \arctan(\alpha + \varphi) = 76,71 \text{ Nm}$

$W = \omega_H C_v = 24121,97 \text{ W}$

$C_H = C_v \cdot \eta_1$

$T_R = ?$
 $C_H = ?$
 $W_{MAX} = ?$

$\omega_H = 293,06 \text{ rad/s}$

$T_R = \frac{C_H}{\omega_H} = 0,337$

$T = \frac{P_v}{\omega_H} = 0,311$

$C_2 \omega_2 = \eta_1 C_1 \omega_1 \rightarrow C_2 \frac{T}{r_1} = C_1 \rightarrow C_1 = 24,438 \text{ Nm}$

$\omega_1 = 99 \text{ rad/s}$

$C_1 \omega_1 = \eta_2 C_H \omega_H \rightarrow C_H = \frac{C_1 T r_1}{\eta_2}$

$\frac{y-0}{8521=0} = \frac{x-3000}{2800-3000} \rightarrow -200y = 8,521x - 25516,2$

$\rightarrow x = 2400 \rightarrow y = 25,516 \text{ Nm}$

$W_{MAX} = 6420,5 \text{ W}$